

Leveraging Delay-Doppler altimetry for Enhanced Sea-State Characterization

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¹CLS, France

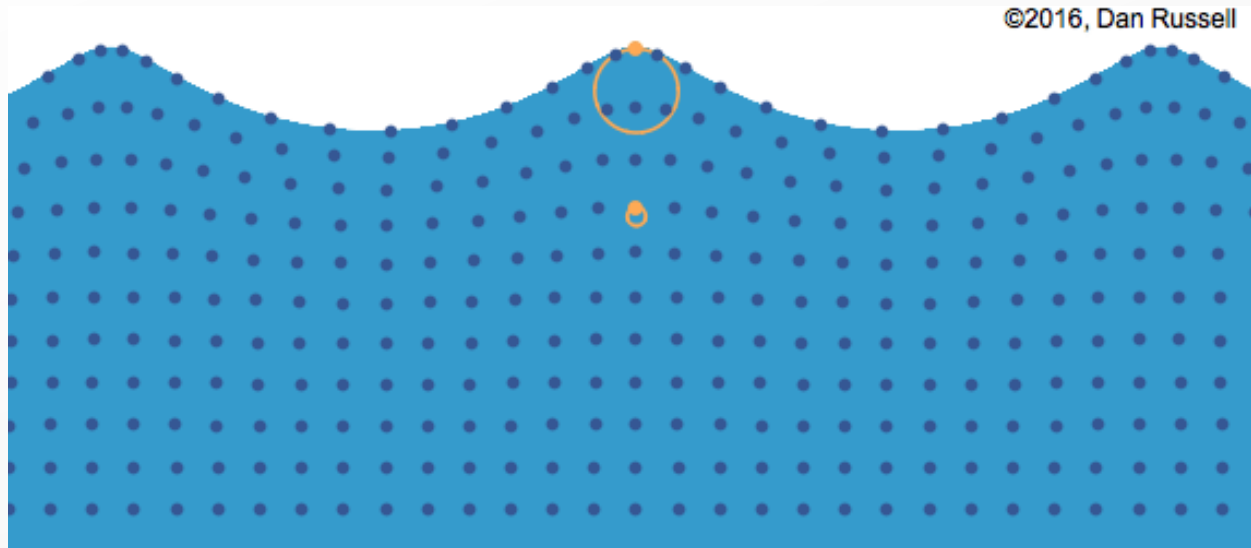
²CNES, France

³University of Maryland, USA

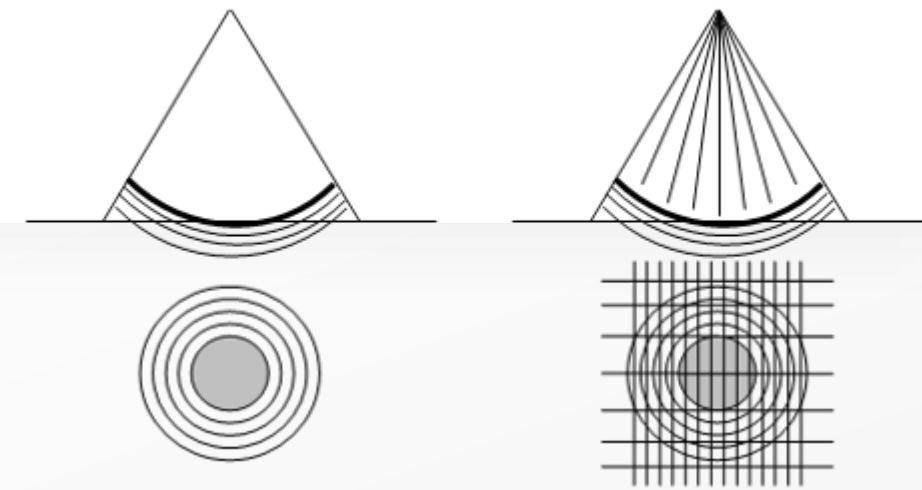
⁴IFREMER, France

Delay-Doppler: Limitations so far

Since the Delay-Doppler uses the Doppler effect to locate the signal along-track, it is impacted by the ocean dynamics, and **particularly the waves and their wind-driven contribution**.



Noise? Or new sea state variable!



The bigger impact is due to **the variation of the vertical component of the waves velocity weighted with radiometry** over the footprint. This quantity can be directly linked to the waves second momentum:

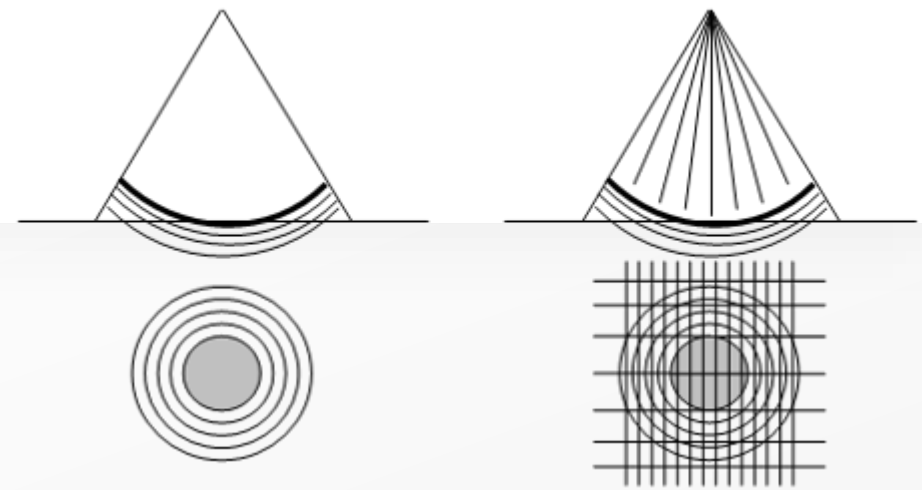
$$\sigma_v^2 = m_2 = \int_0^{+\infty} \omega^2 S(\omega) d\omega$$

where $S(\omega)$ is the power density spectra of the sampled ocean area. Using the standard SWH and mean zero-crossing wave period T_{02} , it can be rewritten as:

$$\sigma_v = \frac{\pi}{2} \frac{SWH}{T_{02}}$$

Delay-Doppler: Limitations so far

Since the Delay-Doppler uses the Doppler effect to locate the signal along-track, it is impacted by the ocean dynamics, and **particularly the waves and their wind-driven contribution.**



Another impact is due to the Doppler due to horizontal wave-facets motions weighted by their radiometry. This can be written as **the along-track projection of the Stokes drift**, weighted by the mean square slope (MSS):

$$u_x \sim \frac{U_{Stokes}}{2 MSS} \cos(\phi_{Stokes} - \phi_{sat})$$

Taking advantage of the wind dependency of the Stokes drift and MSS, it can be fitted with the following formula:

$$u_x \sim A(U_{10}) \cos(\phi_{wind} - \phi_{sat}) + B(U_{10})$$

Noise? Or another sea state variable!

Transforming noise into wind and waves variables

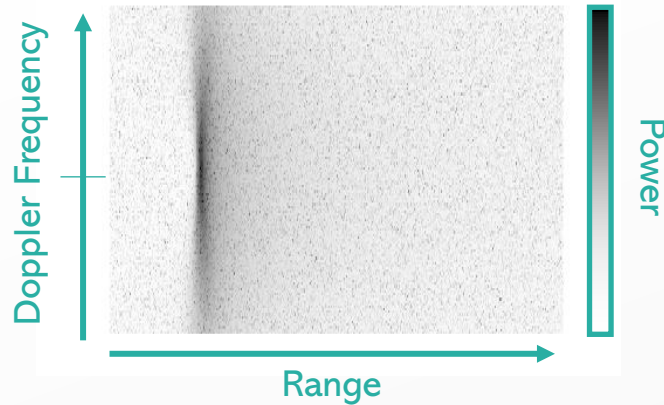
Presenting our new Sentinel-6HR 5-parameter product!
January–June 2022 and January–June 2024

- ❖ **Removing the major sea-state-dependent biases**
Aligning Delay-Doppler with Low Resolution Mode (LRM) altimetry without Look-Up Table or ERA5 inputs
- ❖ **High-Resolution (~ 300 m) along-track**
For coastal areas, extreme events or wave-topography disentanglement
- ❖ **Offering two new sea-state variables**
Related to wave period and wind speed
- ❖ **Soon (by summer 2026) available on Aviso!**



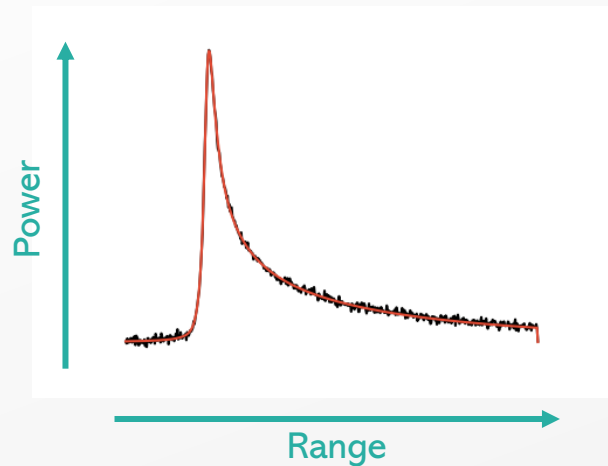
Leveraging Delay-Doppler altimetry

After the L1B processing and range migration correction, for each ground point, we get a “stack” of Doppler looks:



Currently not directly used

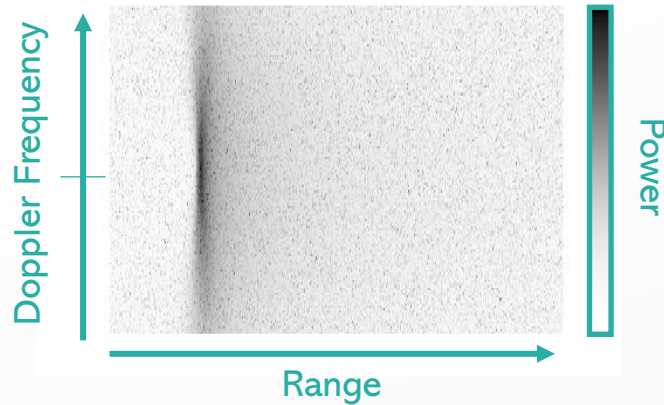
In the current operational chain, the Doppler looks are summed to get the multilook waveform, which is then retracked:



Numerical retracking: using the real Point Target Response
3 parameters : Epoch, Amplitude and SWH

Leveraging Delay-Doppler altimetry : “2-Dimensional retracking”

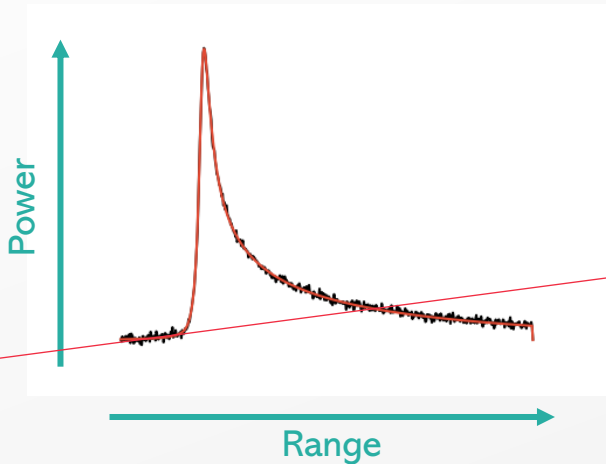
After the L1B processing and range migration correction, for each ground point, we get a “stack” of Doppler looks:



Numerical “2-Dimensional” retracking: using the real Point Target Response
5 parameters : Epoch, Amplitude, SWH, σ_v and u_x

Now using all available information

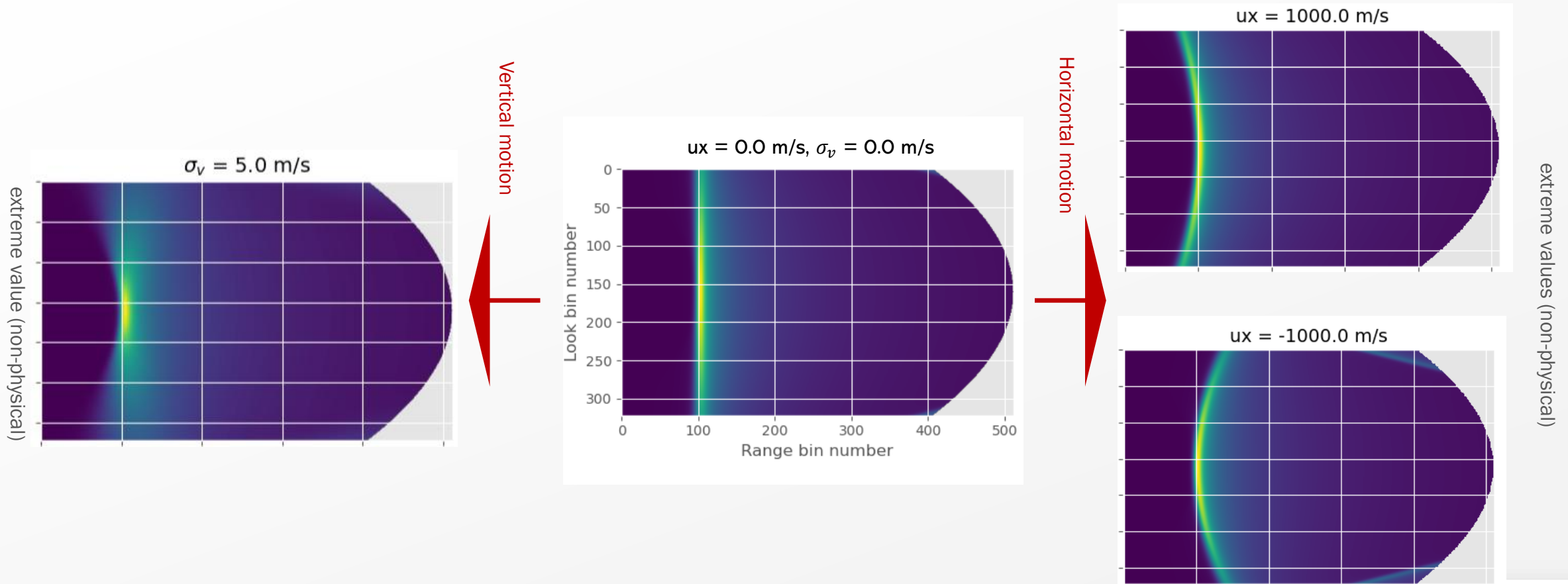
In the current operational chain, the Doppler looks are summed to get the multilooked waveform, which is then retracked:



Numerical retracking: using the real Point Target Response
3 parameters : Epoch, Amplitude and SWH

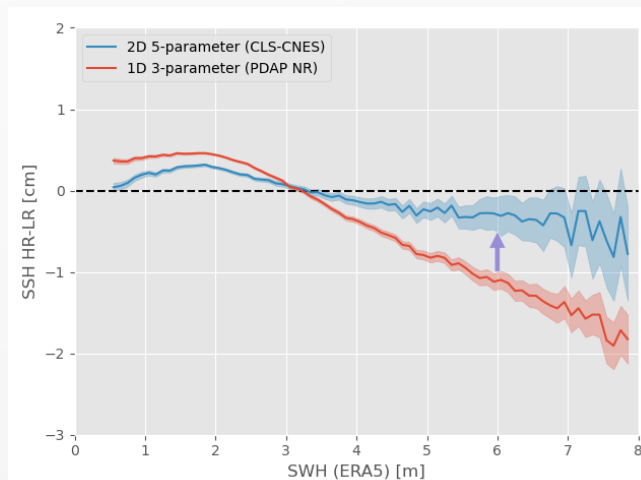
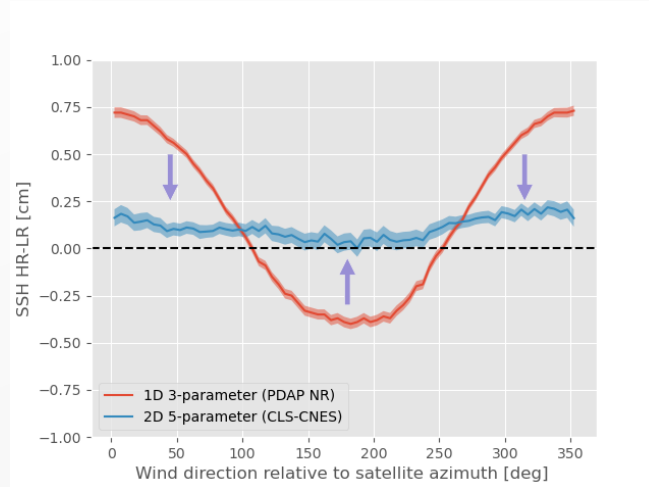
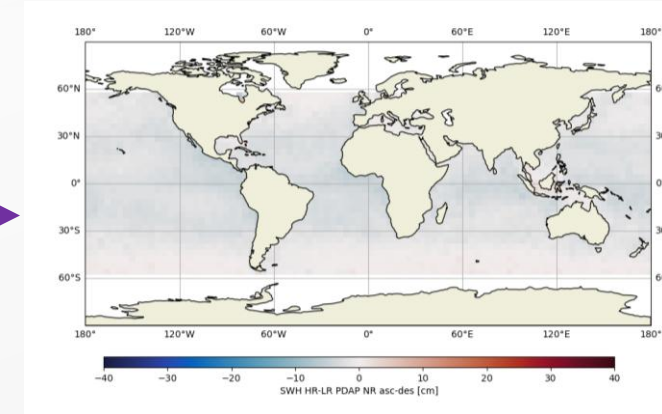
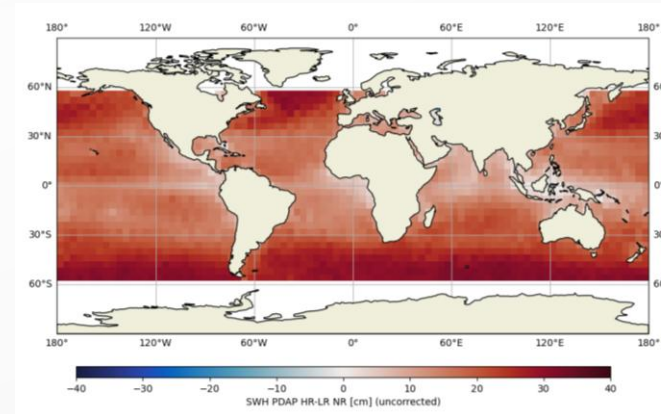
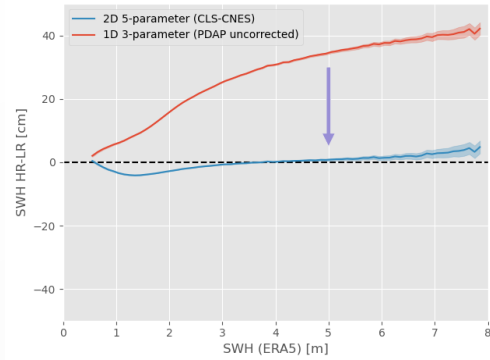
Leveraging Delay-Doppler altimetry : “2-Dimensional retracking”

Retracking the full stack instead of the multilook allows us to constrain the surface motion:



Resolving the biases: alignment with LRM without any Look Up table

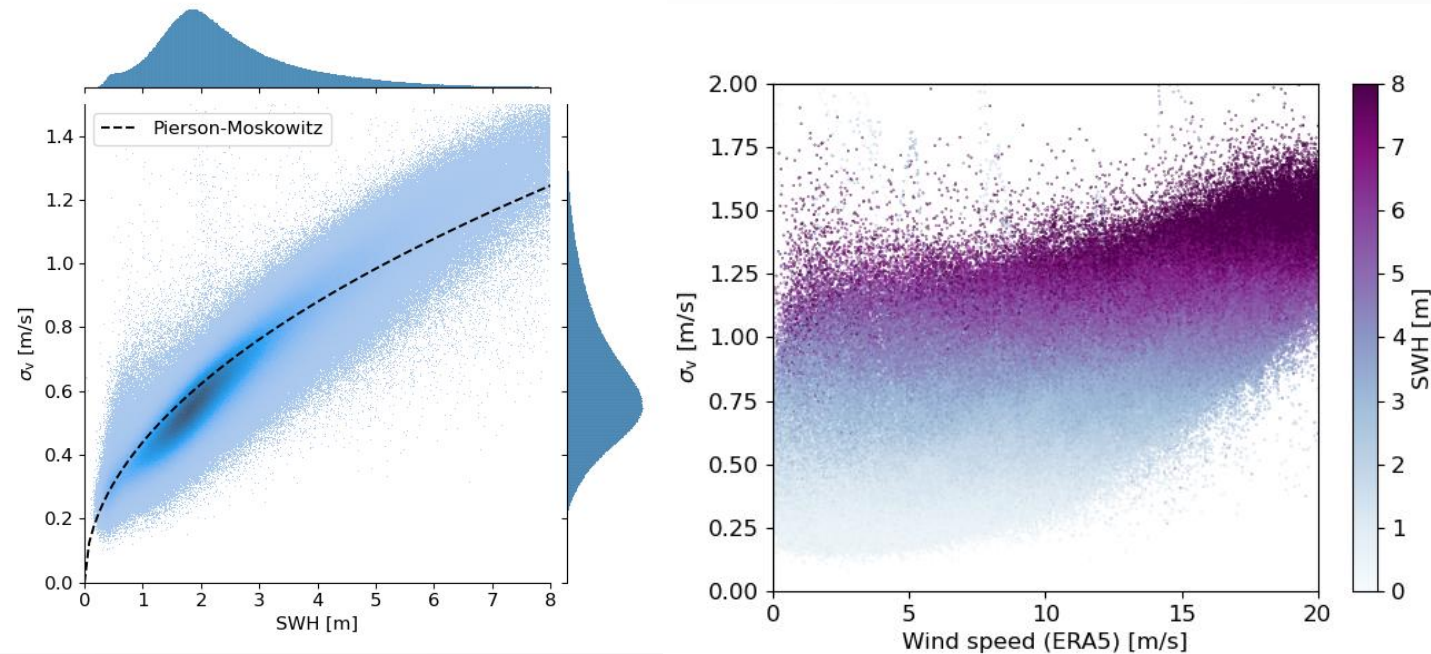
Removing the overestimation of the waves heights



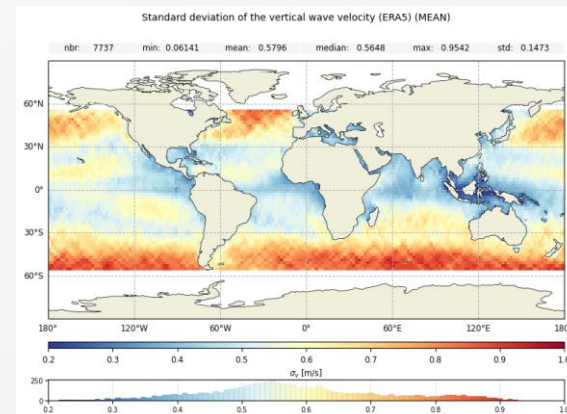
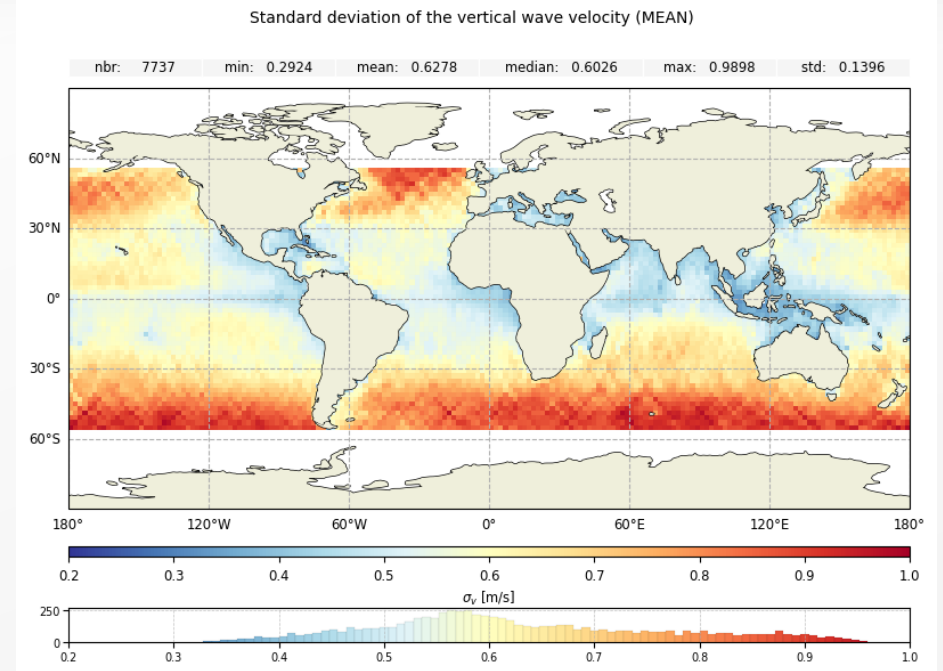
Removing the wind (and wave)-dependent SSH bias

Retrieving new variables: characterizing ocean dynamics

Wave vertical velocity standard deviation σ_v



The vertical velocity variance is **correlated to both the significant wave height and wind speed**, roughly as expected by the theoretical wave spectrum models for a fully-developed sea



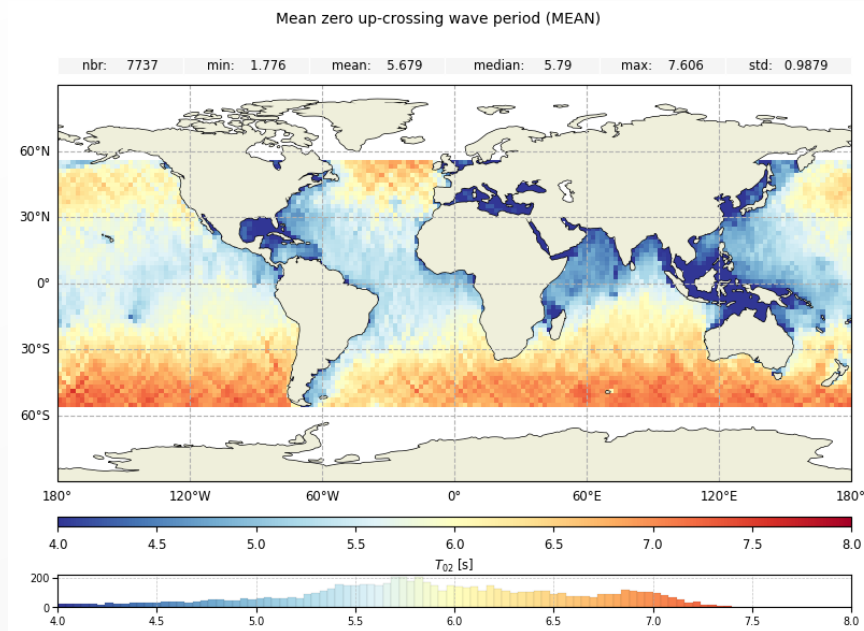
CLS/CNES

ERA5

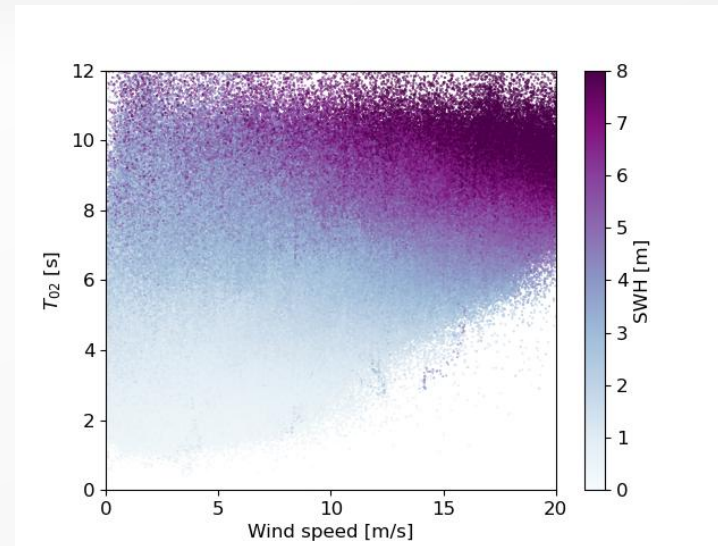
Retrieving new variables: characterizing ocean dynamics

Wave vertical velocity standard deviation σ_v

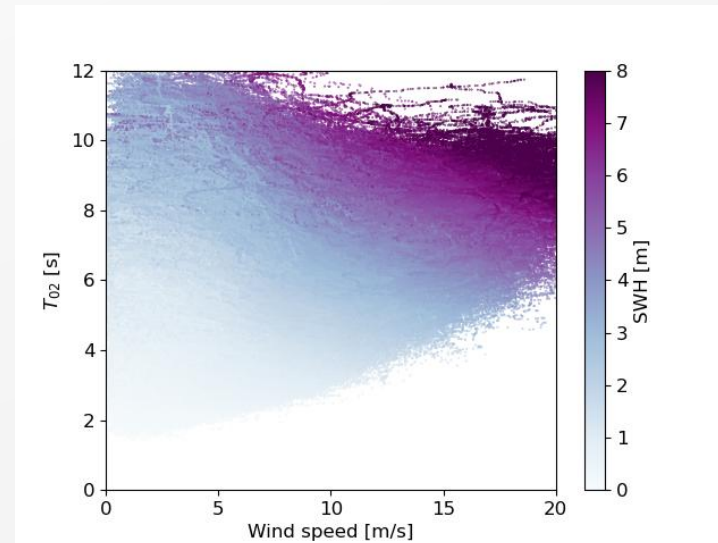
→ Retrieving the mean zero-upcrossing period $T_{02} = \frac{\pi SWH}{2 \sigma_v}$



T_{02} is an integrated parameter that gives more weight to the higher frequencies of the wave spectrum, i.e. wind waves. It is used to estimate the average period of the zero-crossing waves in a sea state.



← CLS/CNES

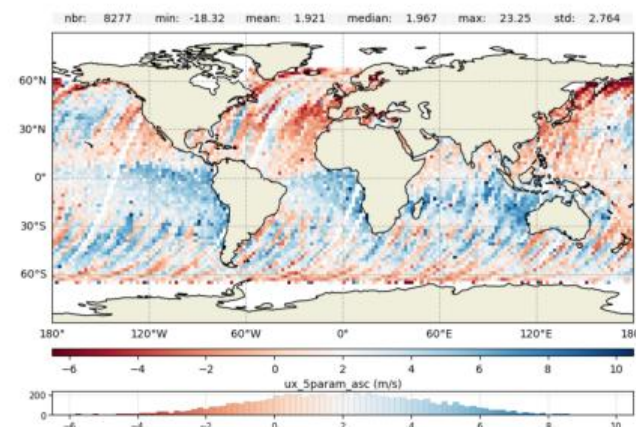


← ERA5

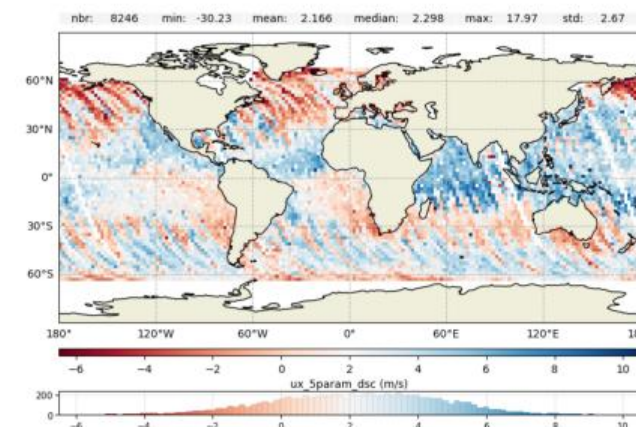
Retrieving new variables: characterizing ocean dynamics

Effective along-track surface velocity u_x

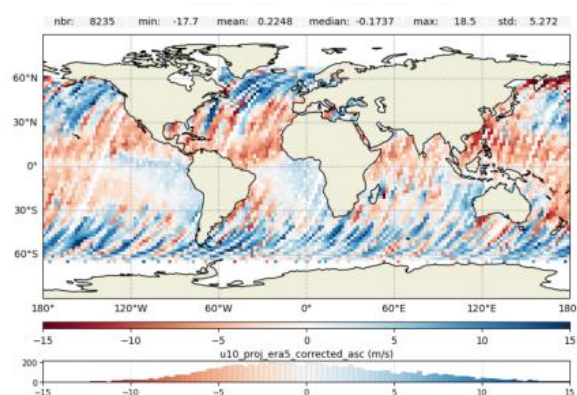
Ascending



Descending

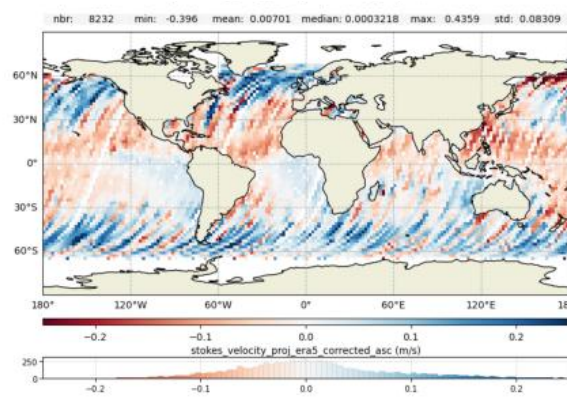


Ascending



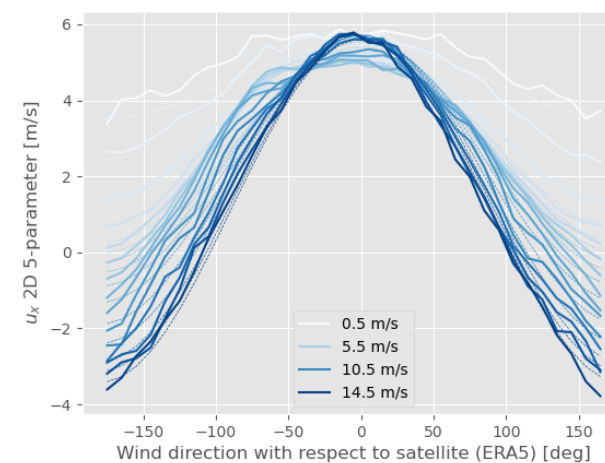
Projected wind speed

Ascending



Projected Stokes drift

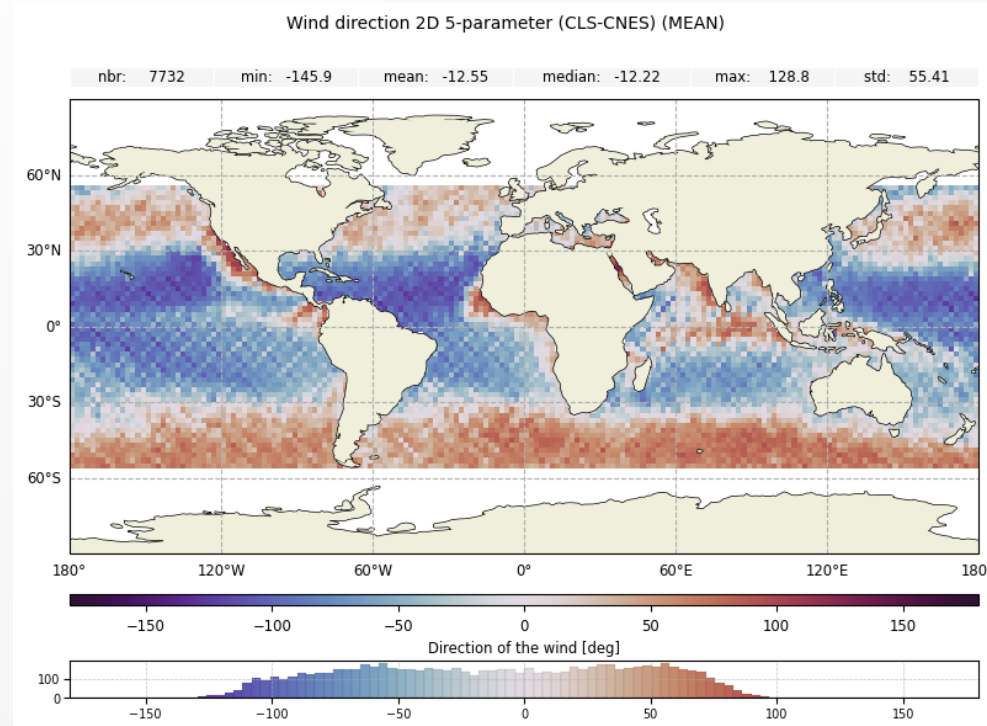
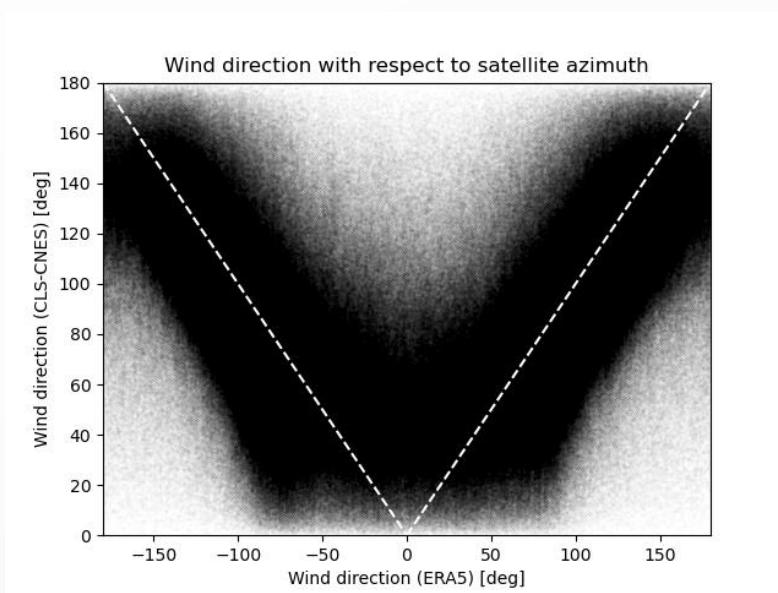
January-June 2026



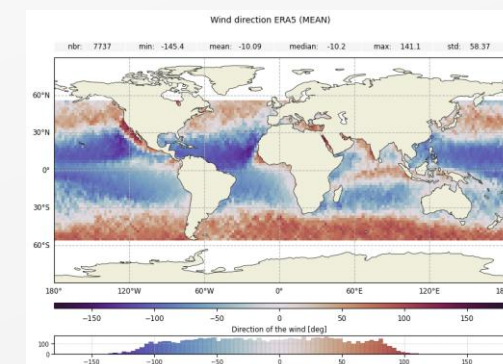
Retrieving new variables: characterizing ocean dynamics

Effective along-track surface velocity u_x
→ Perspective: Retrieving the wind direction

(Further validation is needed on this retrieval)



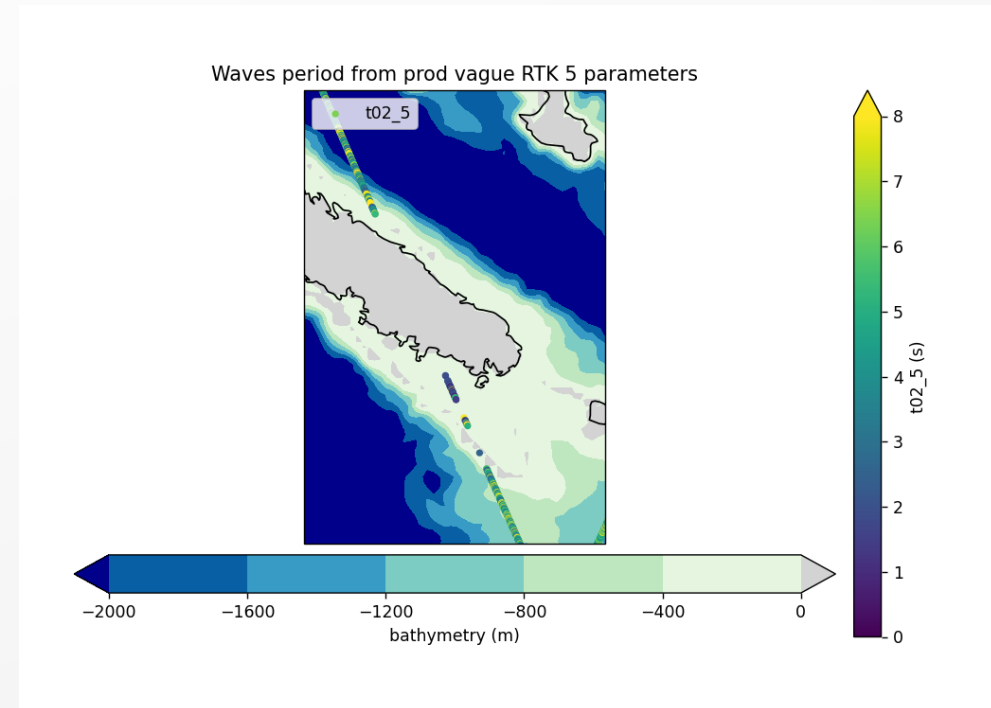
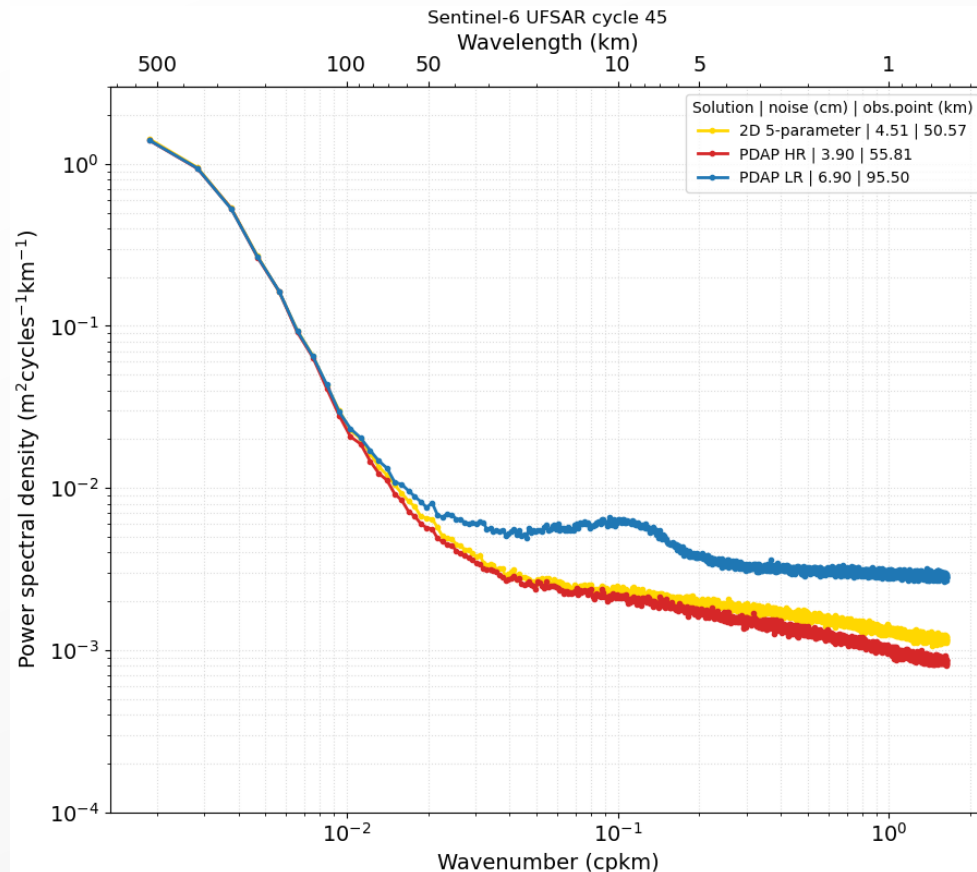
ERA5



Using ERA5 to calibrate the wind dependency and to remove the left-right ambiguity

Keeping the Delay-Doppler improved along-track resolution

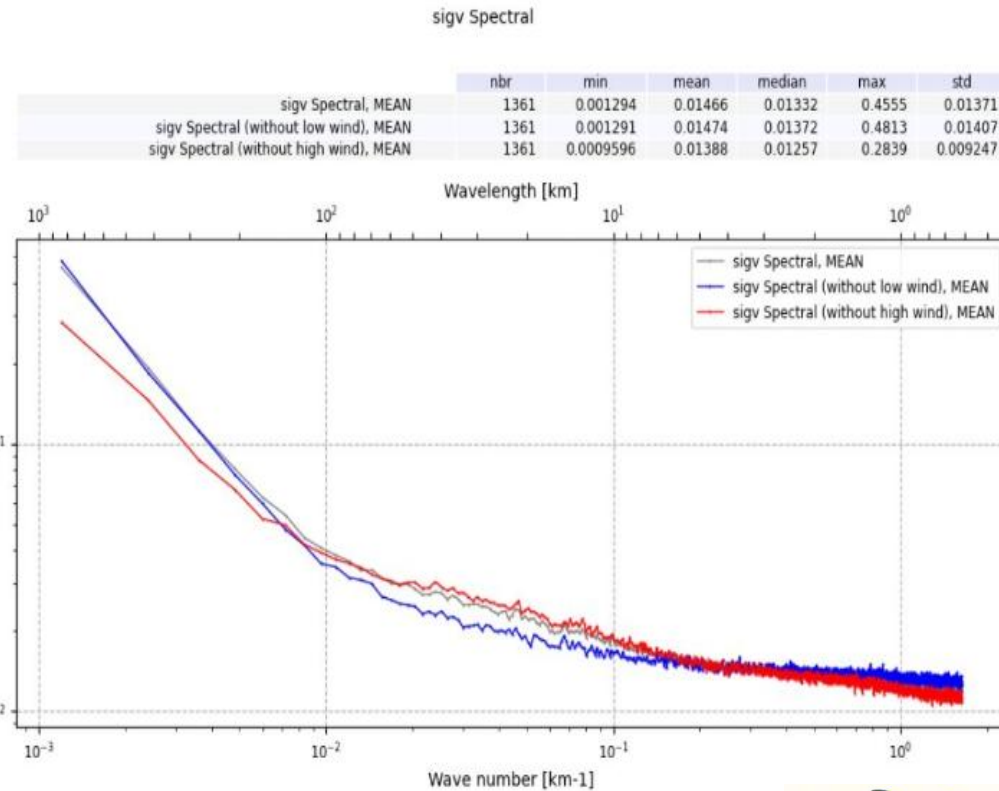
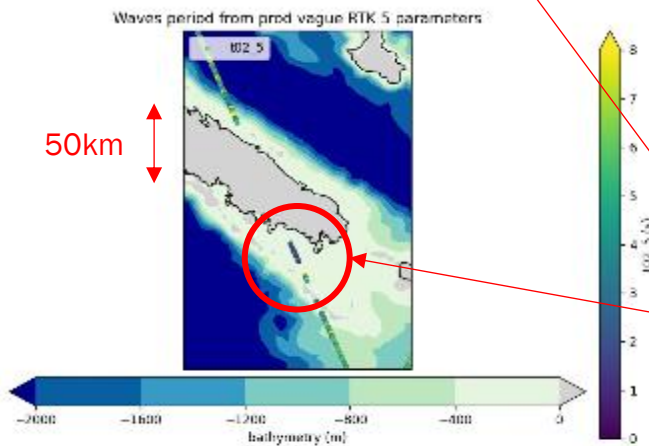
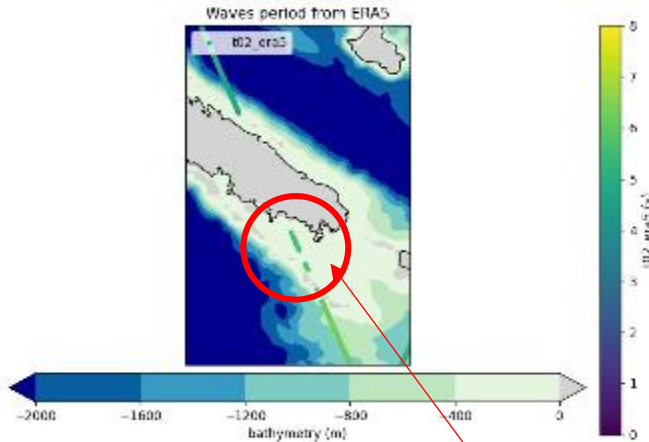
The high along-track resolution can be used to study coastal areas, extreme events or wave-topography disentanglement



Retracked wave period when entering the lagoon of New Caledonia

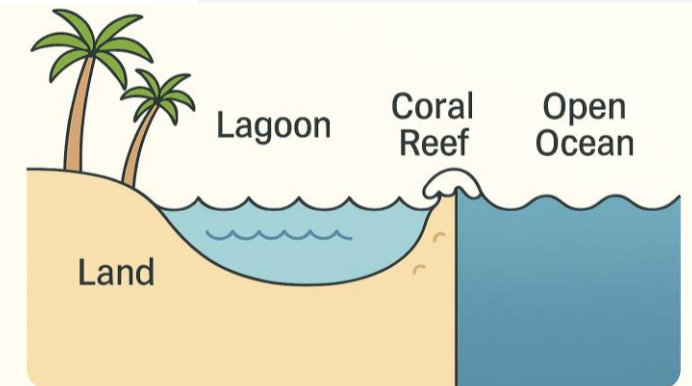
Example of applications: reduction of swell inside a lagoon

New Caledonia



The **removal of low winds** area reduces the spectral slope, illustrating the impact of **wind/waves interactions or uncertainty** to be studied with such products

The reduced period inside the lagoon is observed with the data whereas the model misses this variation



Thank you for your listening!

→ Contact: Irodet@groupcls.com



Be ready for the incoming product on Aviso by mid-July!

DOI: 10.24400/527896/AVISO-2026.008



New wind and wave variables to assimilate!



Higher resolution without the associated biases!

→ Prospects for the present and future SAR altimetry missions (CRISTAL, S3NG-T, S6NG)

This work was supported by CNES in the frame of the CNES/ESTEC agreement



Supplementary material

Leveraging Delay-Doppler altimetry

We made use of Christopher Buchhaupt's model (Egido and Smith 2017, Bucchaupt 2020–2023):

$$\text{Model} = \frac{P_u}{2F_s} \text{IFFT} \left(\frac{1}{N_{looks}} \sum_{\eta} \text{PDF}_r \times \text{PDF}_{az} \times \text{PTR}_r \times \text{PTR}_{az} \times \text{FSSR} \times e^{-\frac{2i\pi\eta f_d}{1 + \frac{u_x}{v_{sat}}}} \right) + \frac{t_n}{N_{looks}}$$

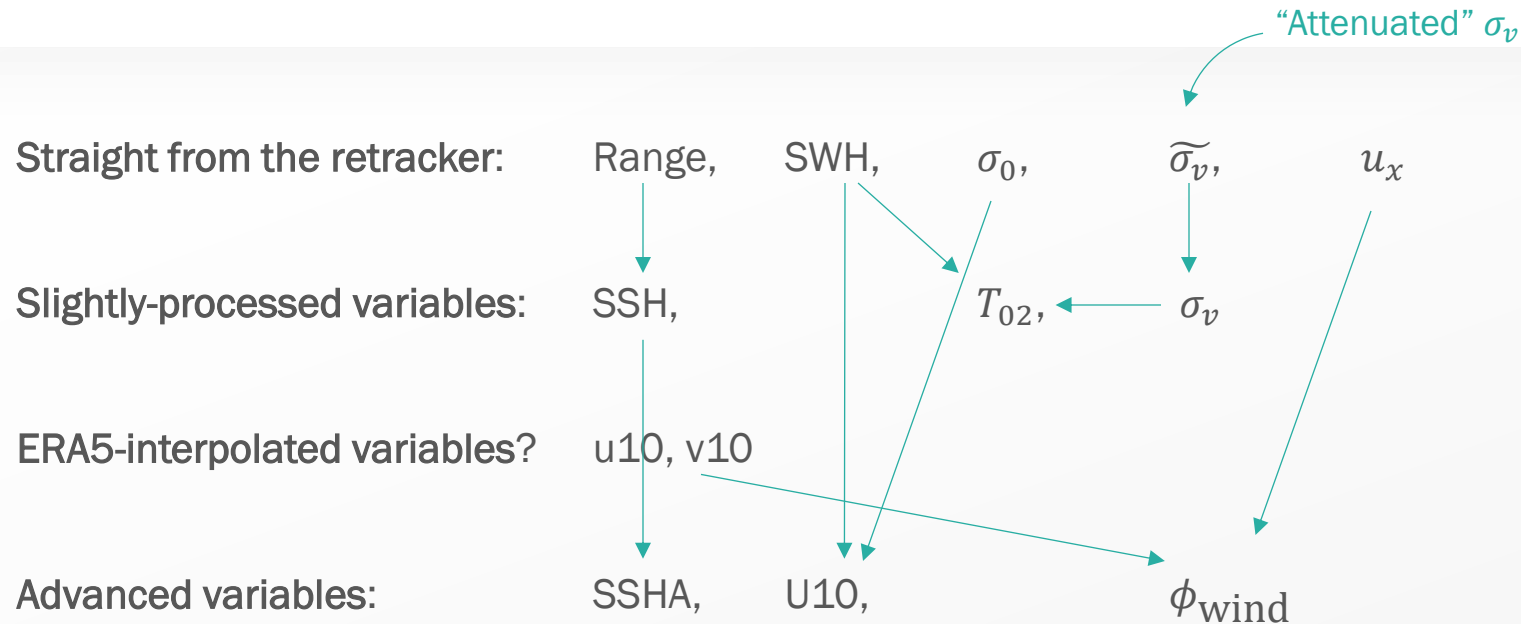
Adding a new term in the physical model to account for vertical surface motion:

$$\text{PDF}_{az} = e^{-\frac{4\pi^2 a_v \sigma_v^2 \eta^2}{\lambda_c^2}}$$

Modifying the iDFT to account for horizontal surface motion

→ Direct theoretical dependency in σ_v^2 and u_x , without model input!

Product content



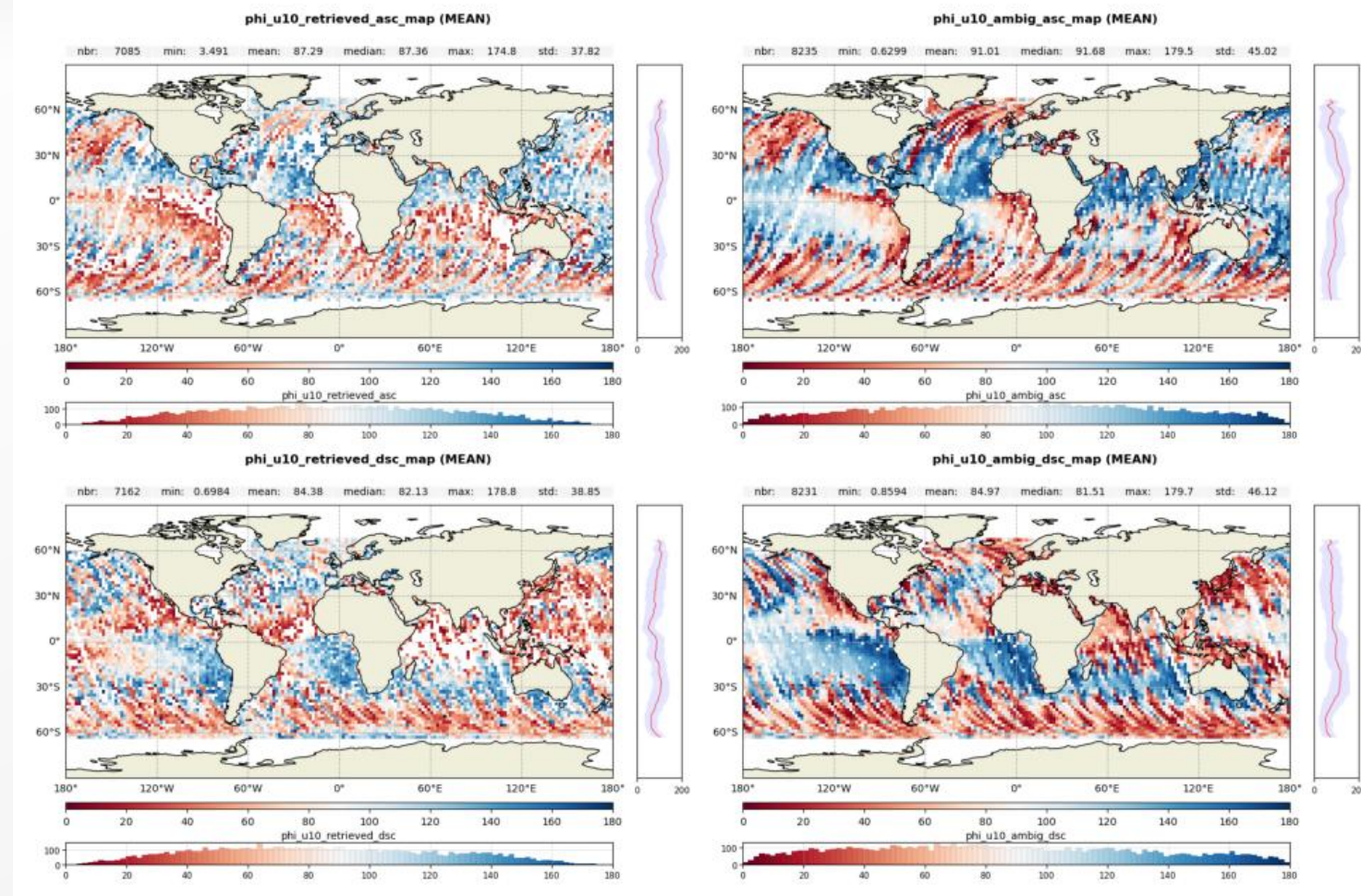
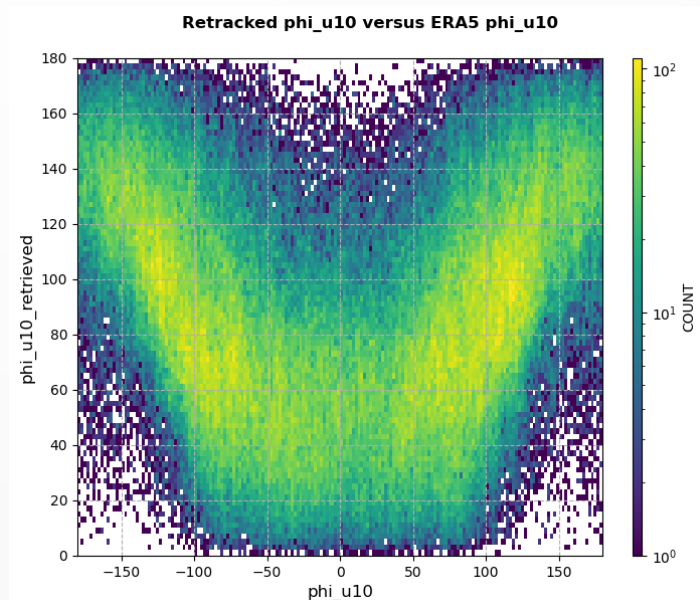
Deriving SSHA from SSH: Using geophysical corrections

Deriving U10 from σ_0 : Using Collard et al., neural network prediction calibrated with model and altimetry data

Deriving ϕ_{wind} from u_x : Using $u_x = A(U_{10}) \cos(\phi_{\text{wind}} - \phi_{\text{sat}}) + B(U_{10})$, with $A(U_{10})$ and $B(U_{10})$ calibrated with model and altimetry data. U_{10} can be the altimeter wind speed or the model wind speed. Finally, a model must be used to remove the left-right ambiguity associated with the cosinus.

Retrieving new variables: characterizing ocean dynamics

Effective along-track surface velocity u_x
→ Retrieving the wind direction

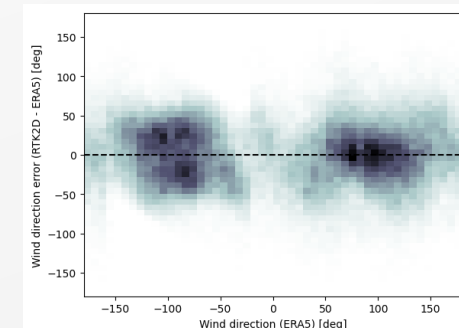
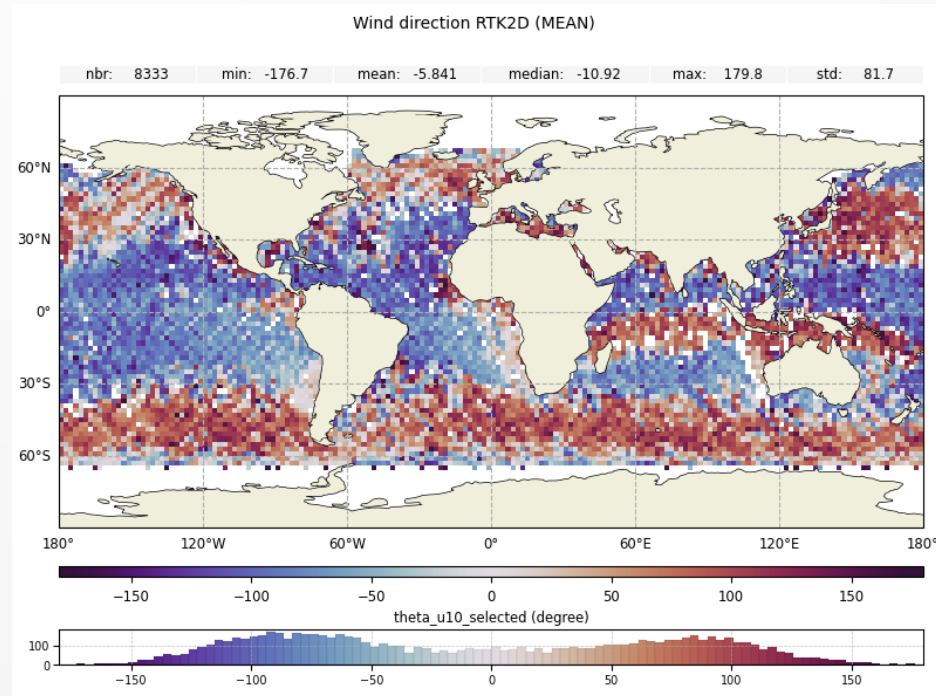
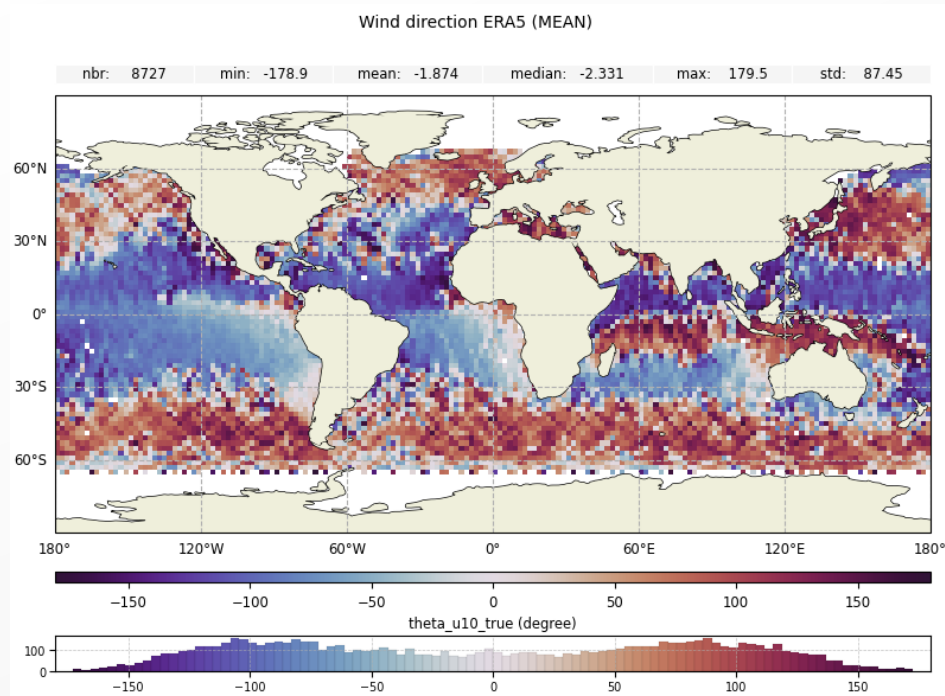


Perspective: Using models or cross-overs to remove the left-right ambiguity

Retrieving new variables: characterizing ocean dynamics

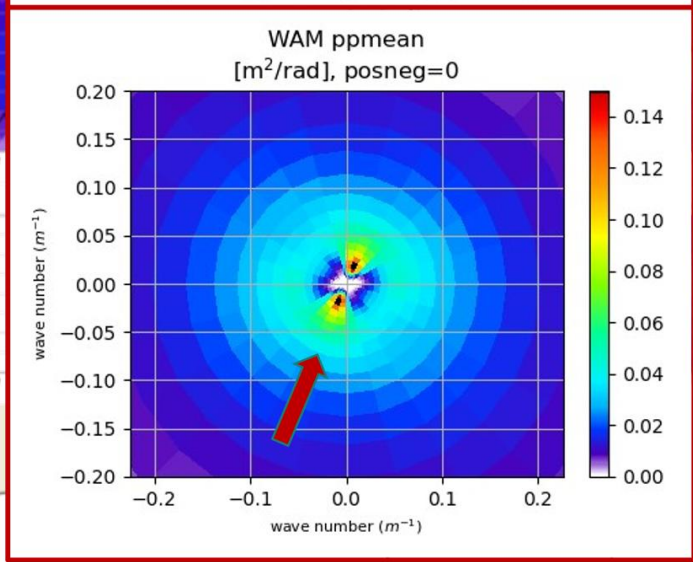
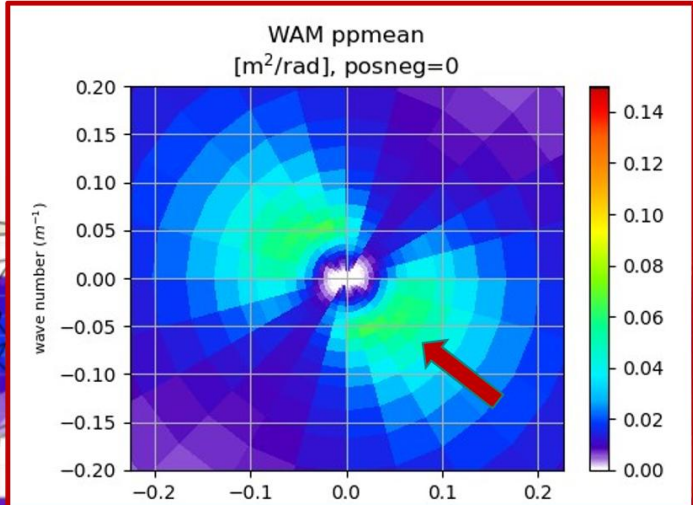
Effective along-track surface velocity u_x

→ Retrieving the wind direction, removing the left-right ambiguity using the ERA5 model

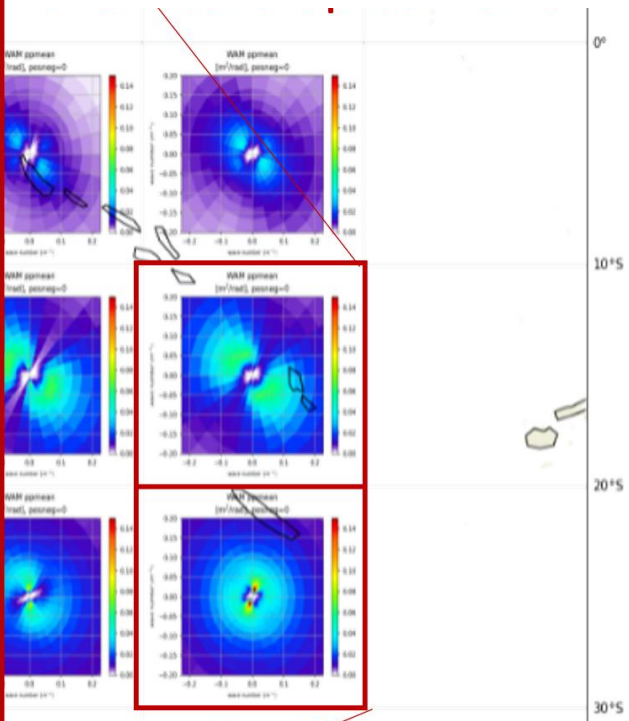


CFOSAT spectral data

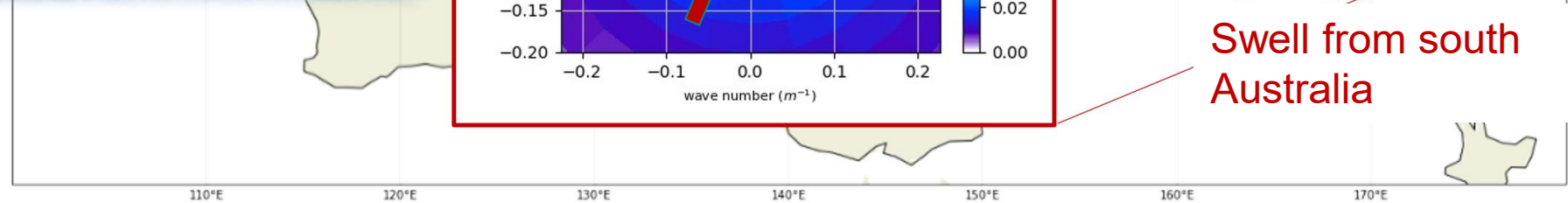
Use Case in New Caledonia



Trade winds driven waves in the intertropical zone

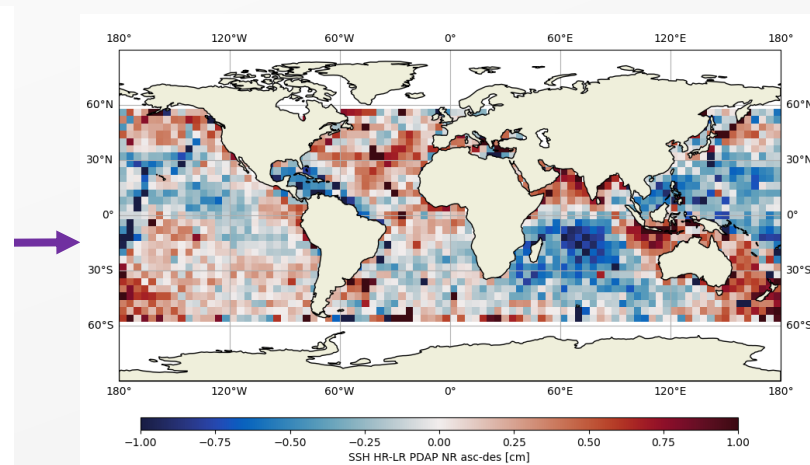
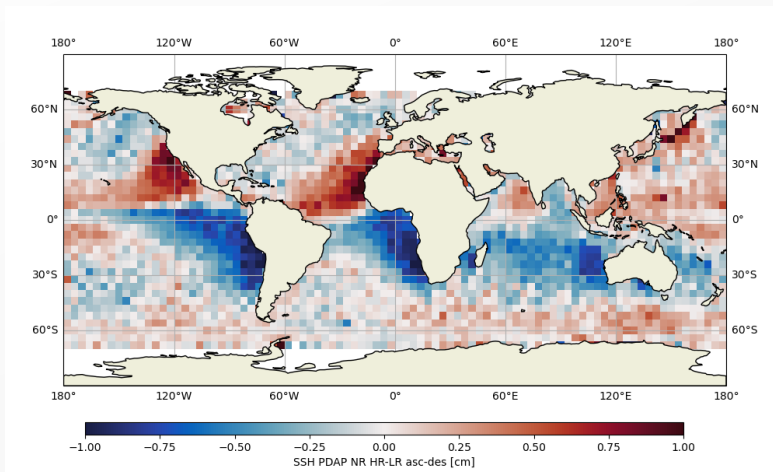
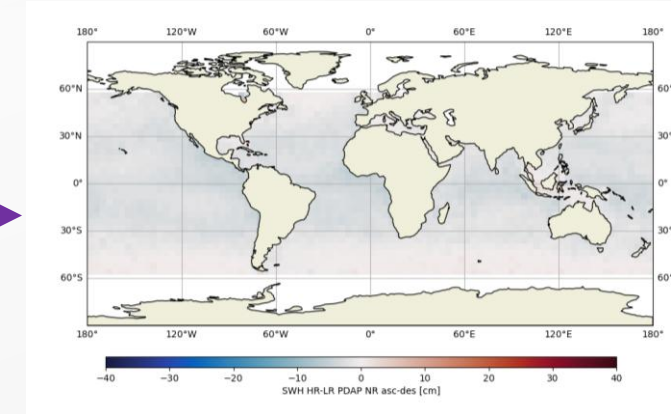
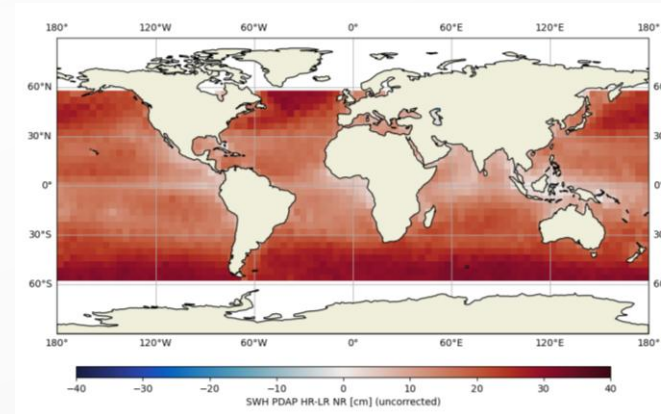
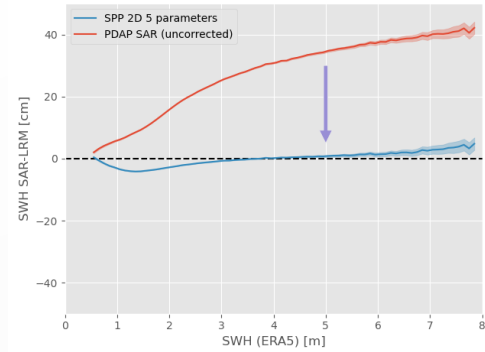


Swell from south Australia

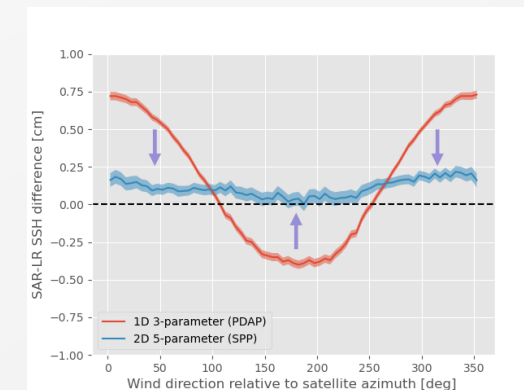


Resolving the biases: alignment with LRM without any Look Up table

Removing the overestimation of the waves heights

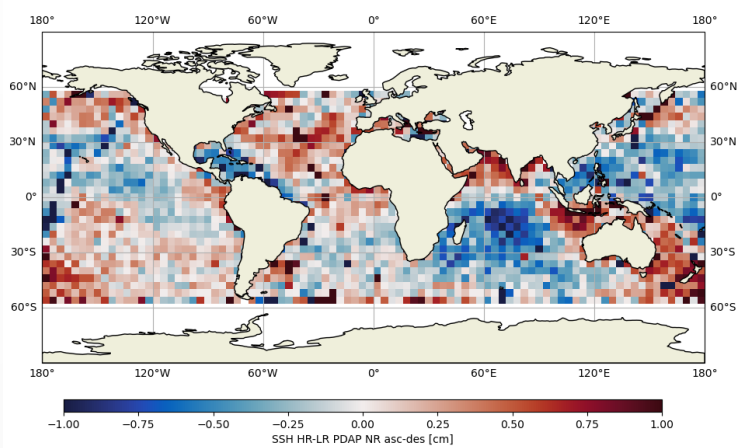


Removing the wind-dependent SSH bias

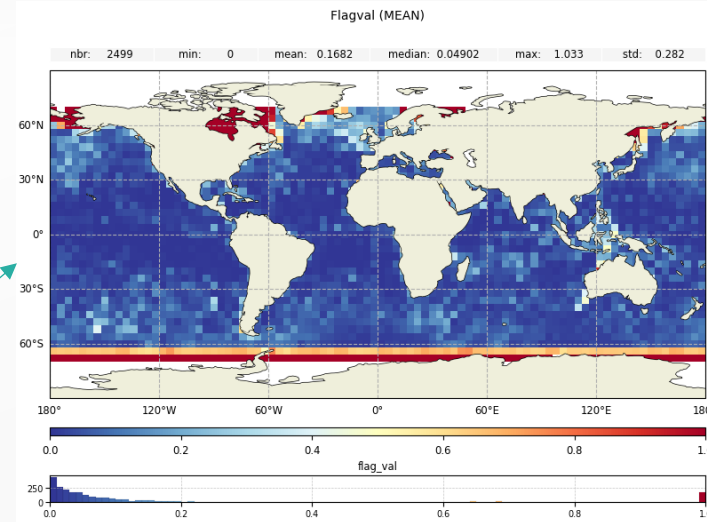


Editing questions

Cycle 45



Flagval
(SSHA)



Custom editing:
 $|\text{Lat}| < 55^\circ$
 $0 \text{ m} < \text{SWH} < 20 \text{ m}$
 $-130 \text{ m} < \text{SSH} < 100 \text{ m}$
 $0 < \sigma_v < 2 \text{ m/s}$
 $|u_x| < 60 \text{ m/s}$

