# A Broadband View of the Sea Surface Height Wavenumber Spectrum (The contribution of surface waves to the SSH variability)

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This is how we usually picture the SSH spectrum:

Red spectrum: variance decreases with wavenumber

Consistent with QG turbulence theory







# but ... surface waves!

- At scales from 1-500 m the SSH is dominated by surface gravity waves
- Blue spectrum: variance increases with wavenumber



## So what?

mesoscales

Scale separation between QG turbulence and surface wave dynamics:

• The red and blue zones have been traditionally explored independently

 But ICESat2 resolves scales where many processes overlap, as will SWOT

 Our goal: connect red and blue segments of the spectrum



Surface







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#### Assessment of ICESat-2 for the recovery of ocean topography

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 How does ICESat-2 view the ocean surface?

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# Airborne laser altimetry: Modular Aerial Sensing System (MASS)





- Scanning Lidar (~ 500 m swath)
- Measures the SSH with sub-meter horizontal resolution
- Resolves the 2D wave field

# SWOT pre-launch airborne campaign (April 9, 2019)

Measurements from the Scripps Institution of Oceanography (SIO) MASS





Strong winds 11-15 m/s
Swath width: ~ 500 m
Hs = 3 m

Sea:	Swell:
$T_p = 6 s$	$T_{p} = 11 s$
$\lambda_{\rm p} = 60 \ {\rm m}$	$\lambda_{\rm p} = 200 \ {\rm m}$
$\theta_{\rm p} = 321^{\circ}$	$\theta_{\rm p} = 308^{\circ}$



Villas Bôas et al. (2022) https://doi.org/10.1029/2021GL096699



The red zone (k < 10<sup>-1</sup> cycles/km)
The spectrum from MASS is red and typical of mesoscale turbulence + Garrett-Munk spectrum
Falls with a k<sup>-11/3</sup> to k<sup>-5</sup> slope



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- Consistent with ALtiKa spectrum (Chereskin et al., 2019)



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- Falls with a k<sup>-11/3</sup> to k<sup>-5</sup> slope
- Consistent with ALtiKa spectrum (Chereskin et al., 2019)
- Consistent with the llc4320



The gray zone (10<sup>-1</sup> < k < 1 cycles/km)</p>

- The spectrum flattens out becoming fairly white
- Many dynamical processes could be contributing to the SSH variance at these scales
- Consistent with energy levels from Infra-Gravity waves (e.g., Ardhuin et al, 2013; Aucan & Ardhuin, 2013)



The blue zone (k > 1 cycles/km)
At high wavenumbers the spectrum is blue and dominated by surface waves
We see both the swell and sea peaks
Up/down-wind and cross-wind are

remarkably different

# Filtering the surface wave signal

Blackman-Harris window in the azimuth direction







The blue zone (k > 1 cycles/km)
 The peak is shifted towards lower wavenumbers (especially for the swell)

 The variance is much lower in comparison to the omnidirectional spectrum

#### Take aways

The variance in the surface wave band can be over
 20 times larger than the variance at submesoscales.

 Without directional wave information, it could be challenging to interpret the SSH variability at scales from 1 km to 100s of meters

 SWOT's OBP filter should remove most of the surface wave energy. The potential for aliasing will depend on dominant wavelength, height, and direction.

- Higher waves → filtering is less effective
- Higher relative angle → filtering is less effective



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