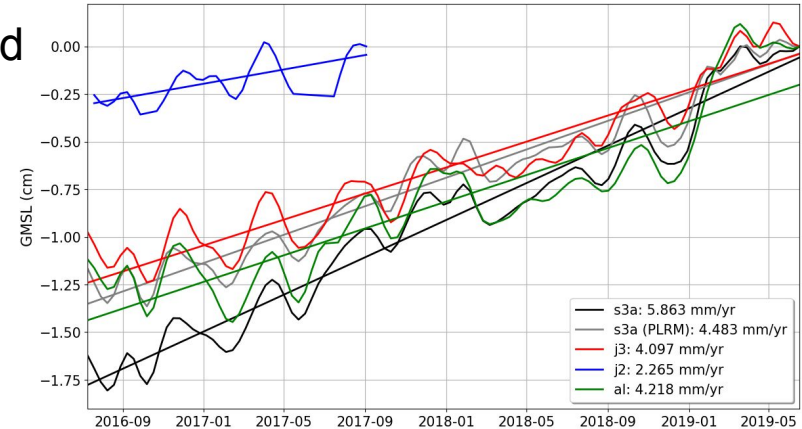


What sea-level drifts can be detected at global and regional scales by comparing recent altimetry missions together: S3A, Jason-3 and Saral-Altika?

OSTST | October 19-23, 2020 | Virtual Meeting

R.Jugier, R.Fraudeau, M.Ablain (MAGELLIUM)
M.Raynal, A.Guerou (CLS)
P. Femenias (ESA/ESRIN)

- GMSL evolution is well monitored with a good description of its error and uncertainties (Ablain et al. , 2019)
- However the description of potential GMSL drift on recent altimeter missions is quite challenging over short period (3-5 years).



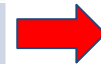
Objectif of this study is:

- To provide the global and regional MSL drift detection capability comparing recent altimeters missions (S3A, Jason-3 and Saral/Altika) and analysing the sensitivity of the method :
 - A focus on the detection of S3-A global and regional MSL drift using SAR-mode data is provided

- Method based on (*Ablain et al., 2019*)
 - The estimator of β with the OLS approach is noted $\hat{\beta} \sim (X^t X)^{-1} X^t y$
 - with the following distribution taking into account the error variance-covariance matrix :

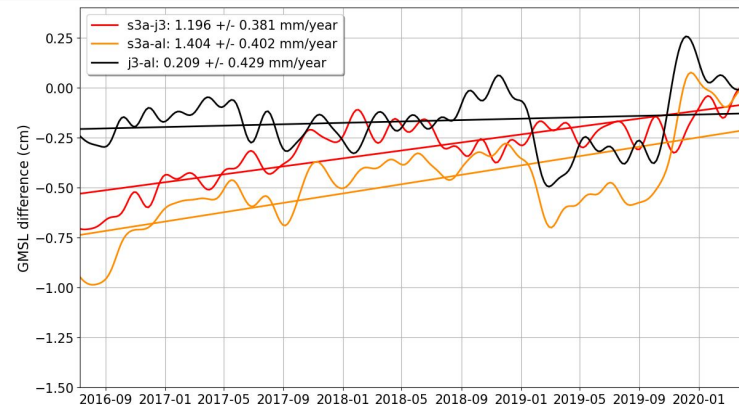
$$\hat{\beta} = N(\beta, (X^t X)^{-1} (X^t \Sigma X) (X^t X)^{-1})$$
- Σ derived from the error budget description
- HF and MF error variance are computed directly from the GMSL difference signal :
 - GMSL computed with AVISO method from Marine L2P products
 - Comparison of GMSL time series after interpolation on the same time sample (usually using the Topex-Jason mission cycles as reference periods)

Source of errors	Error category	Jason-2/3 GMSL uncertainty level (1σ)	GMSL differences Uncertainty level (at 1σ)
High frequency errors: altimeter noise, geophysical corrections, orbits ...	Correlated errors ($\lambda = 2$ months)	$\sigma = 1.2$ mm	σ between 0.6 and 0.8 mm (depending on altimeter missions)
Medium frequency errors: geophysical corrections, orbits ..	Correlated errors ($\lambda = 1$ year)	$\sigma = 1$ mm	σ between 0.5 and 0.7 mm (depending on altimeter missions)
Low frequency errors: wet tropospheric correction (WTC)	Correlated errors ($\lambda = 5$ years)	$\sigma = 1.1$ mm (\Leftrightarrow to 0.2 mm/yr for 5 years)	$\sigma = 0$ (model WTC error are cancelled between 2 missions)
Low frequency errors: orbits (Gravity fields)	Correlated errors ($\lambda = 10$ years)	$\sigma = 0.5$ mm (\Leftrightarrow to 0.05 mm/yr for 10 years)	$\sigma = 0.5$ mm * sqrt(2)
Long-term drift errors: orbit (ITRF) and GIA	Drift error	$\delta = 0.12$ mm/yr	$\delta = 0.1$ * sqrt(2) (GIA error is removed between 2 missions)

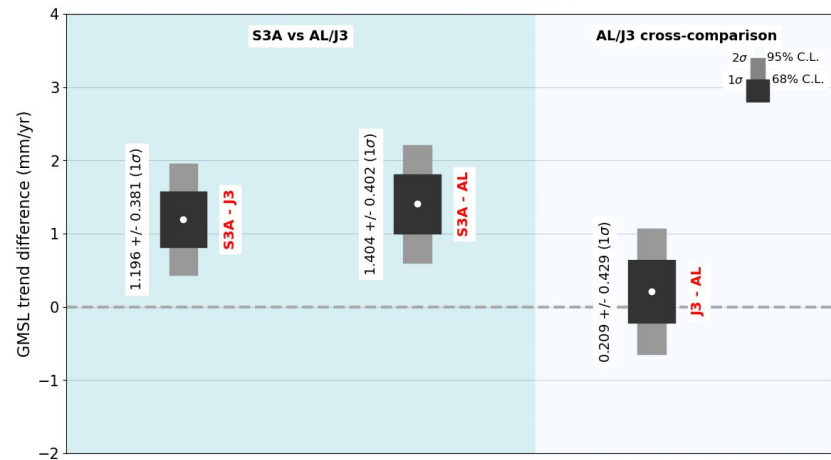


GMSL drift uncertainty

- Drifts and uncertainties on S3A compared to J3 and AL (period 07/2016 to 04/2020) :
 - No significative J3 vs AL drift makes for a strong basis for comparison with S3A
 - S3 vs J3 and AL both find approx **1.3 ± 0.4 mm/yr drift (68% C.L.)**
- Data updated from *Ablain, OSTST, Chicago, Oct. 2019* :
 - + 1 year period
 - reprocessing with more homogeneous data
- The origin of this drift has been explained by altimetry experts (see J.Aublanc, OSTST 2020)

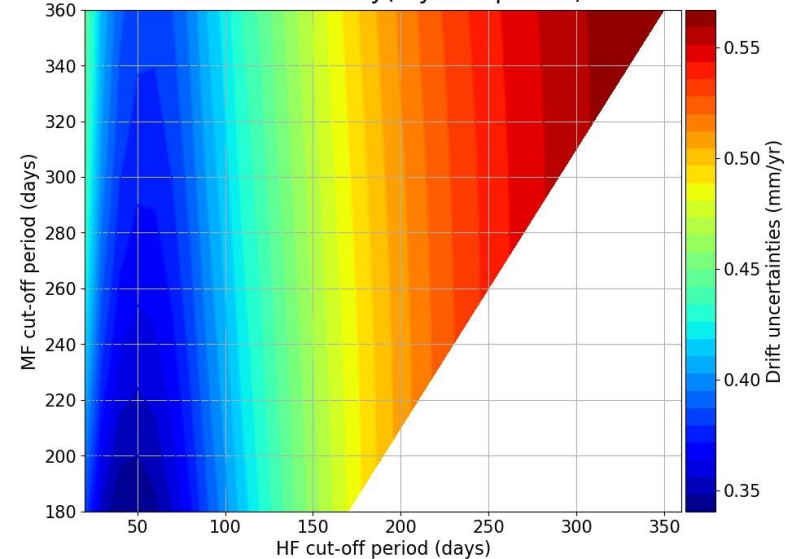


S3A GMSL trend differences vs AL/J3 using model WTC
Period: 07/2016 to 04/2020



- The sensibility of error budget has been studied for high frequency errors
-
- Uncertainties are computed for different HF and MF cut-off frequencies :
 - Low impact from the variation of the MF frequency.
 - Variations of the HF period has a high impact on the computed uncertainties for short time periods : up to 25%.
 - The currently chosen periods HF = 2 months and MF = 1 year correspond to a minimum in estimated uncertainties.

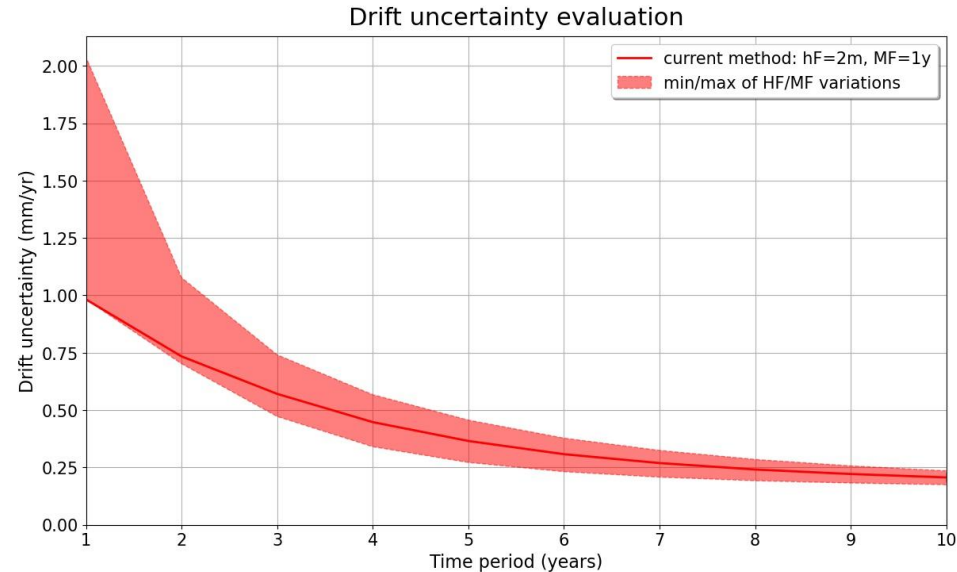
HF and MF cut-off frequency choice impact on estimated drift uncertainty(4 years period)



Uncertainties computed for a time period of 4 years, for different HF and MF cut-off frequencies.

HF variance is computed as the variance of the residue from a low-pass Lanczos filter at the HF frequency. MF variance is computed as the variance of the difference of the residue from a low-pass Lanczos filter at the MF freq. and the signal filtered at the HF freq.

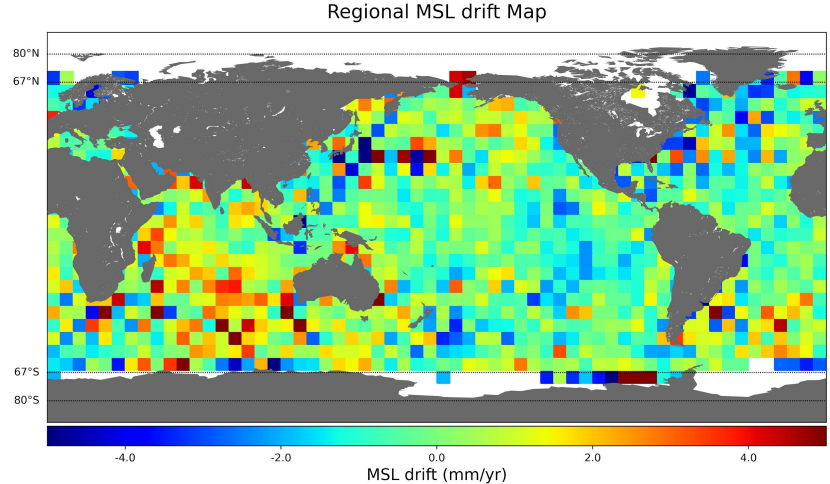
- Uncertainties evaluated for :
 - current method with frequencies HF=2m and MF=1y
 - all combinations of frequencies HF in [2m, 1y] and MF in [6m, 1y]
- For time periods < 3y :
 - current method (HF=2m, MF=1y) is the least conservative i.e. yields lower uncertainties than other combinations
- At 3y, drift unc. between [0.5, 0.75] mm/yr
- At 5y, drift unc. between [0.25, 0.4] mm/yr
- At 10y, drift unc. < 0.25 mm/yr
- A more robust approach must be devised for short time periods



Min/max of uncertainties computed for all HF variations between 2 months and 1 year and all MF variations between 6 months and 1 year, for different time periods.

Regional MSL drift uncertainty

- Regional MSL drift and associated uncertainties have been analyzed at regional scales
- From experience, regional drifts in altimetry are very difficult to detect by such a direct approach because of the ocean variability that is not observed in the same way
- Such an approach is especially effective between the tandem phase
- However, our intention is to quantify precisely the level of uncertainty reached as a function of the period duration and also of the size of the regional area analysed by the direct method.



*Regional MSL trend differences between S3A and J3:
are there significant ?*

Regional MSL drift uncertainty

- Same method than the one used at global scale, based on (*Ablain et al., 2019*)
- HF and MF errors computed directly from regional MSL signals
- Low frequency (WTC) and long-term drift errors (orbit, GIA) values taken from *Prandi et al. 2020*

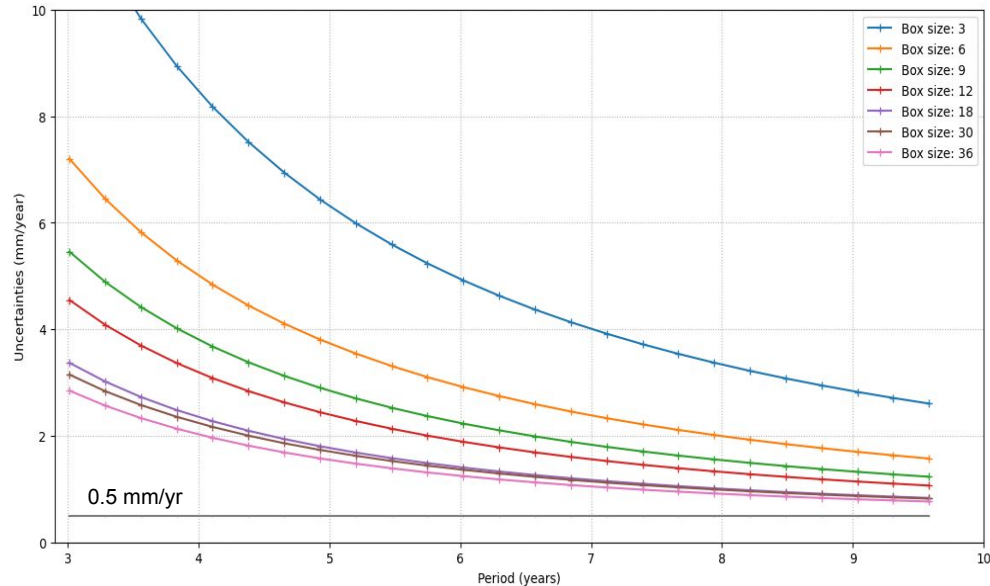
Source of errors	Error category	Jason-2/3 GMSL uncertainty level (1σ)	GMSL differences Uncertainty level (at 1σ)
High frequency errors: altimeter noise, geophysical corrections, orbits ...	Correlated errors ($\lambda = 2$ months)	location dependent	location dependent
Medium frequency errors: geophysical corrections, orbits ..	Correlated errors ($\lambda = 1$ year)	location dependent	location dependent
Low frequency errors: wet tropospheric correction (WTC)	Correlated errors ($\lambda = 5$ years)	location dependent	$\sigma = 0$ (model WTC error are cancelled between 2 missions)
Long-term drift errors: orbit	Drift error	$\delta = 0.33$ mm/yr	$\delta = 0.33 * \sqrt{2}$ mm/yr
GIA	Drift error	location dependent	$\delta = 0$ mm/yr (GIA error is removed between 2 missions)



From Prandi et al. 2020 (submitted)

Regional MSL drift uncertainty

- Uncertainties evaluated for different box sizes and different time periods
- HF and MF variance is computed from S3/J3 but results for other missions are very similar
- Regional drifts under 2 mm/yr can be detected for time periods of over :
 - 4.5 years for box sizes $\geq 18^\circ$
 - 6 years for box sizes $\geq 12^\circ$
 - 8 years for box sizes $\geq 6^\circ$
- Regional drifts under 1 mm/yr can be detected for time periods of over 8 years for box sizes $\geq 18^\circ$
- The C3S requirement of detecting 0.5 mm/yr drifts at regional scale is not achievable using this method over a mission's life cycle.

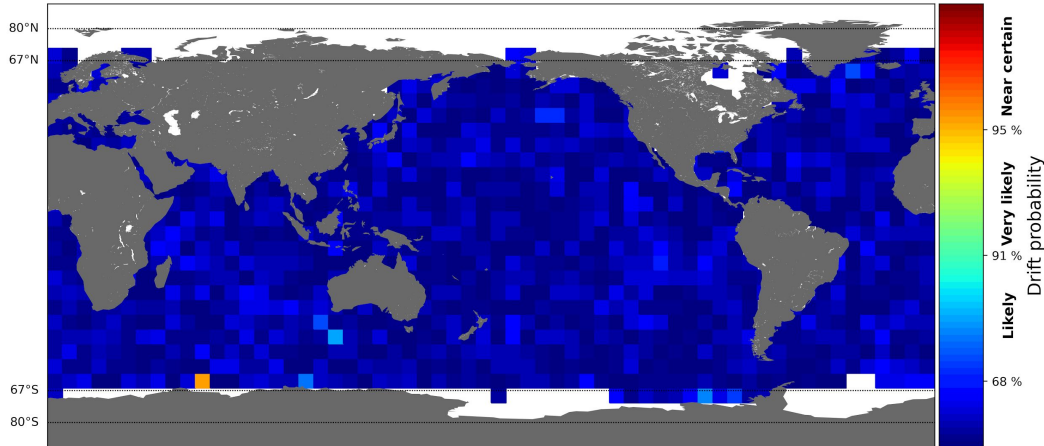


Evolution of uncertainties depending on the mission period for different box sizes (from $3^\circ \times 3^\circ$ to $36^\circ \times 36^\circ$).

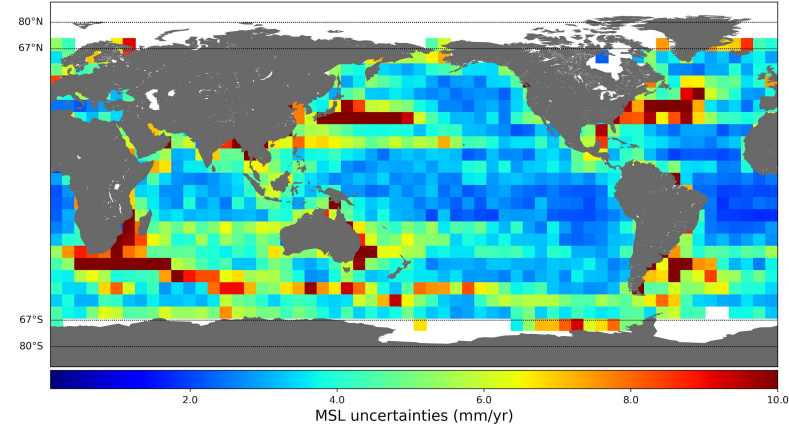
Regional MSL drift uncertainty

- Regional MSL drift and uncertainties, and drift probability are evaluated on S3A/J3, for box sizes of 6° , represented as deviation from the mean GMSL S3A/J3 drift.
- Zones with high computed drifts also have high drift uncertainties : simply a reflexion of high ocean variability in those zones.
- Method accuracy insufficient to detect regional drifts on S3A/J3.

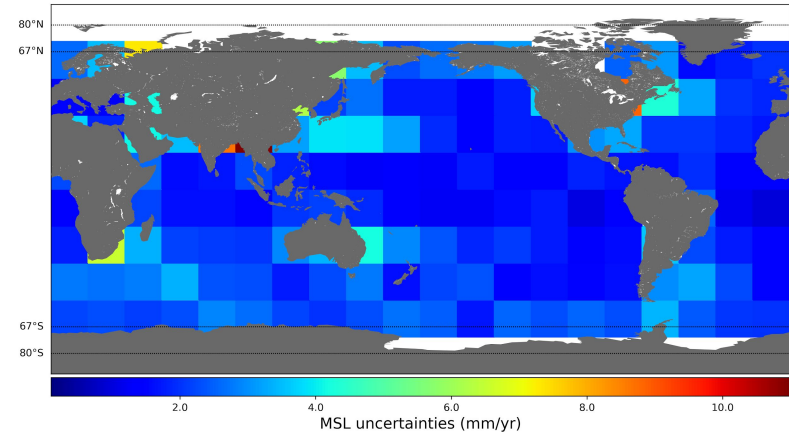
Drift probabilities on s3a/j3 with 6° boxes



Regional MSL uncertainties Map: 6° boxes



Regional MSL uncertainties Map: 18° boxes



- The GMSL comparison between recent altimeter missions highlights a significant S3A GMSL (based on SAR mode) drift from 07/2016 to 04/2020 compared to SARAL/Altika and Jason-3:
 - ◆ +1.3 mm/yr with an uncertainty of 0.4 mm/yr (68% confidence level)
 - ◆ no significant drift detected between Jason-3 and SARAL/Altika
 - ◆ Cross-comparisons with S3B GMSL have also been performed but results must be consolidated.

- Our uncertainty estimation is sensitive to the error budget allocated especially at high frequencies and for short period lower than 3 years:
 - ◆ An improved and more robust approach is contemplated in order to better estimate uncertainties over short periods of time and thus help detect drifts quicker.

- Regional scales :
 - ◆ Regional drifts ≤ 1 mm/yr can be detected for time periods of over 8 years at 2000 km spatial scale
 - ◆ Detection of drift lower than 0.5 mm/yr as expressed by C3S requirements is impossible at regional scale : **new calibration method must be foreseen to be able to verify this level of requirement (see Ablain presentation, error session or <https://www.essoar.org/doi/10.1002/essoar.10502856.1>)**