Reconstructing the spatial and temporal elevation signals from ICESat-2

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Motivation





 It is known that residue geoid signals may be present on large lakes after correcting the water surface elevations for the geoid

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- Previously modeled using CryoSat-2 and SARAL/AltiKa (Jiang at al., 2019)
- However, this is very clear with ICESat-2
- The residue signal affects the water level time series especially for geodetic altimetry missions

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• The residue signal deteriorates the time series

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Motivation





- We can do a descent job when just considering one track
- A common reference is needed if more tracks are used to reconstruct the water level time series
- To improve the water level time series based on geodetic mission like CryoSat-2 we must be able to minimize the effect of the residue signal
- DTU Space OSTST, Venice November 2022 3.11.2022 Assuming that the spatial signal is constant in time, we can try to separate

Spatial-temporal Model

• We assume that the ICESat-2 observations can described as

$$H_{i,t} = \omega_i + \mu_t + \epsilon_{i,t}$$
 where $\epsilon_{i,t} \sim N(0, \sigma_{obs}^2)$

- Here t = 1, ..., N where N is the number of times and i = 1, ..., M, where M is the number of cells in the spacial grid
- Here μ is a random walk and ω is a Gaussian Markov random field described as

$$\begin{split} \mu_t &= \mu_{t-1} + \eta_i \quad \text{where } \eta_t \sim N(0,\sigma_{RW}^2) \\ & \omega \sim N(0,\sigma_\omega^2 Q^{-1}) \end{split}$$

- The precision matrix Q (inverse covariance matrix) is defined as $Q = Q_0 + I$
- Here Q_0 specifies the neighbor structure and is given by

$$Q_0(i,j) = \begin{cases} \phi \# \text{neighbors}, & \text{if } i = j, \\ -\phi, & \text{if } i \sim j, \\ 0, & \text{otherwise.} \end{cases}$$
(1)

- Here ϕ is a parameters that controls the correlation
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Pratical Workflow

- Project ICESat-2 data to UTM coordinates
- Define a grid for the spatial solution, must define spatial resolution
- Use e.g. lake shapefile to define lake boundary in the grid
- \bullet Set up the neighbor structure, the Q_0 matrix
- Assign measurements to grid cells
- Use model (previous slide) to estimate residual grid and time series
 - Model is implemented in R via the R-package "TMB" http://tmb-project.org

Spatial reconstruction of ICESat-2 water levels



EGM2008 correction lake Tanganvika

EGM2008 correction lake Tanganvika

- Left: 3 x 3 km grid cells, Right: 1 X 1 km grid cells
- In the 1 X 1 km solution we see the tracks. Correlation in the data is not accounted for
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Temporal reconstruction of ICESat-2 water levels



Time in deimal years

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Corrected water level time series



• Still some residue signal, but much better than before

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Corrected water level time series CryoSat-2 13 1 769 2020.5 2021.0 2021.5 2020.0 2022.0 772.0 Sentinel-3/ Elevation w.r.t. EGM2008 771.0 770.0 2020.0 2020.5 2021.0 2021.5 2022.0 SARAI 771.0 770.0 769.0 2020.5 2021.0 2021.5 2022.0 2020.0 Time in decimal years

• The improvement is more evident when zooming in

• The lighter colors show the water level time series before the correction

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- Set up a spatial-temporal model to describe the ICESat-2 water levels
- Apply spatial grid to correct the water level from other altimetry missions
- We obtain improved water level time series from CryoSat-2, AltiKa, and Sentinel-3
- More investigations are needed to improve the model
- To space agencies: Missions in a geodetic orbit (like CryoSat-2, ICESat-2) are essential for hydrology

Thank you, questions?



Please, consider submitting to EGU 23-28 April 2023

G3.2 EDI*

Advances in methods and applications for satellite altimetry .

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