



OSTST 2023 Puerto Rico

## ***Introduction of 2/rev harmonics in the empirical forces model for Sentinel altimetry satellites***

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POD Session, 8 November 2023

# Perturbation Forces for Precise Orbit Determination

Gravitational Forces: earth gravity field, gravity perturbations (moon, sun, planets), ocean & solid earth tides

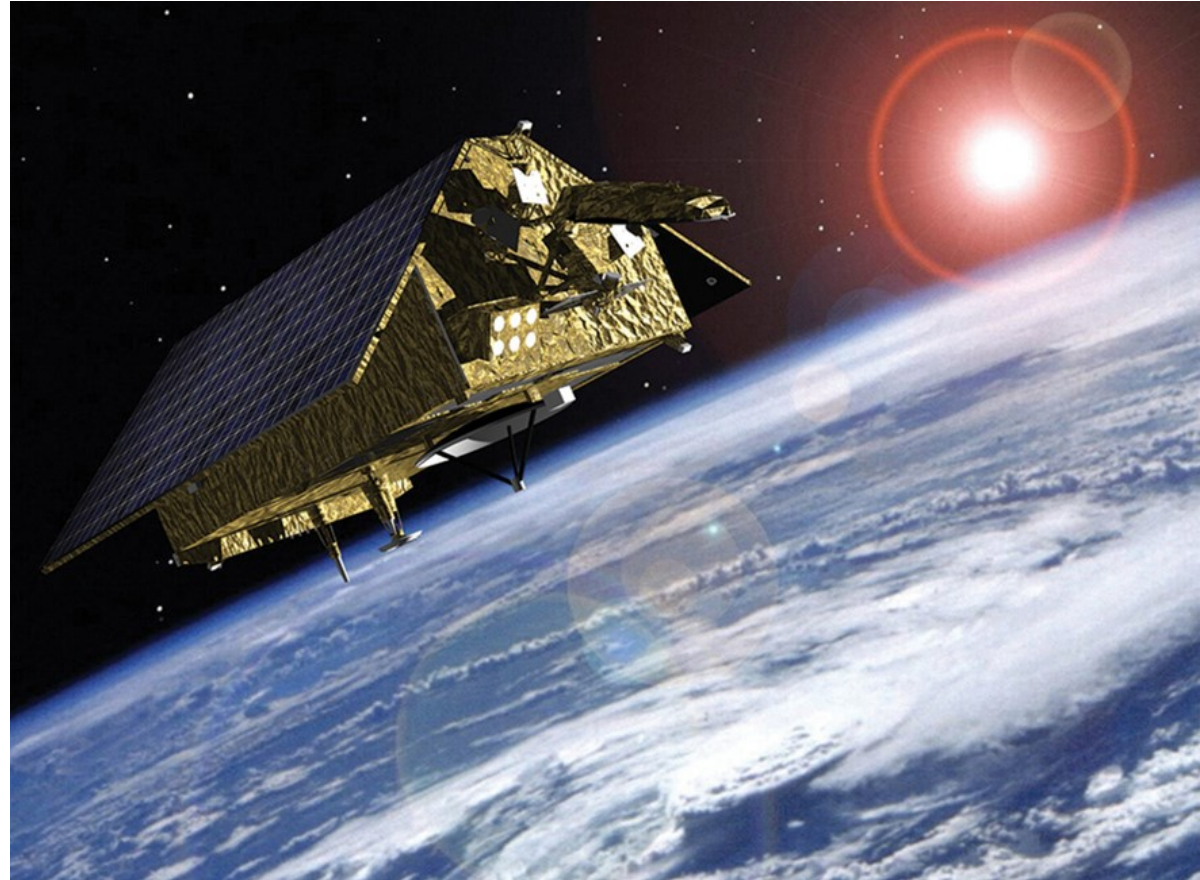
Forces on satellite: atmospheric drag, radiation pressure (direct solar radiation, albedo, earth IR radiation)

Sentinel-6 MF:

Pre-launch initial model

ESA's documentation model

**Previous studies from CNES team showed a 2/rev contribution to the empirical forces for Sentinel-6 MF**

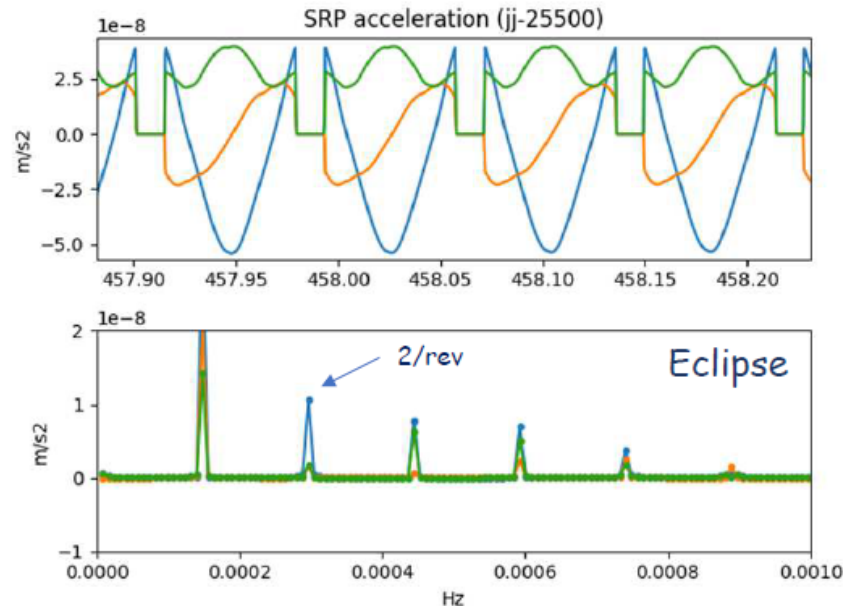
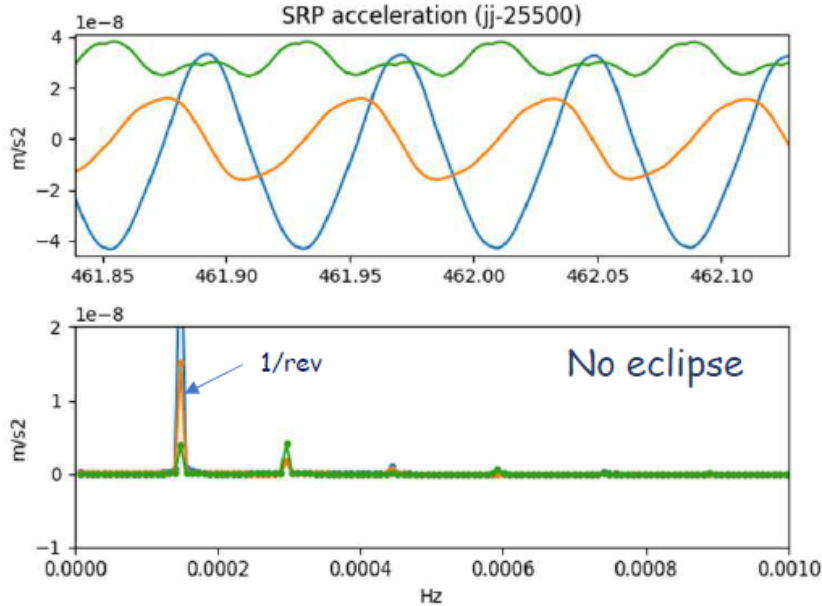


# Spectral analysis, radial displacement harmonics



## Sentinel-6 radiation pressure model analysis

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R, T, N accelerations

These two arcs are around the  $\beta$  value where eclipses begin (~55 degrees)

The SRP harmonics amplitudes are due to the eclipse transition

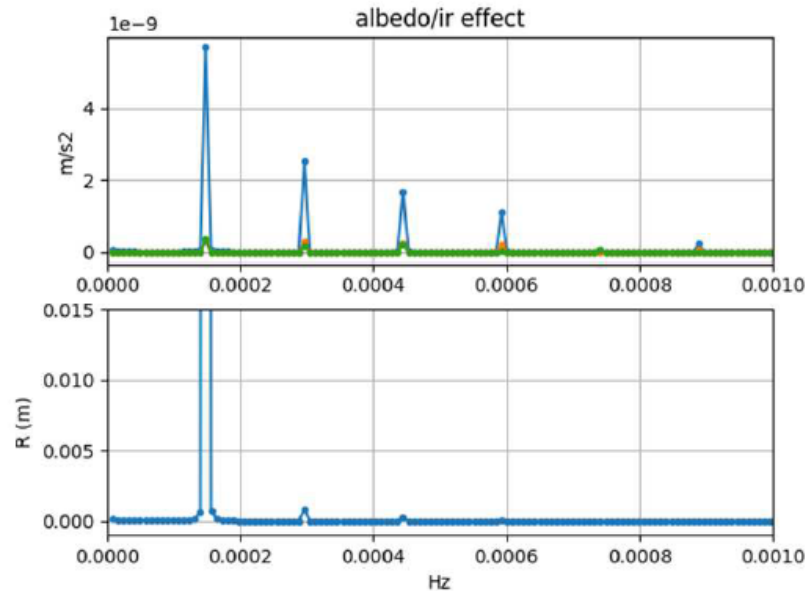
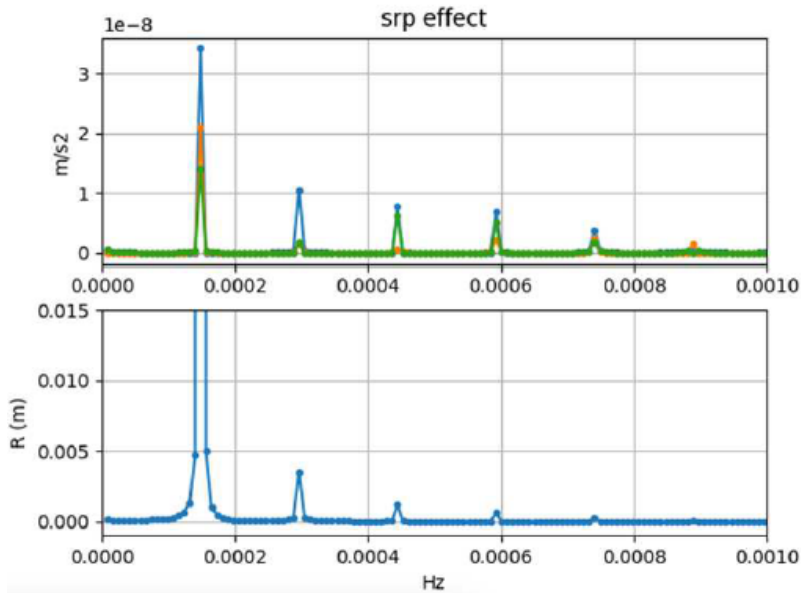
Source : Slides taken from Mercier F., et al (2022)

# Spectral analysis, radial displacement harmonics



## Sentinel-6 radiation pressure model analysis

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R, T, N accelerations, radial response, begin of eclipse period

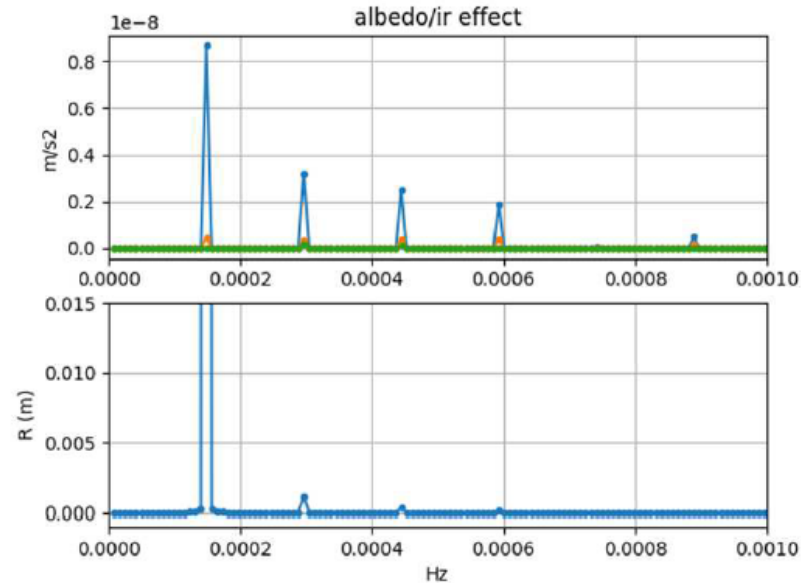
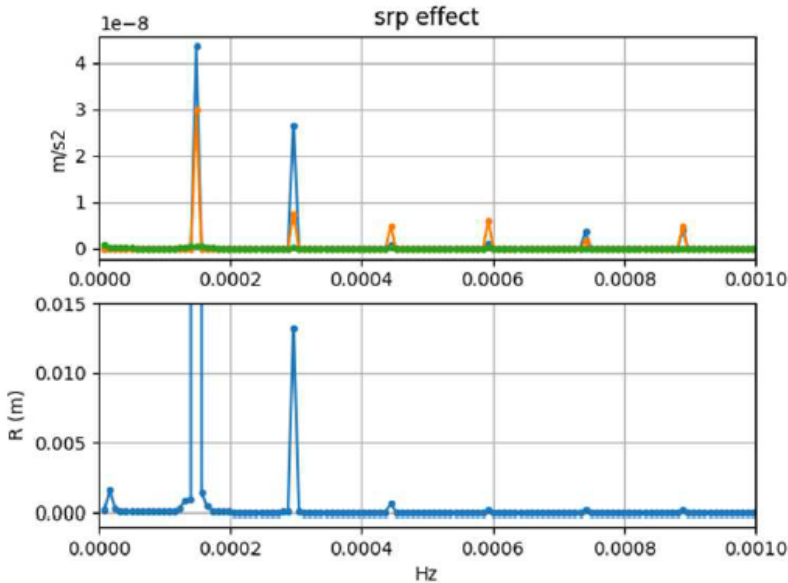
2/rev, main harmonic : here, the SRP contribution is below 5 mm amplitude  
the albedo/ir response is negligible

Source : Slides taken from Mercier F., et al (2022)

# Spectral analysis, radial displacement harmonics

## Sentinel-6 radiation pressure model analysis

OSTST 2022, Venice, POD Session



R, T, N accelerations, radial response,  $\beta$  value close to 0 (sun close to the orbital plane)

2/rev, main harmonic : here, the SRP contribution is higher (1.4 cm)  
the albedo/ir response is negligible

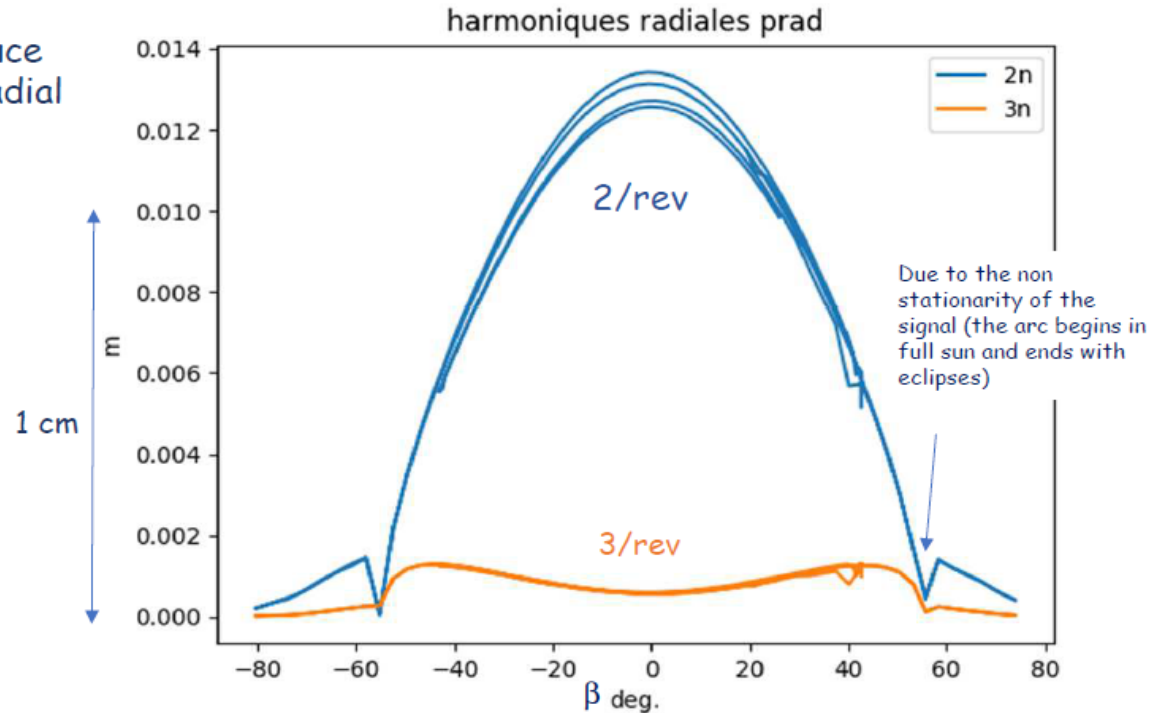
higher harmonics : negligible

Source : Slides taken from Mercier F., et al (2022)

# SRP harmonics amplitudes and beta angle

Radial 2/rev and 3/rev due to SRP acceleration :

10% error in the amplitude produce less than 1.5 mm at 2/rev in radial (~1.5 cm for the complete model see preceding slide)



Source : Slides taken from Mercier F., et al (2022)



Sentinel-6 radiation pressure model analysis

OSTST 2022, Venice, POD Session

## Conclusions from previous studies

CNES POD Team showed a contribution to the radial acceleration spectrum producing 2/rev harmonics during eclipse transitions (mainly due to SRP), dependency on  $\beta$  angle

Proposal of introduction of 2/rev term

$$F = \underbrace{A \cos \omega t + B \sin \omega t + C}_{1/\text{rev}} + \underbrace{D \cos 2\omega t + E \sin 2\omega t}_{2/\text{rev}}$$

- Introduction of 2/rev term in the empirical model



Source : [www.space.com](http://www.space.com)

# Proposed empirical model

$$F = \underbrace{A \cos \omega t + B \sin \omega t + C}_{1/\text{rev}} + \underbrace{D \cos 2\omega t + E \sin 2\omega t}_{2/\text{rev}}$$

1 point / day

	1/rev cos	1/rev sin	const.
R	0	0	0
T	1	1	0
N	1	1	1

1 point / 2rev

	2/rev cos	2/rev sin	const.
R	0	0	0
T	0	0	1
N	0	0	0

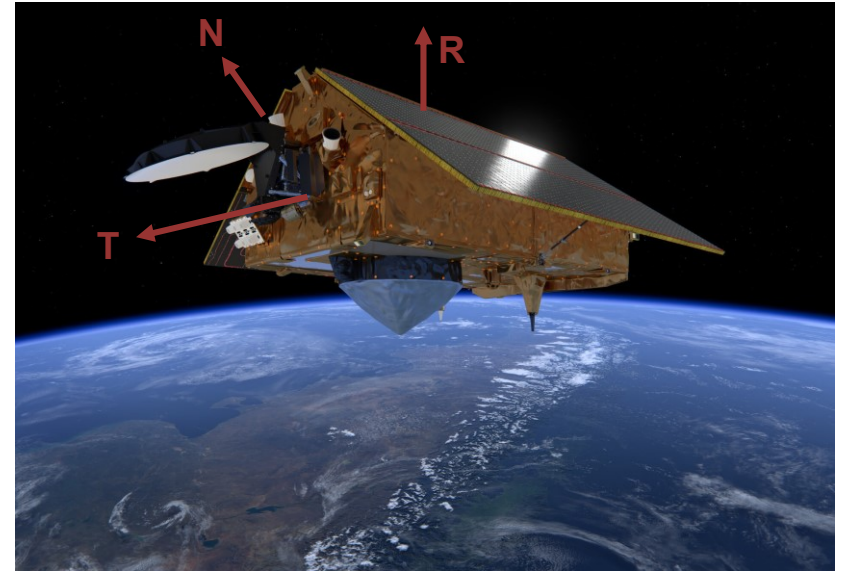


1 point / day

	1/rev cos	1/rev sin	const.
R	0	0	0
T	1	1	0
N	1	1	1

1 point / 2rev

	2/rev cos	2/rev sin	const.
R	<b>1</b>	<b>1</b>	0
T	0	0	<b>0</b>
N	0	0	0



Source : [www.esa.int](http://www.esa.int)

Experiments:

Sentinel 6A –MF : Cycles 18 -100 (21/08/18-23/02/21)

Sentinel 3A : Cycles 100-201 (05/05/21-06/08/23)

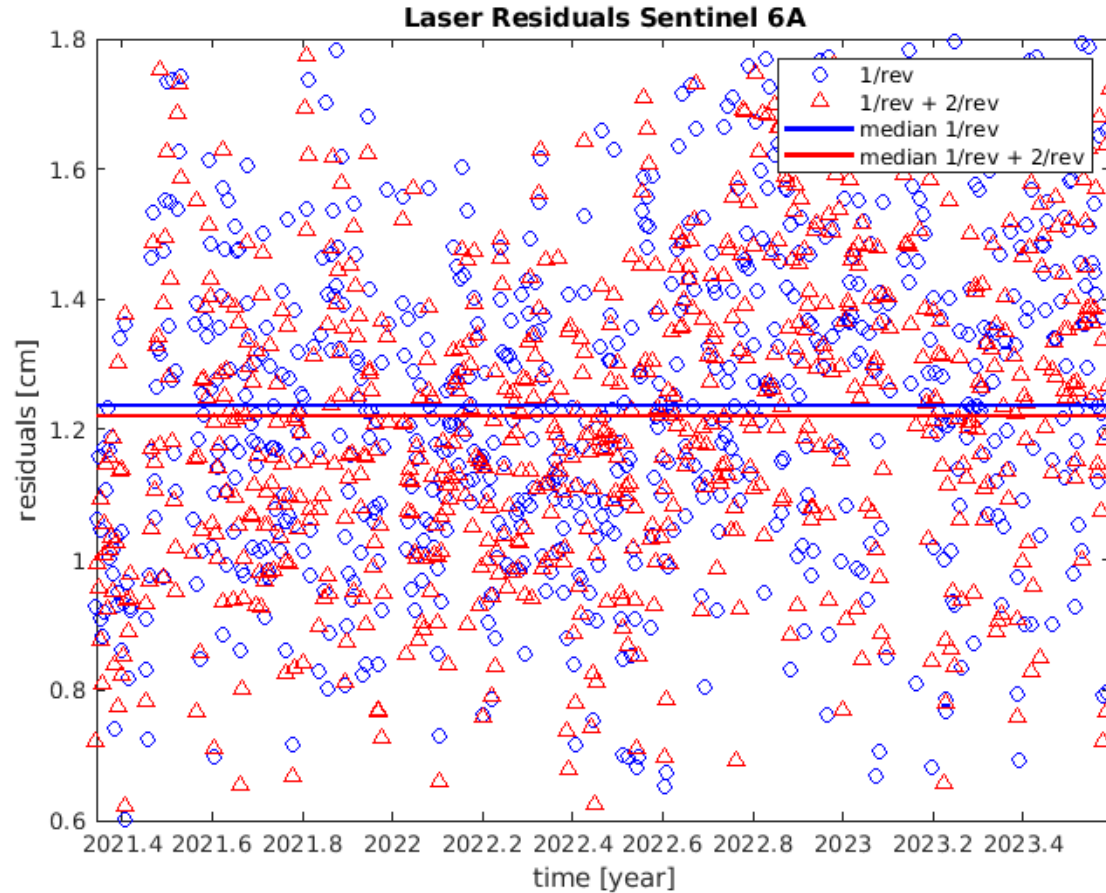
Standard: POE-F

Processing GNSS dynamic

0: no estimation, 1: estimation



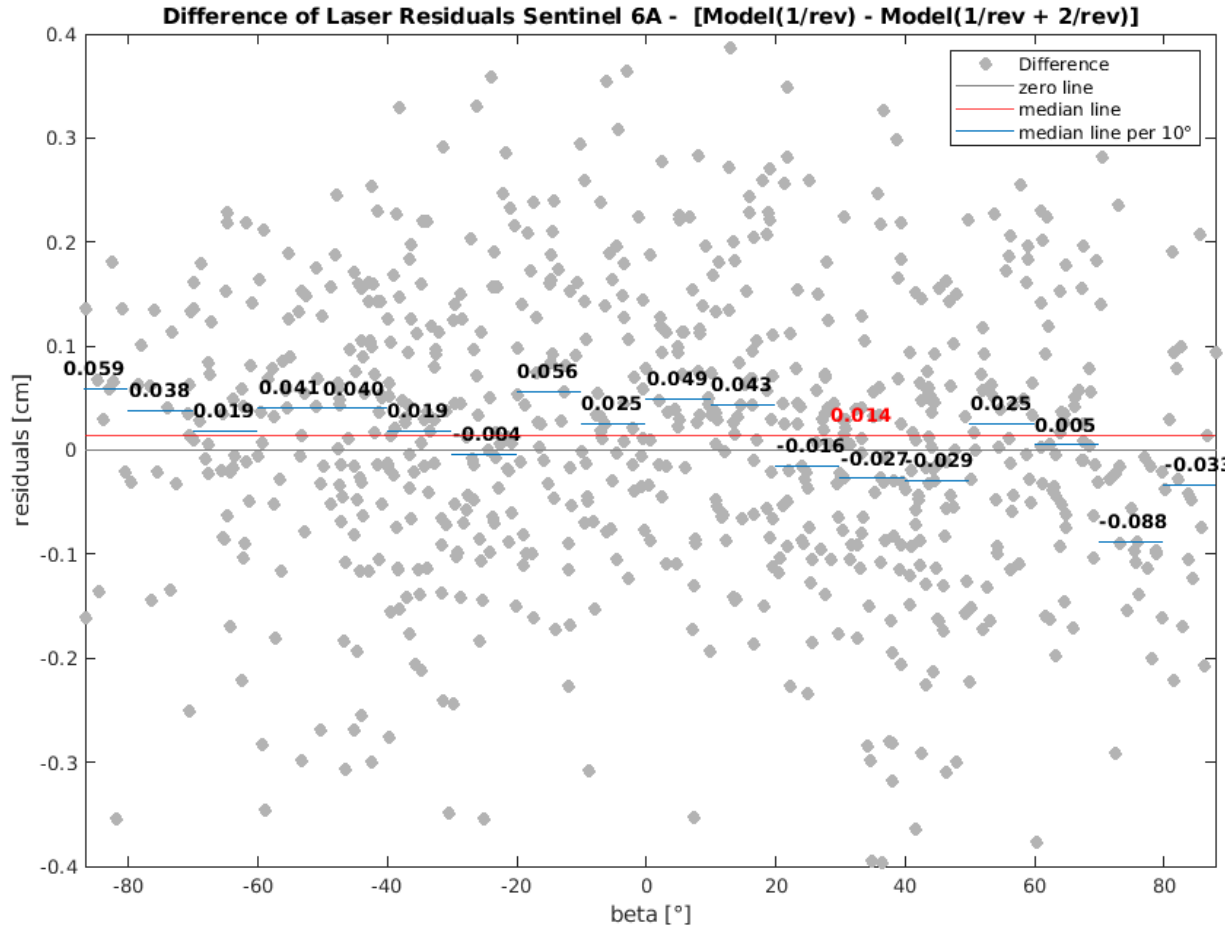
# Results – Sentinel 6-MF



1 value laser residual / day  
 median 1/rev=1,24cm  
 median 1/rev + 2/rev=1,22cm

- ✓ overall better residuals with the proposed model
- ✓ but negligible improvement

# Results – Sentinel 6-MF



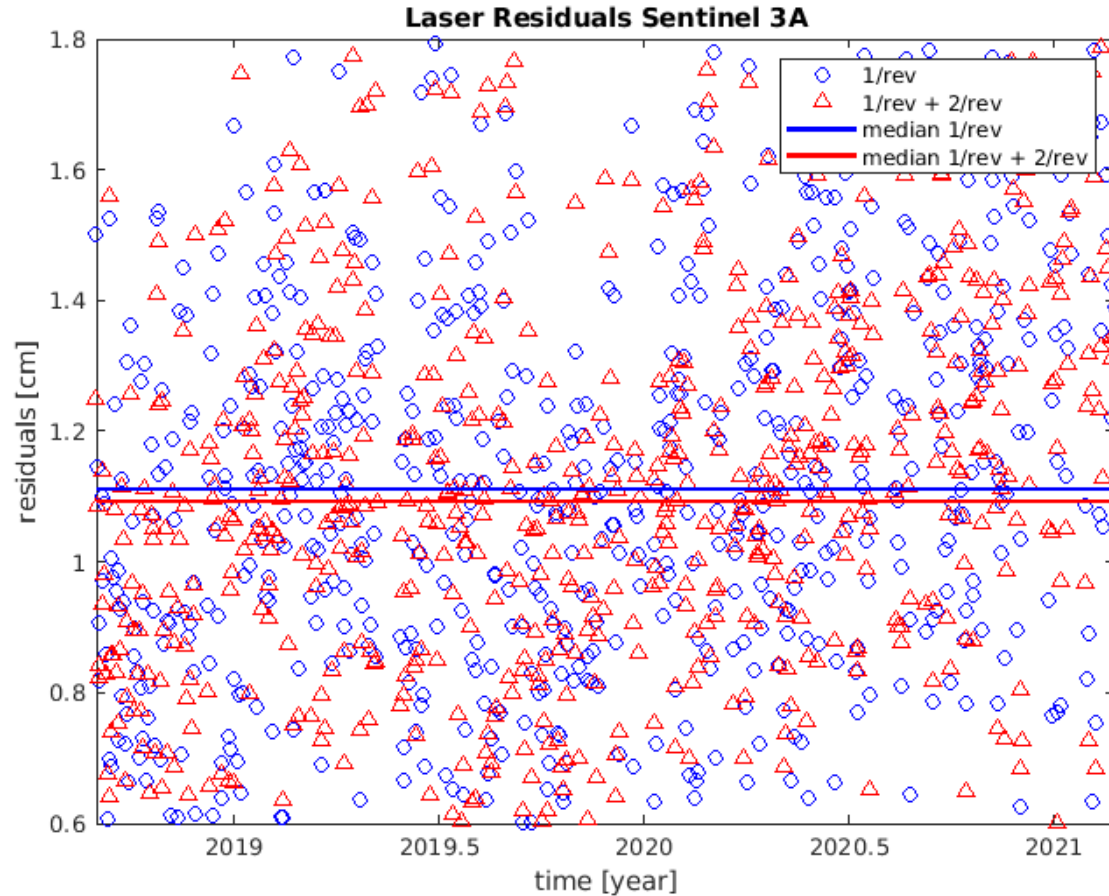
difference of residuals wrt.  $\beta$  angle

black values give the median of each  $10^\circ$   $\beta$  range

red line and value give the median of all residuals

- ✓ overall better residuals with the proposed model
- ✓ better estimation around small  $\beta$  angles  $[-10^\circ 10^\circ]$

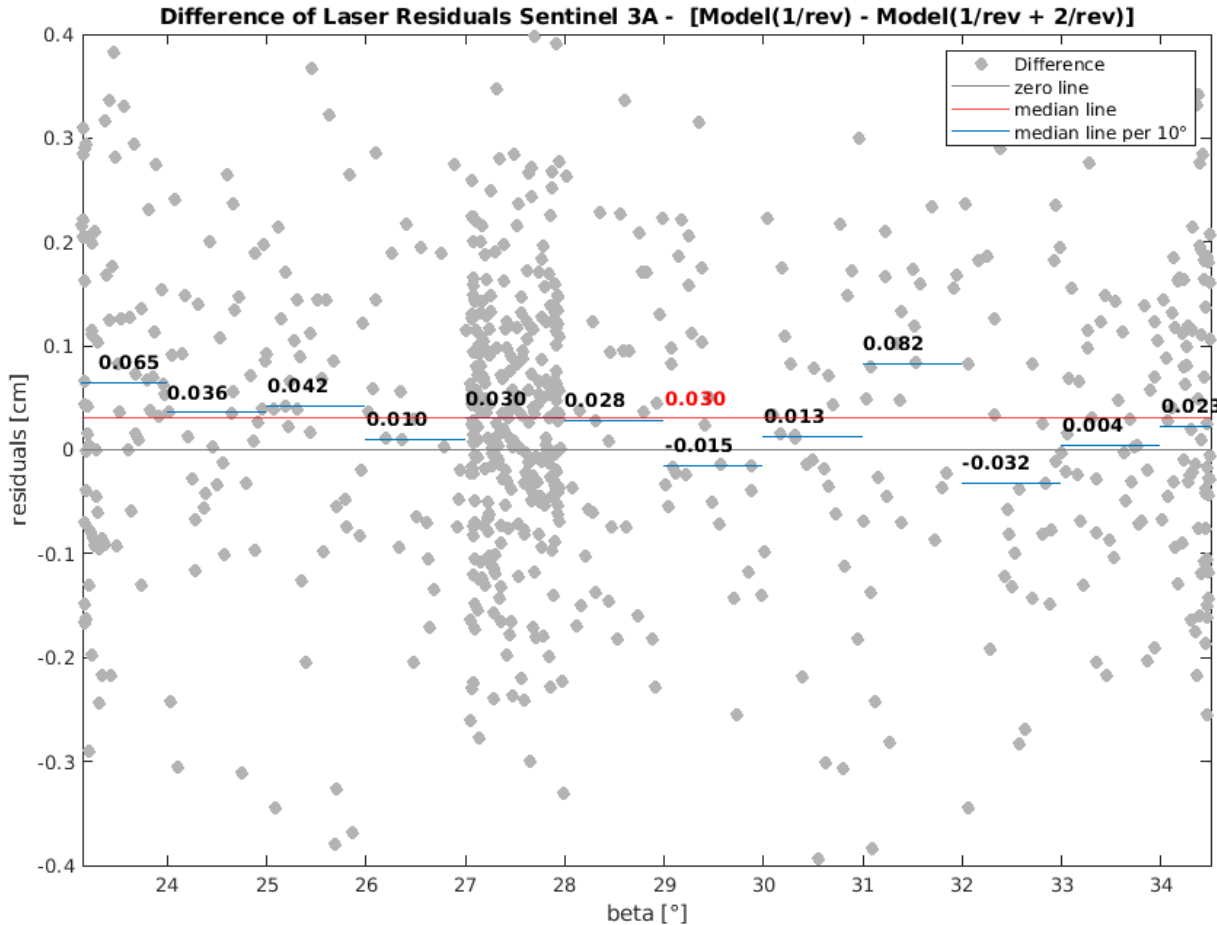
# Results – Sentinel 3A



1 value laser residual / day  
 median 1/rev=1,11cm  
 median 1/rev + 2/rev=1,09cm

- ✓ overall better residuals with the proposed model
- ✓ but negligible improvement

# Results – Sentinel 3A



difference of residuals wrt.  $\beta$  angle

black values give the median of each  $10^\circ$   $\beta$  range

red line and value give the median of all residuals

- ✓ overall better residuals with the proposed model
- ✓ better estimation around smaller  $\beta$  angles with higher eclipse periods [23° 25°]

## Conclusions – Future Work

Estimation of 2/rev empirical forces in the radial direction showed a small improvement on the SLR residuals

Bigger improvement during eclipse seasons (for Sentinel 6A-MF) and longer eclipse periods (for Sentinel 3A)



The CNES POD team will perform more tests to improve the parameters of these 2/rev terms.

More tests will also include DORIS-only dynamic and DORIS/GNSS dynamic processings



# THANK YOU !

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## Sources

- Carrou JP. (1986), Zoom software: error analysis and accurate orbit restitution at CNES. In: Bhatnagar KB (ed) Space dynamics and celestial mechanics. Springer, Dordrecht, pp 381–398
- Morrow R. (2008), Satellite Altimetry [https://www.aviso.altimetry.fr/fileadmin/documents/kiosque/education/Rose\\_cours1\\_2008.pdf](https://www.aviso.altimetry.fr/fileadmin/documents/kiosque/education/Rose_cours1_2008.pdf)
- Mercier F., Couhert A., Moyard J., Cullen R. (2022), Sentinel-6 radiation pressure model analysis, OSTST 2022 presentation, Venice, [https://ostst.aviso.altimetry.fr/fileadmin/user\\_upload/OSTST2022/Presentations/POD2022-Sentinel\\_6\\_radiation\\_pressure\\_model\\_analysis.pdf](https://ostst.aviso.altimetry.fr/fileadmin/user_upload/OSTST2022/Presentations/POD2022-Sentinel_6_radiation_pressure_model_analysis.pdf)

## Images

- [1] [cpaess.ucar.edu/meetings/ostst-2023](https://cpaess.ucar.edu/meetings/ostst-2023)
- [2] [www.esa.int/Space\\_in\\_Member\\_States/France/Dernier\\_coup\\_d\\_aeil\\_sur\\_le\\_satellite\\_Sentinel\\_6](https://www.esa.int/Space_in_Member_States/France/Dernier_coup_d_aeil_sur_le_satellite_Sentinel_6)
- [7] [www.space.com/sentinel-jason-earth-observation-satellite-named-nasa-scientist.html](https://www.space.com/sentinel-jason-earth-observation-satellite-named-nasa-scientist.html)
- [8] [www.esa.int/Applications/Navigation/Galileo\\_enhancing\\_Sentinel-6\\_s\\_sea\\_level\\_monitoring\\_mission](https://www.esa.int/Applications/Navigation/Galileo_enhancing_Sentinel-6_s_sea_level_monitoring_mission)