

# Wave frequency estimation under low-wind conditions

XiFeng Wang

(Interdisciplinary graduate school of engineering sciences Kyushu University)  
(wangxf@riam.kyushu-u.ac.jp)

Kaoru Ichikawa

(Research Institute for Applied Mechanics Kyushu University)  
(ichikawa@riam.kyushu-u.ac.jp)

## 1. Introduction

Recent researches have proved the possibility of retrieving wave periods from altimeter normalized radar cross section ( $\sigma_0$ ) and significant wave height ( $H_s$ ), but all of the algorithms lost its precision in low wind speed condition.

We noted that buoy observations, always treated as "sea truth", ignored the high frequency portion of waves which significantly affects  $\sigma_0$  of altimeters. **These discrepancy of observations would affect wave period retrieval.**

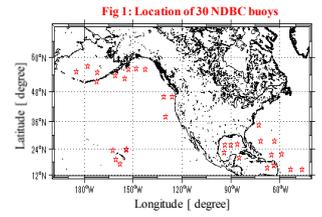
## 2. Data

Altimeter data: Jason2 GDR, 2008 ~ 2014

Buoy data: National Data Buoy Center (NDBC)

Collocation criteria: 50km & 30min

Number of collocated data: 4196



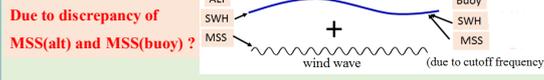
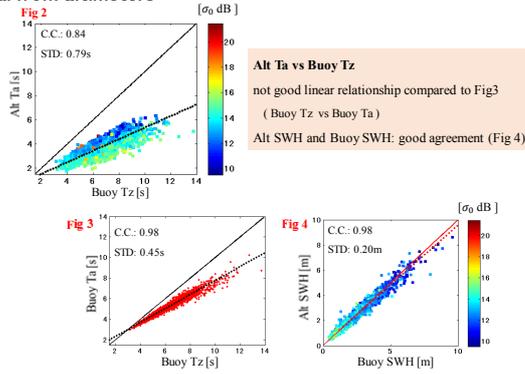
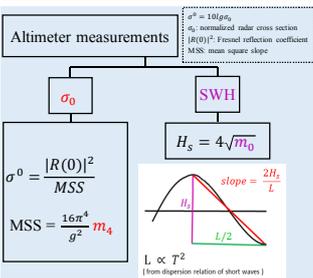
## 3. Rationale of wave period retrieval from altimeters

From buoy wave measurements  $S(f)$ :

$$H_s = 4\sqrt{m_0} \quad S(f): \text{ frequency spectrum}$$

$$T_z = \left(\frac{m_0}{m_2}\right)^{0.5} \quad m_n = \int f^n S(f) df$$

(mean zero-crossing wave period)



## Discrepancy of altimeter and buoy measurements

**Buoy:** NDBC buoys have upper cutoff frequency 0.485Hz ( $L \approx 6.6m$ ) due to buoy size et al.

**Altimeter:** dominated by waves whose lengths is longer than 3 times of incident wavelength ( $L \approx 6cm$ )

	SWH ( $m_0$ )		MSS ( $m_4$ )	
	ALT	Buoy	ALT	Buoy
mainly longer wave				
mainly short wave				
Low $\sigma_0$ (high wind)	wind wave	wind wave	wind wave	wind wave
High $\sigma_0$ (low wind)	swell	swell	wind wave	swell (due to cutoff)

Under high  $\sigma_0$  conditions, mss depend on short waves overlapped on swell, but MSS measured by buoys have no sensitivity to short waves and dominated by swell

## 4. Estimation of missing high frequency spectrum for buoys

Estimation of **missing MSS for high frequency** spectrum of buoys with wind wave equilibrium spectrum and saturation spectrum (Hwang, 2001)

$$MSS = \int_{k_1}^{k_2} k_1 b u_* g^{-0.5} k^{-0.5} dk + \int_{k_2}^{k_4} B k^{-1} dk$$

$u_*$ : friction velocity,  $u_* = \sqrt{C_d} u$

$u$ : wind speed,  $C_d$ : drag coefficient

$k_l = \max(0.95, k_p) rad \cdot m^{-1}$

[ for 6.6m limit ]

$k_u = 100 rad \cdot m^{-1}$

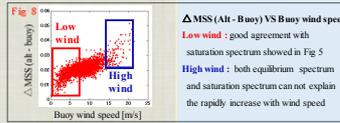
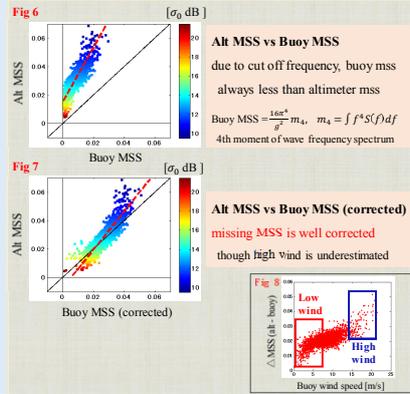
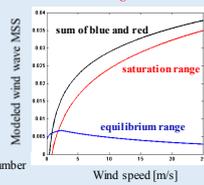
[ for 6cm limit ]

$k_p = \frac{g}{u_*^2}$  peak wavenumber

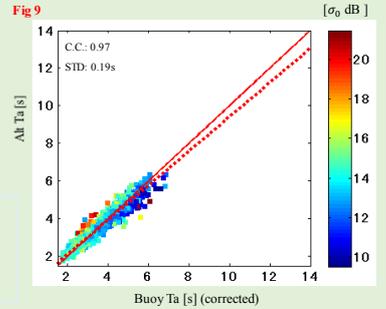
$k_1 = \left(\frac{g}{b}\right)^{1/2} \frac{1}{C_d} k_p$ , separation wavenumber

$b = 5.2 \times 10^{-2}$ ,  $B = 4.6 \times 10^{-3}$

$g$ : gravitational acceleration



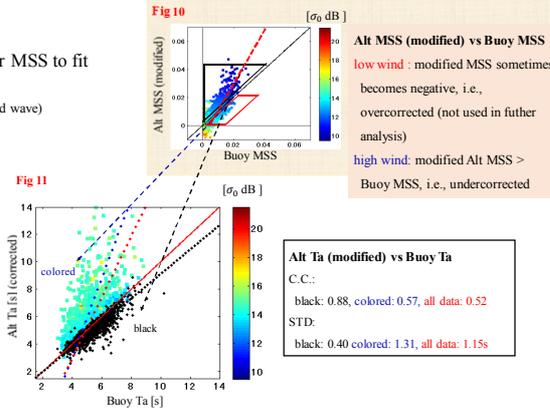
## Alt Ta vs Buoy Ta (corrected) compared to Fig 2, good agreement even in low wind conditions



## 5. Discussion

Conversely, can we modify altimeter MSS to fit practical buoy observations?

Assumption:  $MSS(\text{swell}) = MSS(\text{alt}) - MSS(\text{wind wave})$



For high wind conditions (black points), slightly better agreement w.r.t. Fig 2. For low wind conditions (colored points),  $T_a$  differences are large. Probably, because MSS ( $m_4$ ) is so small that  $T_a = \left(\frac{m_0}{m_4}\right)^{0.25}$  is sensitive to SWH ( $m_0$ )

## 6. Conclusion

Due to cutoff frequency, buoy measurements miss high frequency information of waves, which is necessary in MSS estimation. Through estimation of missing MSS for high-frequency portion of the wave spectrum using buoy wind speed, we found that :

- 1) corrected buoy  $T_a$  shows **good agreement** with altimeter  $T_a$  even under low wind conditions (Fig 9).
- 2) modification of altimetry MSS to fit buoy observations seems difficult, especially in low wind conditions.

## Reference:

Caires, S., Journal of Geophysical Research, Vol. 110, C02003, 2005  
Gommenginger, C.P., Srokosz, M.A. and Challenor P. G., Geophysical Research Letters, Vol. 30, no. 22, 2150, 2003  
Hwang, P.A. and Wang, D.W., Journal of Physical Oceanography, Vol. 33, pp: 1346-1360, 2001