

Energetics of high frequency internal tides in global HYCOM

Miguel Solano¹, Maarten Buijsman¹, Jay Shriver², Jorge Magalhaes³, Jose DaSilva³, Christopher Jackson⁴, Roy Barkan⁵, Brian Arbic⁶

¹**The University of Southern Mississippi, United States**

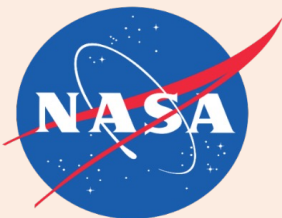
²Naval Research Laboratory, United States

³University of Porto, Portugal

⁴National Oceanographic and Atmospheric Administration, United States

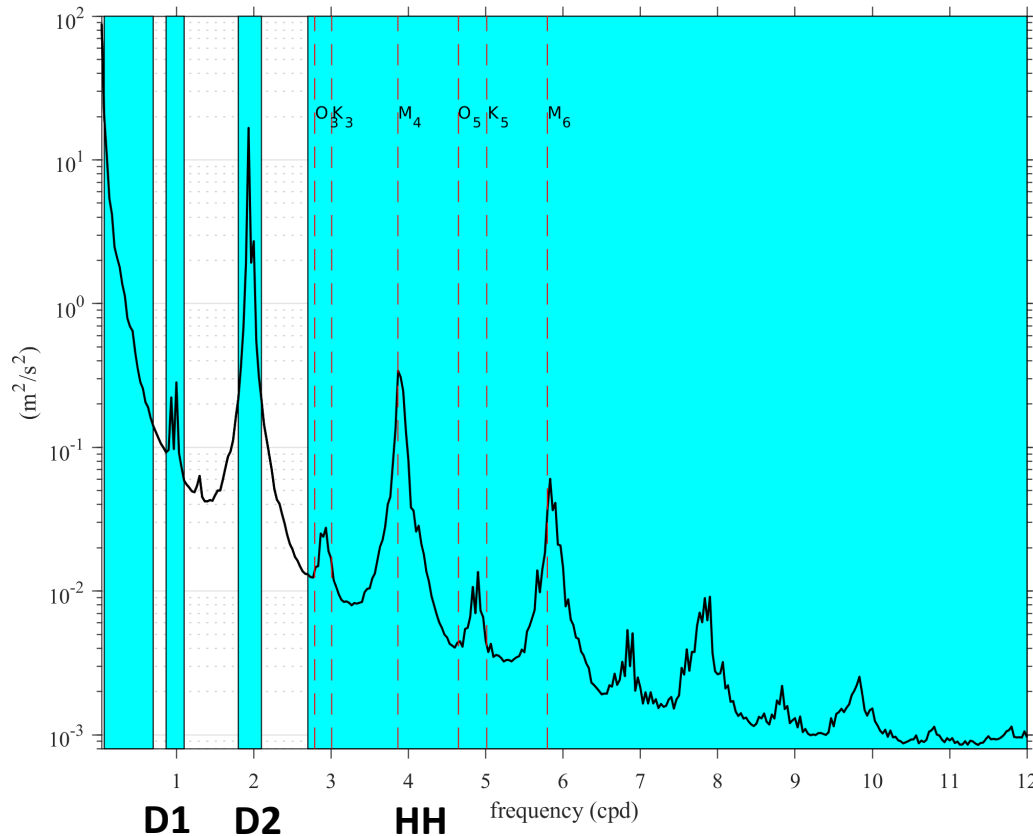
⁵University of California Los Angeles, United States

⁶University of Michigan, United States



Model and Methods

Energy spectra at Amazon Shelf



Hybrid Coordinate Ocean Model (HYCOM)

- 1/25° (4 km) horizontal resolution, 41 vertical levels
- 3 hourly winds
- Tide forcing (M_2 , S_2 , N_2 , K_1 , O_1)
- No data assimilation

Analysis

- Analyze hourly 3D fields for **30 days of May/June 2019**
- Band-pass for semidiurnal (**D2**) and diurnal (**D1**) bands
- Capture the supertidal band (**HH**) via a high-pass
- Conduct **baroclinic energy analysis** in deep ocean (<250m)
- **Coarse graining** to estimate nonlinear energy transfer to HH

Research questions

Why are internal tides observed to steepen in global HYCOM (1/25°)?

Can HYCOM simulate these solitary NLIW?

*How much energy is transferred from tidal to supertidal frequencies in global ocean models?

Internal tides: sources and sinks

Time-mean and depth-integrated energy balance

Tidal (D1+D2) $C = \nabla \cdot F + R$

Supertidal (HH) $C = \nabla \cdot F + R$

Barotropic to baroclinic
energy conversion $C = \overline{\rho' g W}$

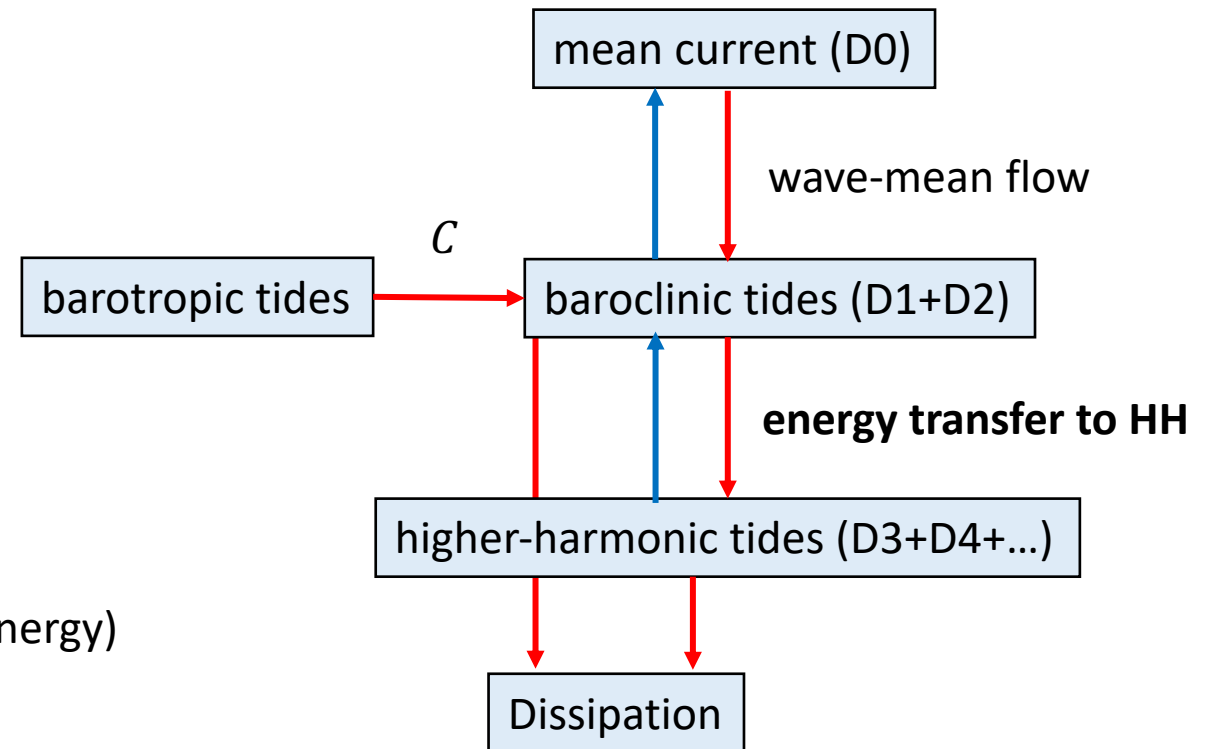
Baroclinic energy flux $F = \overline{\mathbf{u}' p'} + \overline{\mathbf{u} E}$

Residual

1. **Energy transfer to HH** (coarse-grained Kinetic Energy)

$$\Pi_{\tau} - \frac{1}{T} \int_0^h \rho_0 (\overline{u_i u_j} - \bar{u}_i \bar{u}_j) \frac{\partial \bar{u}_j}{\partial x_j} dz dt \quad \tau = 9hr$$

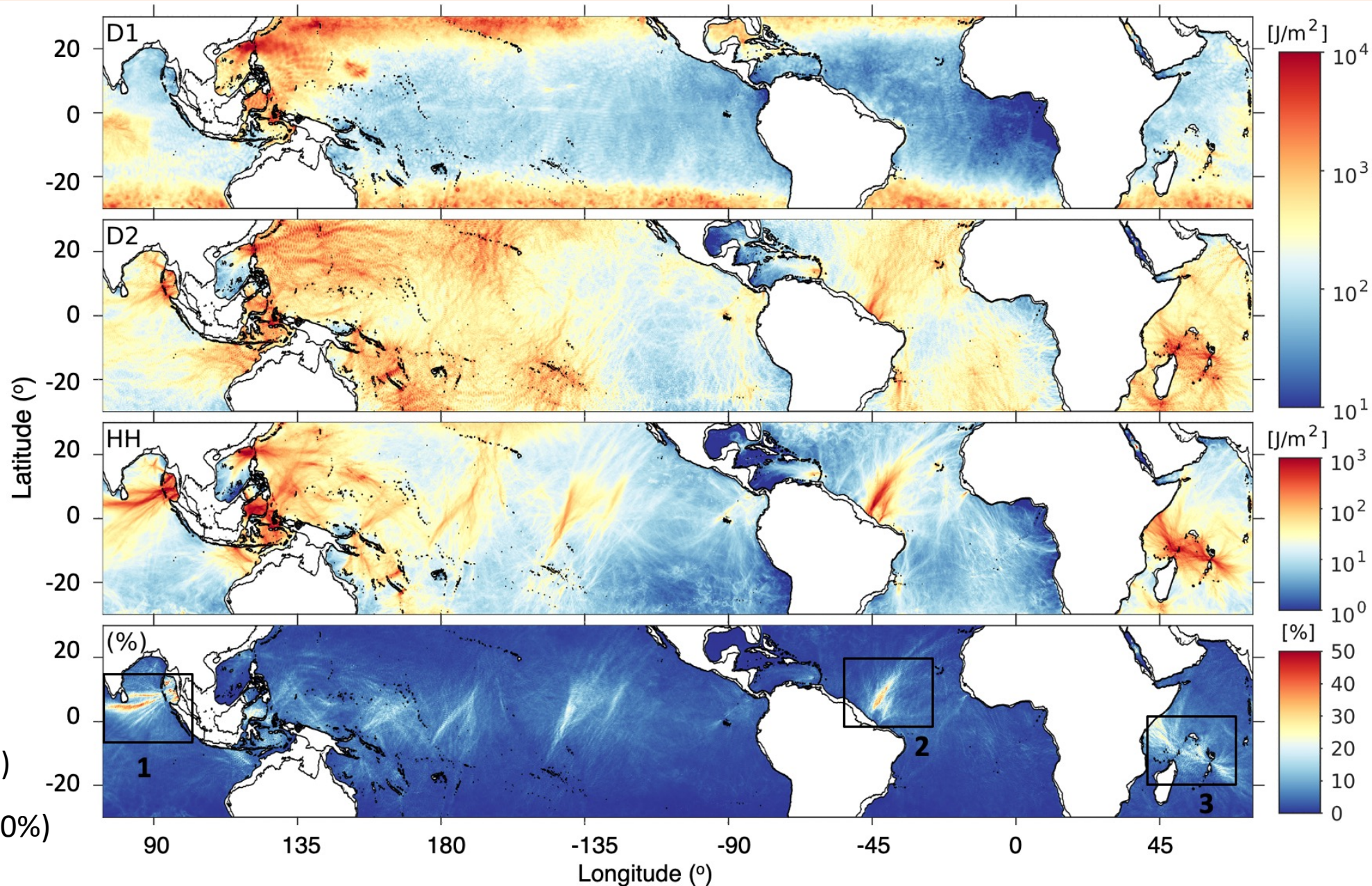
2. Wave-mean flow energy transfer
3. Dissipation



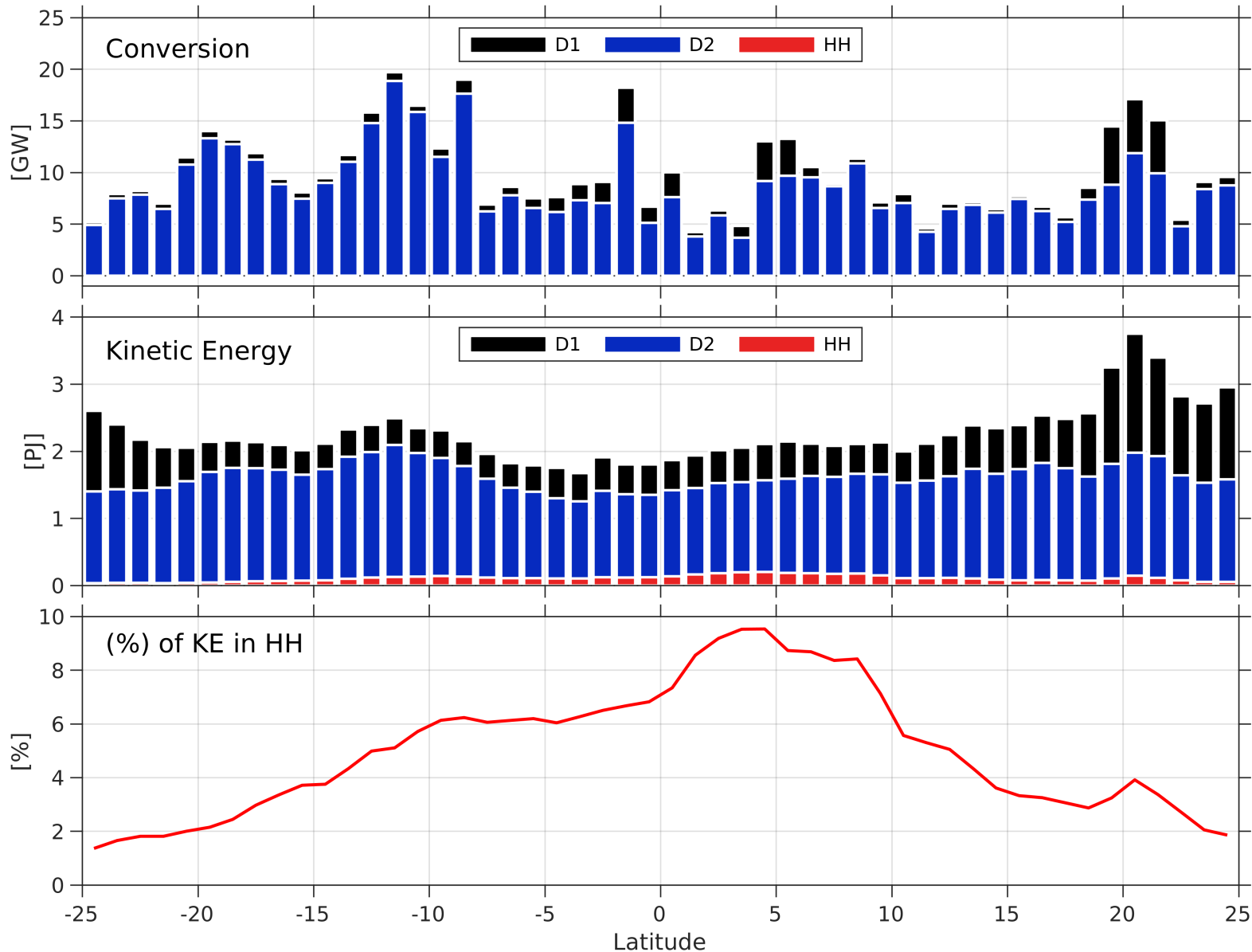
Baroclinic Kinetic Energy

Kinetic Energy

$$\frac{1}{2}\rho_0 \int_{-h}^0 (u'(z)^2 + v'(z)^2) dz$$



Zonal Integrals



Conversion

(D1) = 60 GW

(D2) = 440 GW

(HH) = -2 GW

Kinetic Energy

(D1) = 31.67 PJ (IT + NIW)

(D2) = 76.14 PJ

(HH) = 5.42 PJ (~5%)

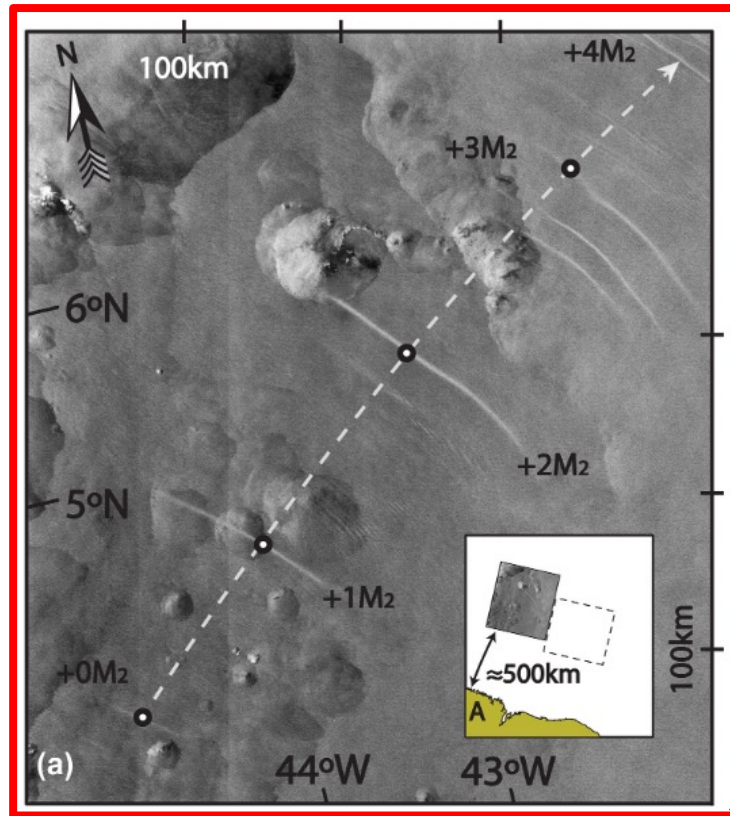
Conversion does not explain the generation of higher-harmonics

HH KE accounts for 5% of IT energy on average, increasing to 10% at the equator

Internal Tide Steepening

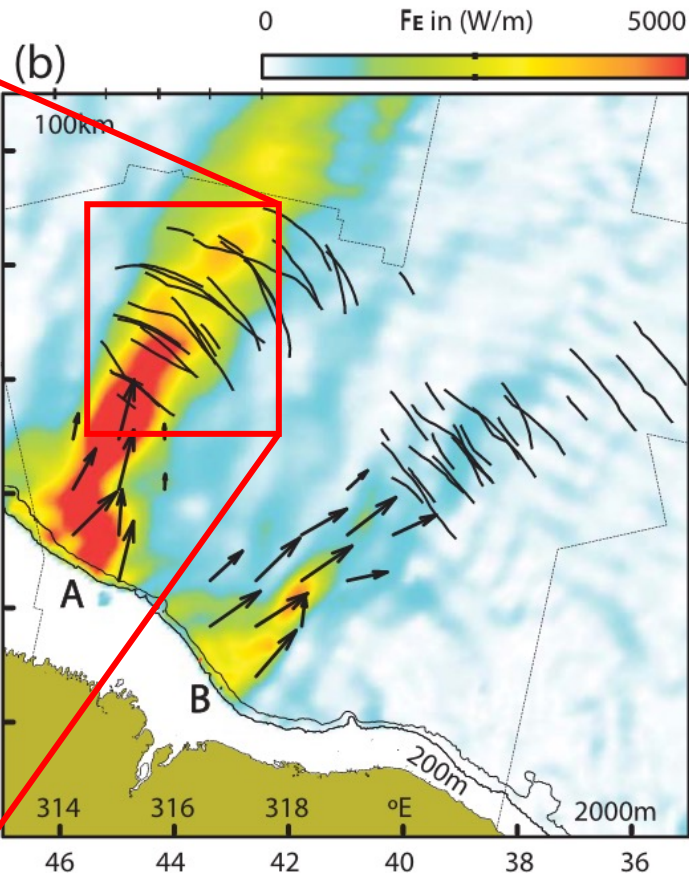
Satellite

Solitary waves at Amazon Shelf



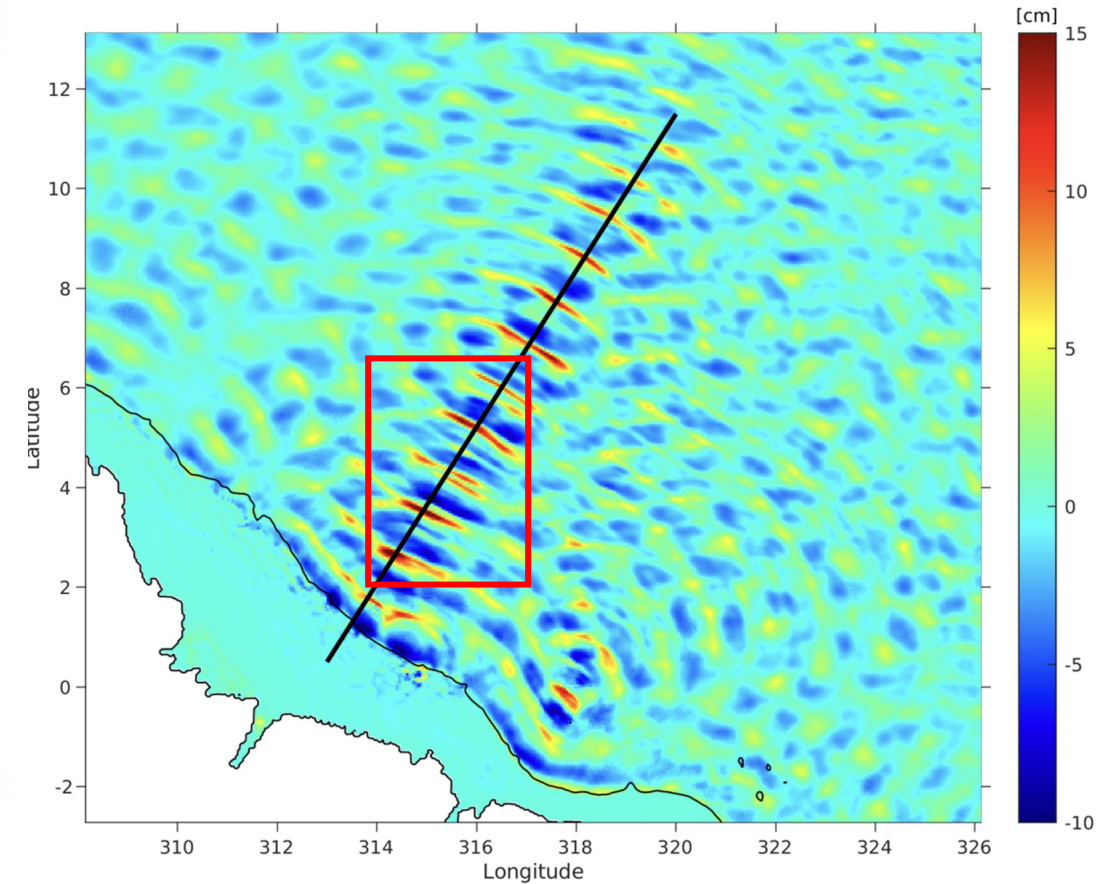
HYCOM

Energy fluxes (D1+D2) frequencies



HYCOM

Steric Sea Surface Height

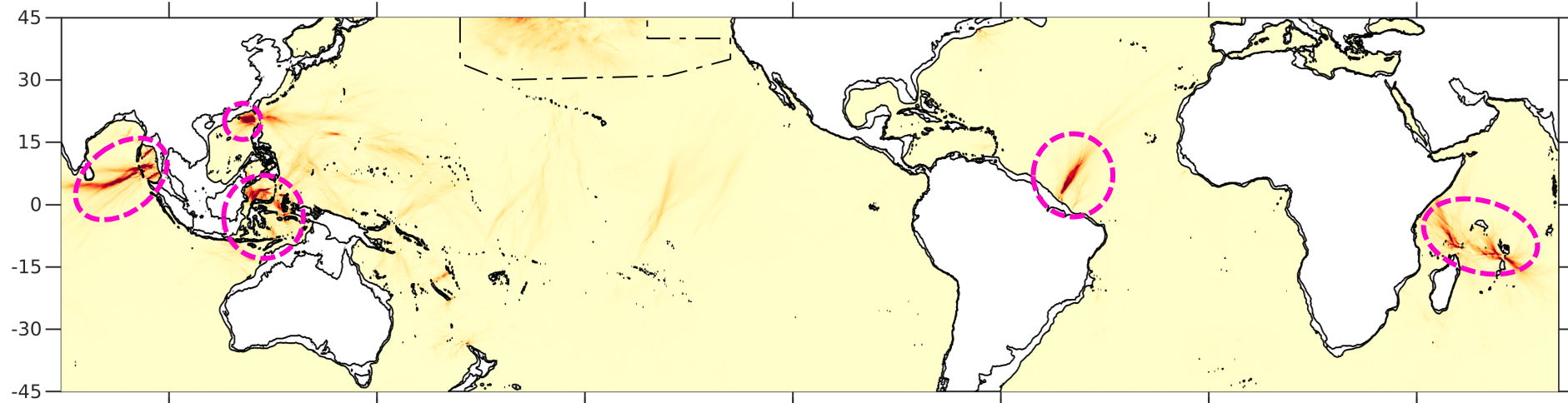


Magalhaes et al. (2016)

Nonlinear Internal Waves (NLIW)

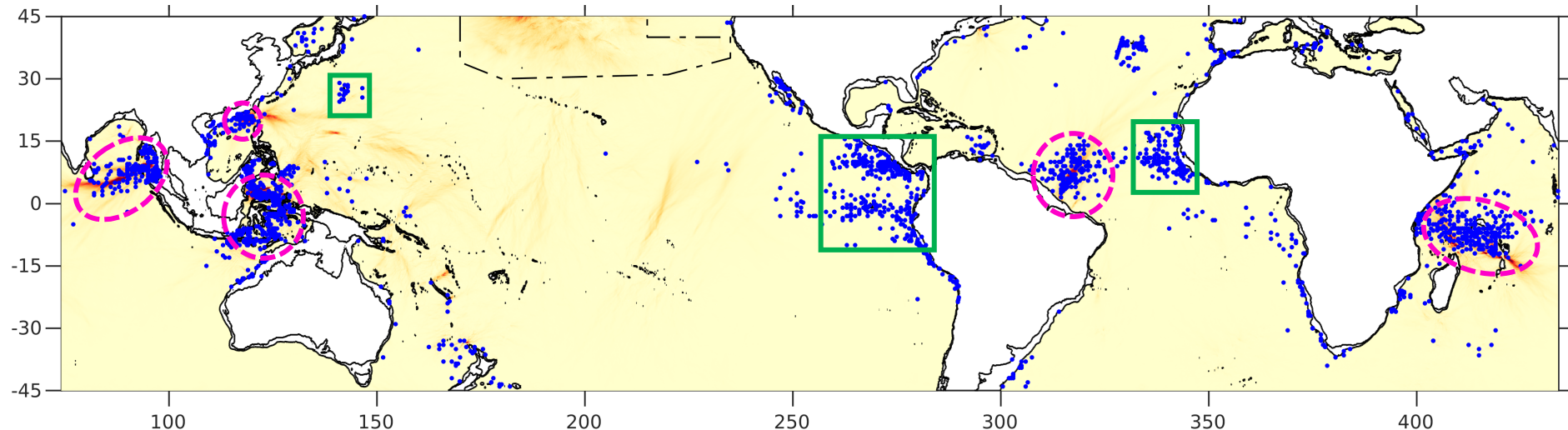
- **Ellipses:**
strong HH fluxes
($> 3 \text{ kW/m}$) coincide
with observations of
NLIW (solitons)

Supertidal (HH) pressure flux in HYCOM



- **Boxes:**
 - Are these NLIW of *nontidal* origin?
 - Tidal generation sites are not well resolved?

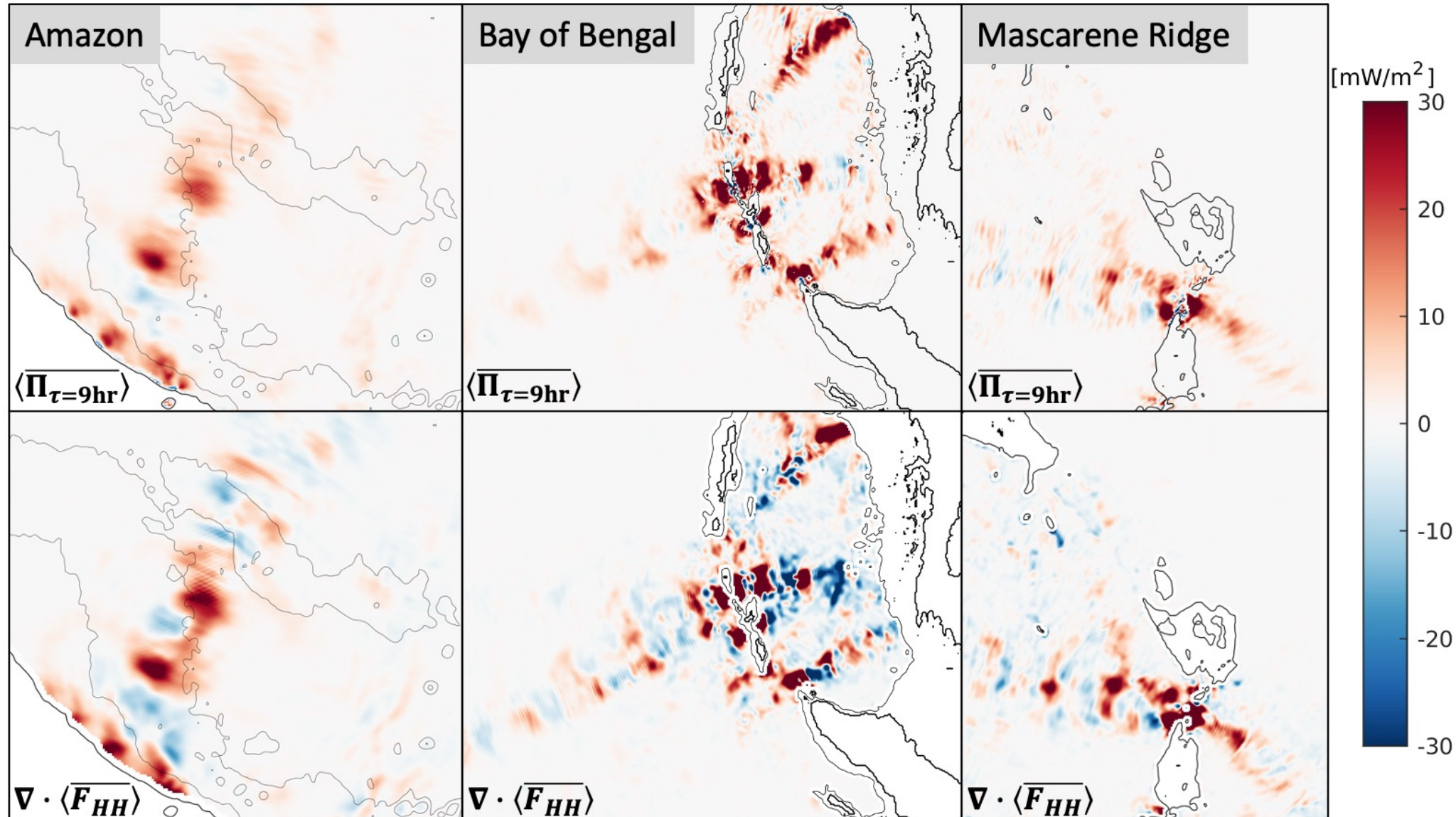
Location of NLIW observed in 250m resolution satellite imagery (Jackson et al. 2012)



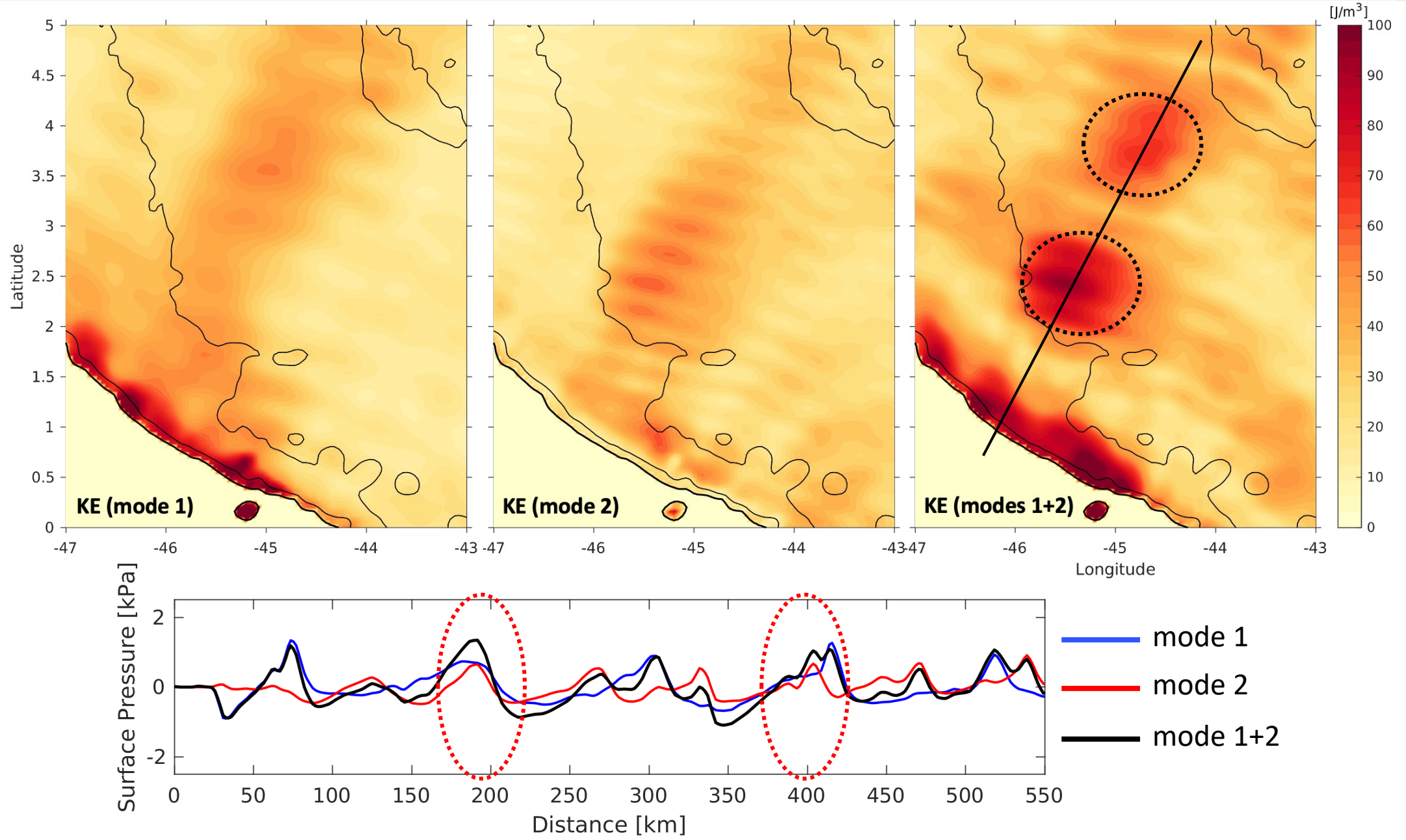
Nonlinear transfer to higher-harmonics

Nonlinear Energy
transfer to HH
(coarse-grained KE)

Supertidal energy
flux divergence

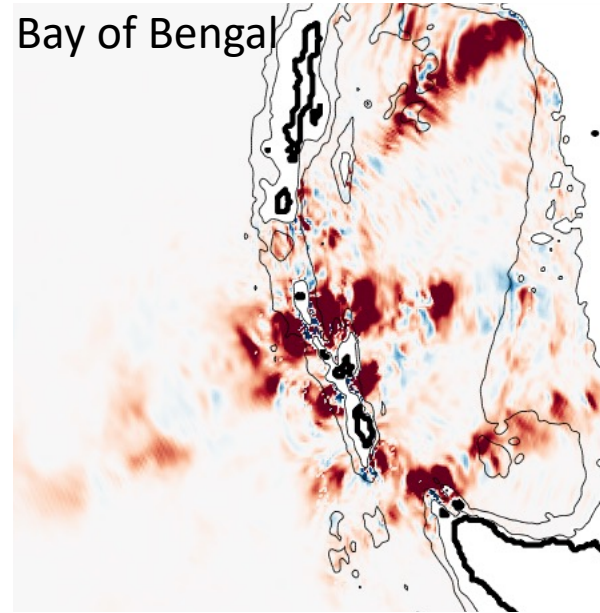
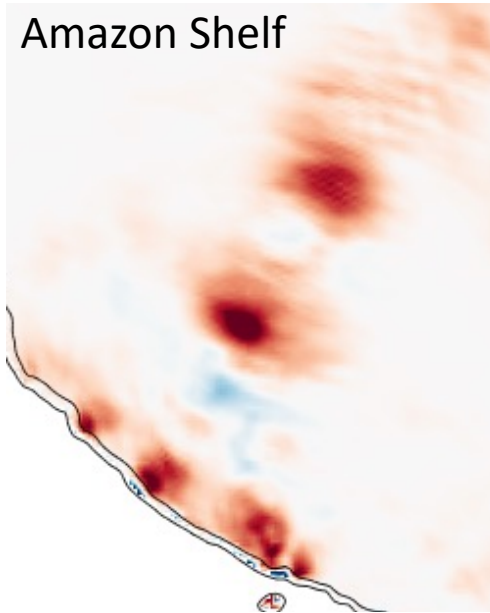


Vertical Mode Decomposition

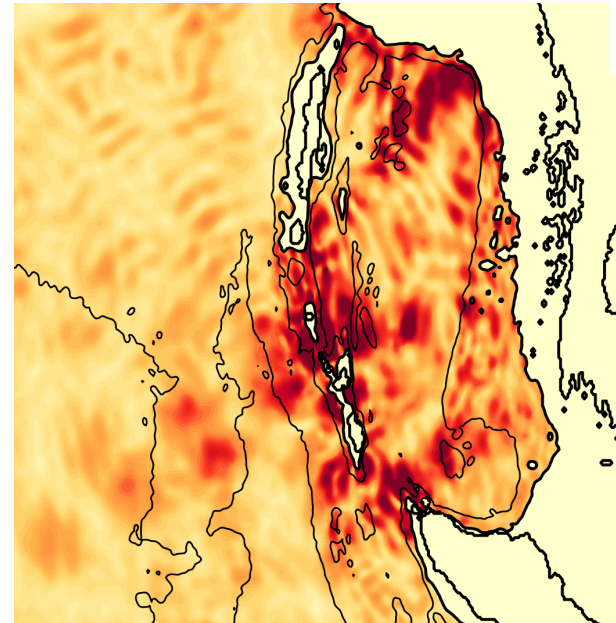
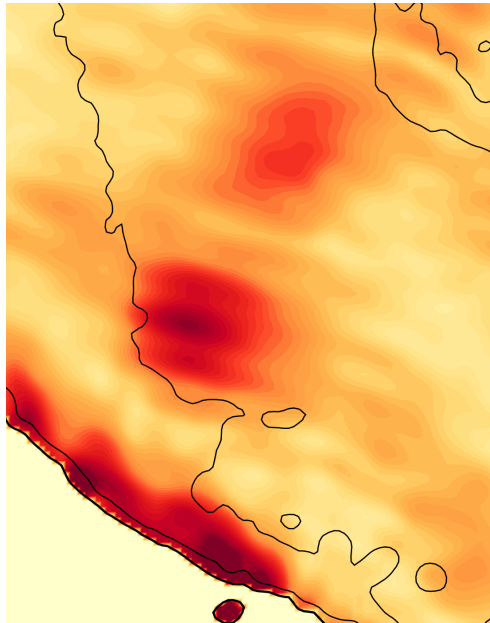


NLIW energy transfer – wave modes

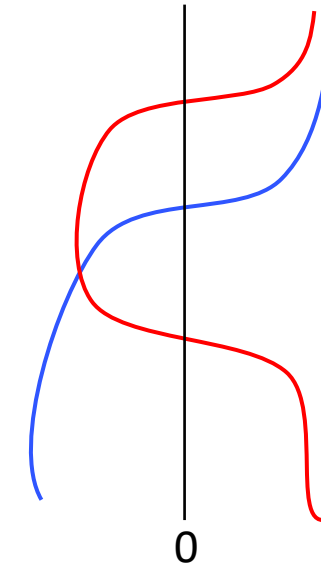
Nonlinear energy
scale transfer to
higher-harmonics



Surface Kinetic
Energy for the
superposition of
modes 1 and 2

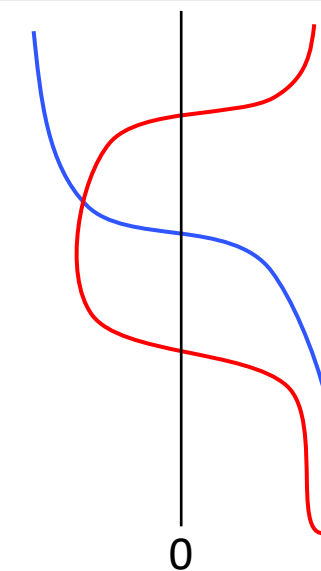


Constructive Interference



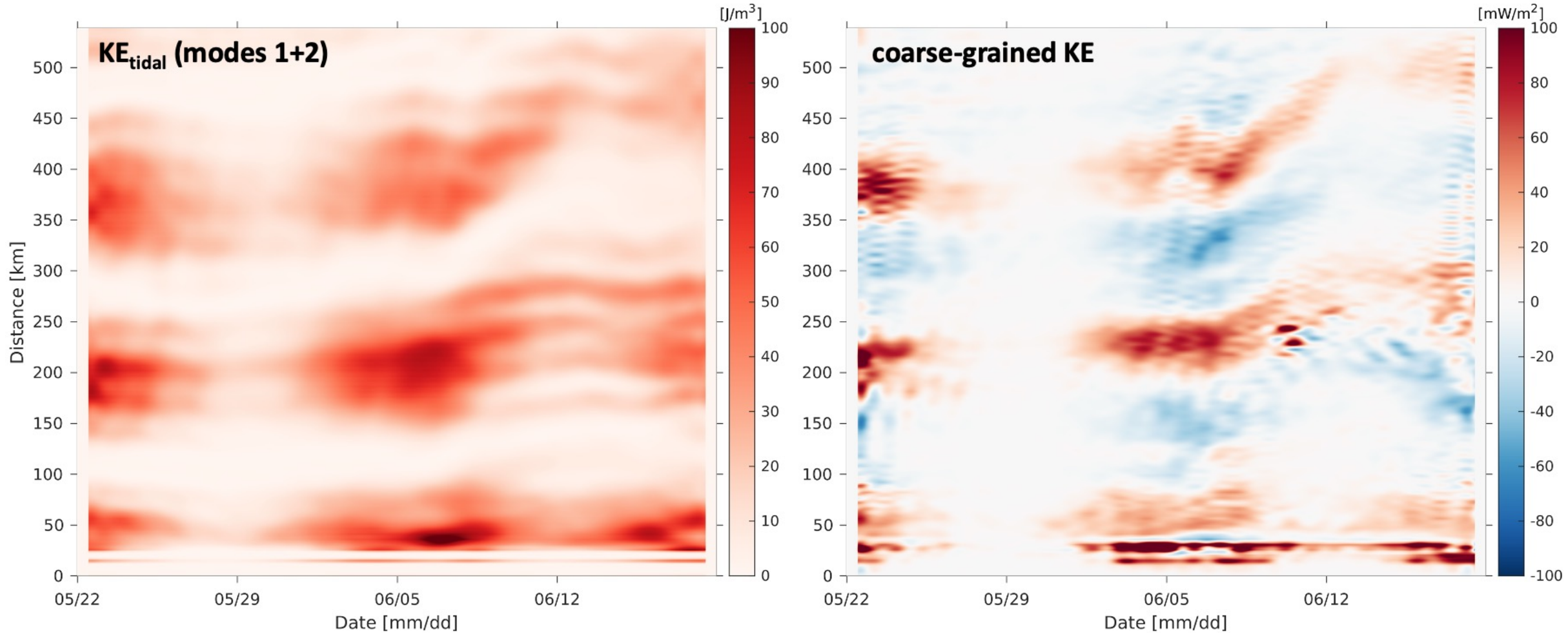
— mode 1
— mode 2

Destructive Interference



— mode 1
— mode 2

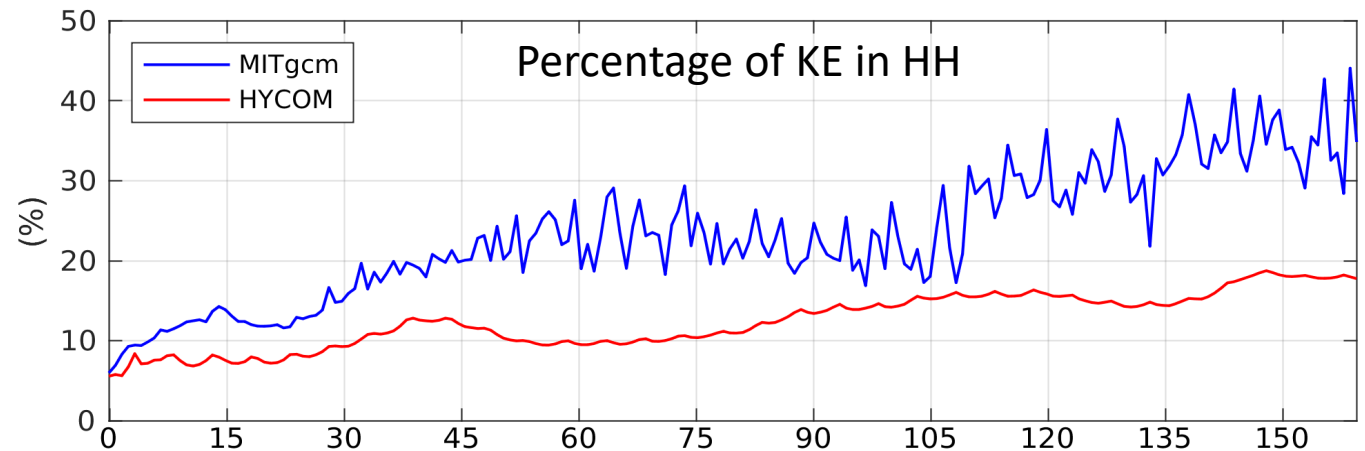
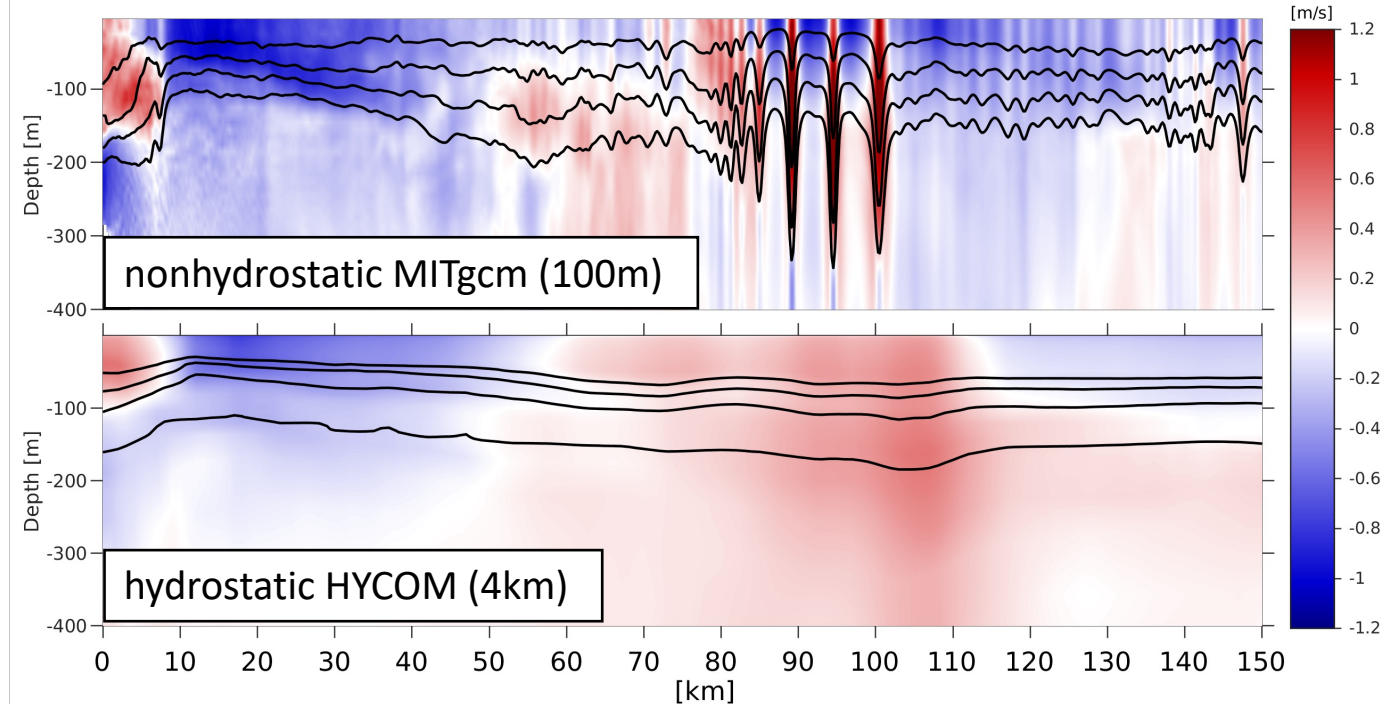
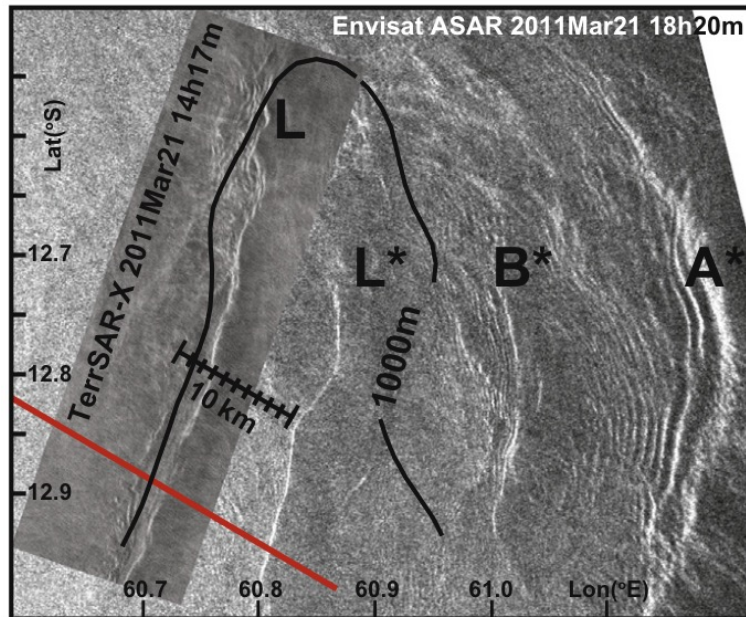
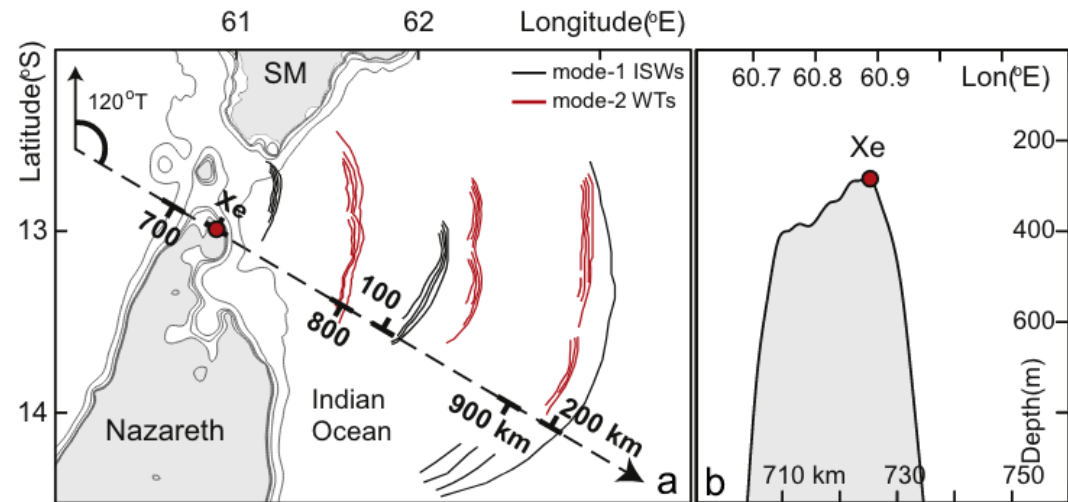
Spatial and temporal modulation



NLIW energy transfer modulated by the spring-neap cycle and slowly-varying stratification changes due to large scale forcing

Are solitary waves resolved in HYCOM?

Solitary Waves at Mascarene Ridge (da Silva et al. 2015)



Summary

- At strong internal tide generation sites, supertidal energy constitutes 20-50% of the total internal tide energy
- Areas with high supertidal energy in HYCOM coincide with observations of nonlinear internal waves (NLIW)
- NLIW energy transfer to supertidal frequencies reveals a banding pattern, where the constructive interference of mode 1 and mode 2 internal tides results in the steepening of the internal tide
- Globally, internal tides transfer a net 40GW to HH within $\pm 25^\circ$
- At current horizontal grid resolution (~ 4 km), these numbers may not be accurate, as solitary waves are not well resolved

