# Experiments with Tidal Analysis of CryoSat-2 Altimetry in the Weddell Sea and on Adjoining Ice Shelves

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### Summary

- Tidal aliasing properties of the CryoSat-2 orbit have been analyzed, accounting for exact-repeat, near-repeat, and crossover periodicities as a function of spatial scale.
- With enough spatial averaging, the 8 largest tides,  $M_2$ ,  $S_2$ ,  $N_2$ ,  $K_2$ ,  $K_1$ ,  $O_1$ ,  $P_1$ , and  $Q_1$ , can be identified and mapped.
- A spatially-coupled harmonic analysis is used here, which combines harmonic time dependence with linear spatial dependence within a local tangent plane. The size of the tangent plane varies with latitude, from about 80km to 250km.
- Because of its high inclination, the CryoSat-2 orbit plane precesses slowly, and determinations of the  $K_1$  and  $K_2$  tides are less accurate.
- The largest source of "noise" in the tidal analysis is the small-scale variability of the mean ice surface, which must be estimated at scales much smaller than the tides.
- Tides inferred from CryoSat-2 are compared with tides from in situ GPS and bottom pressure recorders (King et al, 2011, and Padman's Antarctic Tide Database). CryoSat-2 tides agree with in situ measurements better than



**Figure 7:** Number of observations per 3.5-km×3.5km grid cell for  $Z_0$ , the mean surface.

Figure 8: Standard deviation of elevation within each grid cell defining the mean surface.

#### Removing the Mean Surface: LRM, SARin Mode and the Mean Surface

existing data-assimilative models for  $M_2$  and  $S_2$ , and, except for  $K_2$ , their accuracy is similar to the data-assimilative models for the smaller tides.

# Temporal Aliasing: Tidal Phase Sampling as a Function of Spatial Scale



Figure 1: Analysis domain. White circles indicate locations of GPS (King et al, 2011) and bottom pressure data (Padman's Antarctic Tide Database) used for model validation.





## **Cotidal Charts**



Figure 3: Histogram of sample interval for CryoSat-2 data within a 30 km-diameter disc at 70°S. Samples near  $\Delta t = 2$  days and  $\Delta t = 29$  days are associated with pseudo-subcycles. Samples near  $\Delta t = 6$  days and  $\Delta t = 20$  days are associated with intersecting ascending and descending tracks.

**Figure 4:** Phases of  $K_1$  (black) and  $K_2$  (red) sampled by CryoSat-2 within a 240 km  $\times$  30 km zonal patch in the Weddell Sea. Although the alias period of  $K_2$  is shorter than the alias period of  $K_1$ , CryoSat-2 frequently samples the  $K_1$  tide at two phases almost  $180^{\circ}$  apart.



Figure 9: The four largest tides mapped from CryoSat-2 data. The amplitude is shown with the color scale, and phase lines are shown in  $30^{\circ}$  increments.

### **Comparisons with GOT4.10c and CATS8a Models**



**Figure 10:** Comparison of the  $M_2$  and  $K_1$  tides from CryoSat-2 (color) versus CATS8a (white contours).

**Annual Cycle of Radar Cross Section?** 

Root-Mean Square Vector Error [cm] GOT4.10c CATS8a CryoSat-2







**Figure 11:** The annual cycle  $(S_a)$  mapped from CryoSat-2.

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Figure 6: Tidal harmonic constants computed from CryoSat-2 data along a section at 70°S. Analysis of data within large spatial bins (lines) is needed to sample tidal phases uniformly, as compared with **Figure 5:** Theoretical error correlation at analysis of data within small bins (dots). 70°S from the harmonic analysis matrix.

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