#### Accounting for observation error correlations in the assimilation of data from the future SWOT High-Resolution altimeter mission

Emmanuel Cosme<sup>1</sup>, Giovanni Ruggiero<sup>2,3</sup>, Jean-Michel Brankart<sup>2</sup>, Clément Ubelmann<sup>4,5</sup>, Julien Le Sommer<sup>2</sup>

<sup>1</sup>: UGA/LGGE, France <sup>4</sup>: NASA/JPL, USA

<sup>2</sup>: CNRS/LGGE, France <sup>5</sup>: now at CLS, France <sup>3</sup>: now at Mercator Océan, France

G. Ruggiero was funded by the CNES/TOSCA program.











## Summary

- We use the portable ocean SWOT simulator<sup>1</sup> to quantify spatial correlations of errors in the future SWOT observations;
- We develop and implement a method to account for these correlations in the assimilation of (reduced-resolution) SWOT data;
- We conclude that accounting for error correlations is essential to accurately assimilation SWOT observations.

<sup>1</sup> Gaultier et al, 2016, <u>https://github.com/SWOTsimulator</u>

## Why observation error correlations matter for data assimilation?

Because we need the observation error covariance matrix to assimilate the observations.

An assimilation algorithm seeks the best compromise between a prior estimate and the observations by minimizing a cost function:

$$\mathcal{J}(\mathbf{x}) = \operatorname{SomeNorm}(\mathbf{x} - \mathbf{x}^{\operatorname{prior}}) + [\mathbf{y} - \mathcal{H}(\mathbf{x})]^T \mathbf{R}^{-1} [\mathbf{y} - \mathcal{H}(\mathbf{x})]$$
Observations-model
difference
observation error

covariance matrix

## Challenges

- I. We must estimate the observation error covariance matrix.
- 2. What we actually need is the inverse of the observation error covariance matrix.

$$\mathcal{J}(\mathbf{x}) = \operatorname{SomeNorm}(\mathbf{x} - \mathbf{x}^{\operatorname{prior}}) + [\mathbf{y} - \mathcal{H}(\mathbf{x})]^T \mathbf{R}^{-1} [\mathbf{y} - \mathcal{H}(\mathbf{x})]$$
Observations-model
difference
observation error
covariance matrix

## Challenge I: estimating the matrix



We perform 5000 realizations of SWOT errors with the simulator.

point

A realization of **SWOT** errors



# Challenge 2: using the matrix in the assimilation algorithm

The observation error covariance matrix is **too big to be inverted** numerically.

In large systems (meteorology, oceanography), it is considered diagonal. Actually, the design of usual data assimilation systems is based on this approximation.

To alleviate the detrimental effects of this approximation, common (but not satisfactory) solutions are:

- to rule out observations when they are suspected of correlated errors,
- inflating the error variances (diagonal of the matrix).

### Challenge 2: what we propose

Introduce a transformation of the observations:

 $\mathbf{y}^+ = \mathbf{T}\mathbf{y} \qquad \mathcal{H}^+ = \mathbf{T}\mathcal{H}$ 

Note the error covariance matrix  $\mathbf{R}^+$ 

#### Then

$$\begin{bmatrix} \mathbf{y}^{+} - \mathcal{H}^{+}(\mathbf{x}) \end{bmatrix}^{T} \mathbf{R}^{+-1} \begin{bmatrix} \mathbf{y}^{+} - \mathcal{H}^{+}(\mathbf{x}) \end{bmatrix} = \begin{bmatrix} \mathbf{y} - \mathcal{H}(\mathbf{x}) \end{bmatrix}^{T} \mathbf{R}^{-1} \begin{bmatrix} \mathbf{y} - \mathcal{H}(\mathbf{x}) \end{bmatrix}$$

$$\mathbf{T}^T \mathbf{R}^{+-1} \mathbf{T} = \mathbf{R}^{-1}$$

Brankart et al, 2009

## Challenge 2: what we propose

We introduce  

$$\mathbf{T} = \begin{pmatrix} \mathbf{I} \\ \delta_a \\ \delta_c \\ \delta_c^2 \\ \delta_a^2 \\ \delta_c^2 \\ \delta_a^2 \\ \delta_c^2 \end{pmatrix} - \text{Derivative along-track and across-track}$$

and find  $\mathbf{R}^+$  (diagonal) that minimizes the matrix norm

$$\left\| \mathbf{R} (\mathbf{T}^T \mathbf{R}^{+-1} \mathbf{T}) - \mathbf{I} \right\|_F^2$$

Ruggiero et al, 2016

## Results

Correlations with this point



## Results

#### Residual error after analysis (based on 180 analyses)

#### With diagonal R



#### Simulating the correlations



**SWOT** observations

#### Residual error after analysis

Results

#### With diagonal R

Simulating the correlations

With diagonal R, inflated variances











#### What we should have



### Conclusions and discussions

 Accounting for error correlations is essential to accurately assimilate SWOT observations, and we propose a method to do so (Ruggiero et al, JTECH, in press).

- Need to get rid of the uncorrelated KaRIn instrumental error to use the full resolution of SWOT (we are developing denoting techniques);
- The method is applicable to nadir altimetry (using along-track derivatives). Useful?
- The method can be complemented with online diagnostics (Desroziers et al, 2005) to improve the representation of the observation error covariance matrix.

### why error correlations matter?



Brankart et al, 2009