

# Intra-1 Hz Correlations **Graham Quartly<sup>1</sup>**, Walter Smith<sup>2</sup> & Marcello Passaro<sup>3</sup> 1 - PML; 2 - NOAA; 3 - DGFI-TUM







Slope = 0.1211; r2 = 0.48732



*Example of 20 Jason-3 estimates in a 1 Hz record, and a scatter* plot of those observations.

### **Improving Sigma0**

For the MLE-4 processing algorithm, there is a strong correlation between  $\sigma^0$  and  $\psi^2$ . Quartly (2009) showed that for the initial processing of Jason-2 data, the proportionality constant,  $\alpha$ , was 11.34. Thus, a more even series of  $\sigma^0$  values was given by defining an "adjusted value",  $\sigma_{adj}^0 = \sigma_{MLE4}^0 - \alpha \psi^2$ . We would normally expect the along-track  $\sigma^0$  variation to be smooth, as 20 Hz values are spaced every 330 m and correspond to a measurement over a disk ~8km across.



However, the appropriate value for the current Jason-2 processing, and for Jason-3 is  $\alpha$ =11.0. This probably reflects a change in the fitted model e.g. a more realistic representation of the PTR (point target response). Segmenting a according to different wind-wave conditions, we find that it varies slightly with  $\sigma^0$ , being a little higher in very calm conditions.

## Introduction

For a conventional radar altimeter operating over a homogeneous surface, the expected shape of a waveform is well known, with various models and numerical algorithms being used to extract the geophysical parameter of interest: epoch (giving range and thus SSH), wave height (H<sub>s</sub>), amplitude ( $\sigma^0$ ), and, for some, a mispointing angle (termed  $\psi^2$ ). However, the echo from a single pulse suffers from incoherent summation of reflections from different facets; on-board averaging in groups of 90 produces a shape akin to the Brown model, but with clearly visible Rayleigh (fading) noise. Provided the on-board retracker kept the reception window in exactly the right place, averaging hundreds of these together would give a shape close to the ideal.

However, in many cases, we are interested in the small scale variations of the parameters, e.g. to look at coastal currents, to infer bathymetry, or to study SSH spectra. Consequently all high-resolution geophysical estimates are affected by the Rayleigh noise on the waveforms.

As a number of parameters are determined from the same noisy data, there can be correlations in the biases of these estimates. This poster investigates these correlations and suggests how they may be used to provide better estimates



Example of 20 Jason-3 estimates in a 1 Hz record, and a scatter plot of those observations. (Note range had to be detrended otherwise *it is dominated by an orbit term.*)

### **Improving SSH ?**

Sandwell & Smith (2005) had shown that retrackers such as MLE-4 produce correlated errors in range and H<sub>s</sub>. Both range and Hs are estimated principally from the bins on the leading edge. The range term is rapidly changing, as the altimeter is approaching to or receding from the Earth; thus the correlation is better shown using detrended values. Processing a large number of 1 Hz data shows the constant of proportionality to have a mean ( $\beta$ ) of 0.099, but with a wide interquartile range.



Actually,  $\beta$  varies with the slope of the leading edge, with slightly lower values at low  $H_s$ . We can produce an adjusted value for SSH using a variable value for  $\beta$ :  $h_{adi} = h_{MLE4} + \beta(Hs)$ . Hs

### Implementation

Series of 200 consecutive estimates of pseudo-SSH (blue - MLE-4; green - adj.; red - MLE-3; cyan - MLE3 (adj))

MLE-4 (orig) – MLE-4 (adj) – MLE-3 (orig) – MLE-3 (adj) –

### **Different altimeters** & retrackers

The GDRs for Jason-3 also provide estimates determined using an MLE-3 model. As a different overall set of free parameters is being used, the observed correlation between range and H<sub>s</sub> is different  $(\beta_3=0.090)$ . The procedure can be applied to other altimeters, different operating frequencies, and with the use of different retrackers. All yield different proportionality constants, showing that this relationship is dependent upon the instrument and the retracker.



shown as a function of  $H_S$ .

### **Different altimeters**

AltiKa, the first Ka-band altimeter, has a different shaped mean waveform, due to narrower antenna beamwidth and shorter reception Unsurprisingly, use of an MLE-4 model shows strong bins. correlations between  $\sigma^0$  and  $\psi^2$ ; in this case,  $\alpha = 8.4$ . However the spread of values is much wider than for the Ku-band altimeters.





### Series of 200 consecutive estimates of $\sigma^0$ (blue - MLE-4; green - adj.; red - MLE-3).

100 Consecutive waveforms

In the above plots a simple global adjustment is applied --  $\alpha.\psi^2$  or  $\beta.H_s$  respectively, leading to smoother more realistic along-track profiles, with absolutely no filtering. In the case of  $\sigma^0$ , the result is almost akin to the output of the MLE-3 retracker, which has a preset value for  $\psi^2$ , whereas for range, dependencies are noted for both MLE-4 and MLE-3, and both can be separately corrected, leading to a clear reduction in the 1 Hz values of S.D. (range).



Improvement in  $\sigma_h$ , after simple adjustment to Jason-3 ranges.



Improvement in AltiKa range after simple adjustment. Lines are offset to show reduction in small-scale variability.

### **Applications & Implications**





*Relationship between Jason-3's Ku- and C-band values* for  $\sigma^0$ . (top) Mean difference in narrow  $\sigma^0$  bins (bottom) Scatter (i.e. S.D. about mean)

3) Improved spectra. Power spectra of  $\sigma^0$  variations are much lower for  $\sigma^{0}_{adj}$  than  $\sigma^{0}_{MLE4}$  at short scales. This is achieved on the 20 Hz data without any along-track smoothing.

altimeters was improved by a factor of 3 once  $\sigma^0$  values were adjusted.

There have been several applications of this adjustment, and it

1) Rain-flagging. The dual-frequency rain-flagging (based on

2) Inter-calibration. Comparison of Jason-1 and Jason-2

can be applied at 1 Hz, without the need to "correct" all the individual

the close connection of observations at Ku- and C-band) was

unworkable with MLE-4 data. A much tighter relationship was found

using  $\sigma^{0}_{adj}$ ; results using  $\sigma^{0}$  from the MLE-3 fitter (which does not

allow  $\psi^2$  to vary) were almost as good as for  $\sigma^0_{adj}$ .



*Comparison of Jason1 & Jason-2*  $\sigma^{0}_{Ku}$  *measurements:* (left) MLE-4, (right) Adjusted values. The scatter for the latter is one third of that for MLE-4 values

The values for  $h_{adj}$  are more consistent than  $h_{MLE4}$  (lower  $\sigma_h$ ), have less small-scale noise. What needs to be tested is whether this adjustment improves the agreement between Jason-2 and Jason-3 during their tandem phase. Also, does the reduction in  $\sigma_h$  lead to an increased ability to detect bathymetric features (obtained via double differentiating the SSH values along track)

This applied "correction" changes SSH values by tens of centimetres, depending upon  $H_s$ . This is very much a property of the retracking algorithm, and thus corresponds to the "tracker bias" component of SSB (sea state bias). Consequently, if applied for ocean studies, it would need a corresponding adjustment to be made to the SSB correction (which is an empirical adjustment at the large scale).



Improvement in Jason-3 range spectra after simple adjustment. (This corresponds to a redcution of the high-frequency noise *component by a factor of 1.7)* 

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Application

20 Hz values.







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