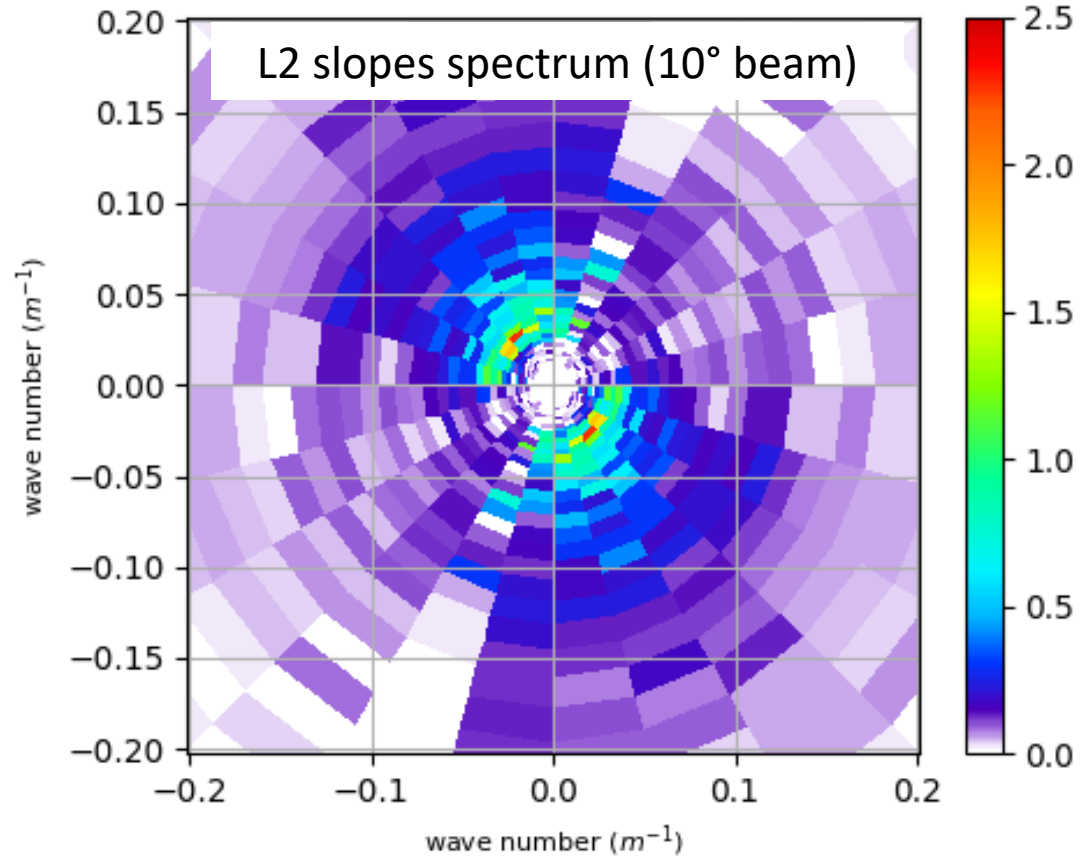
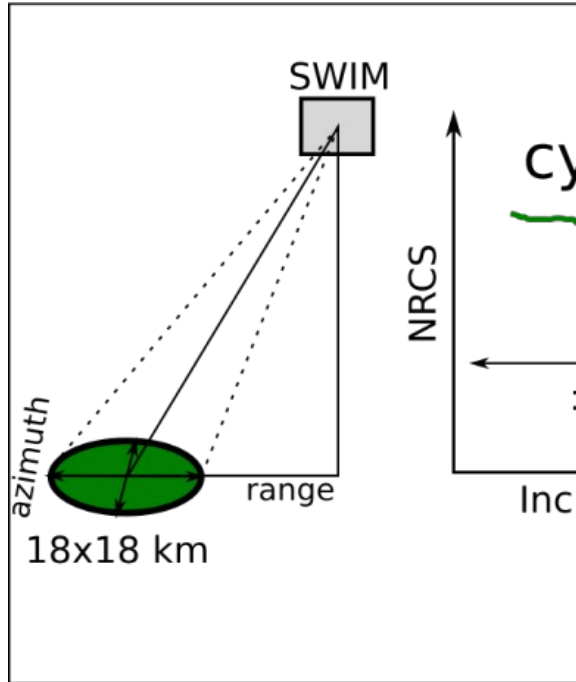


Towards a global Stokes drift product from SWIM/CFOSAT

Charles Peureux, Annabelle Ollivier, Hélène Etienne, Sandrine Mulet¹
Cédric Tourain²
Lotfi Aouf³

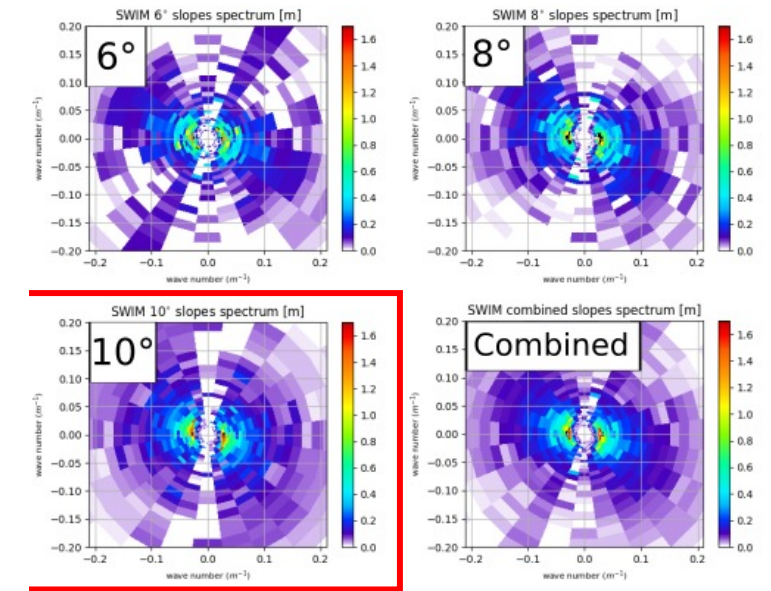
Introduction - SWIM

NRCS modulations <-> ocean waves slopes

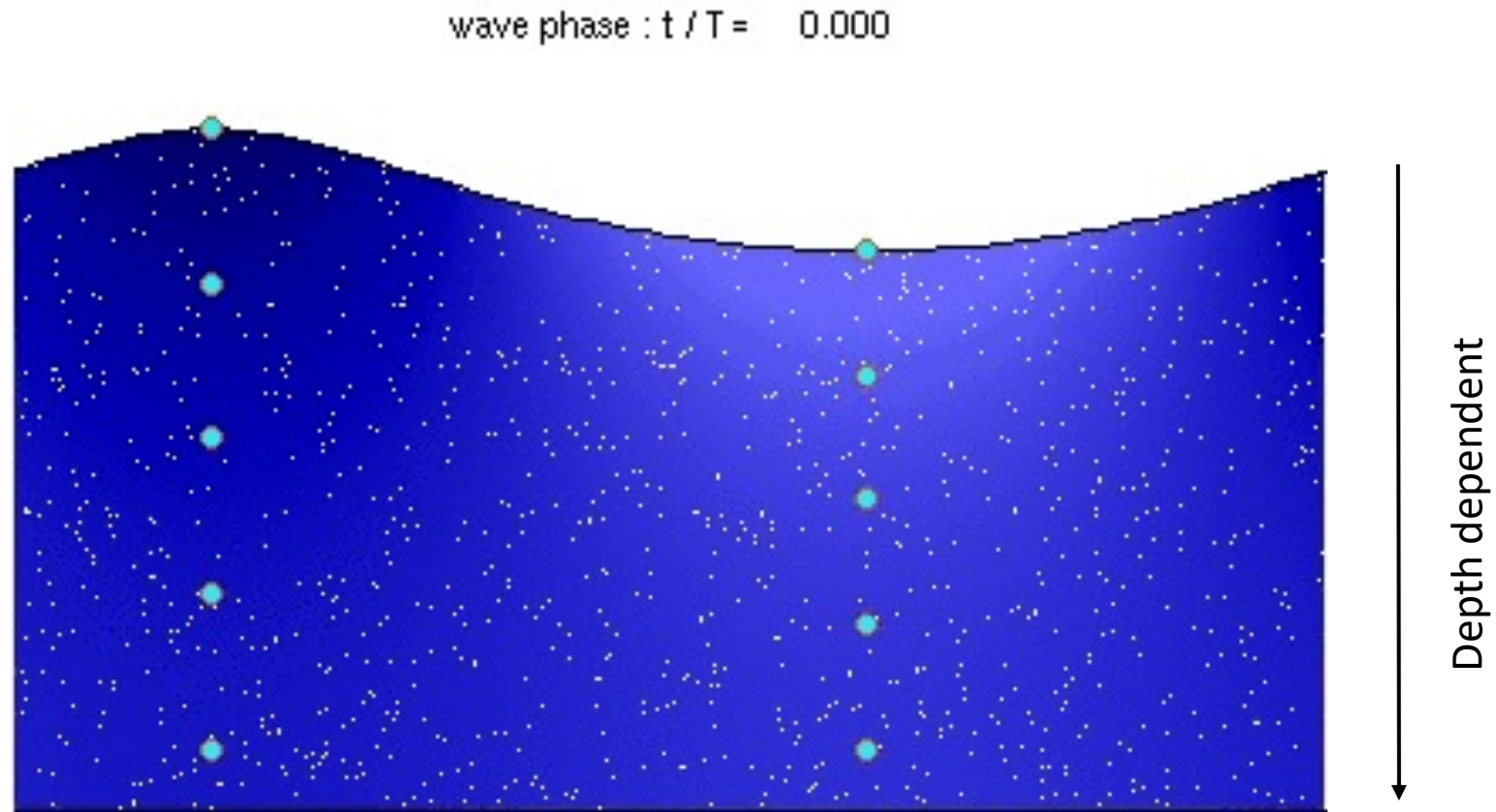


$\lambda > 22 \text{ m}$

L2 slopes spectra



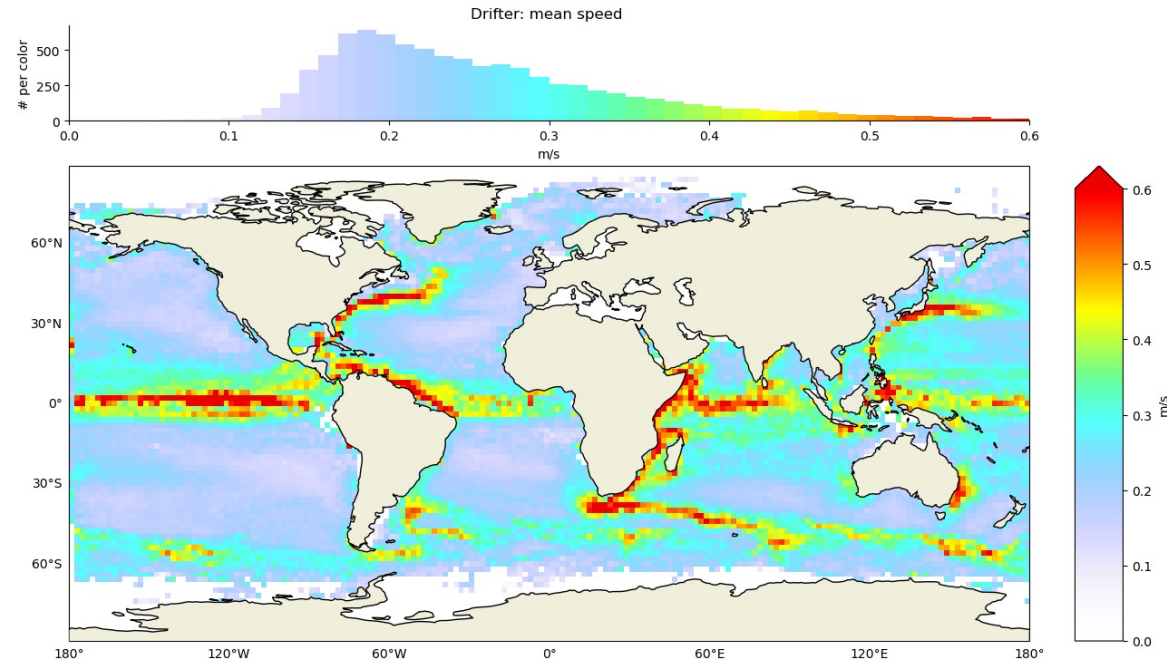
Introduction – Stokes drift



From wikipedia, Stokes drift

Introduction – Stokes drift

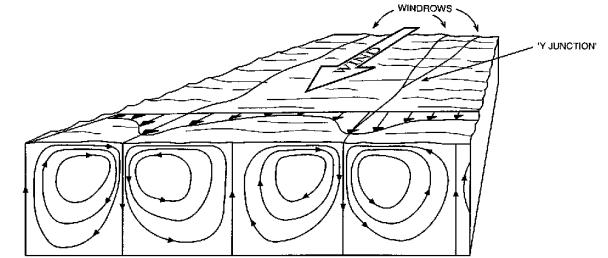
- Drift at the ocean surface (oil, plastics, larvae, plankton, etc ...)



Mean drifters derived currents (courtesy of H. Etienne, CLS)



Lines of sargassum at a Langmuir cell border



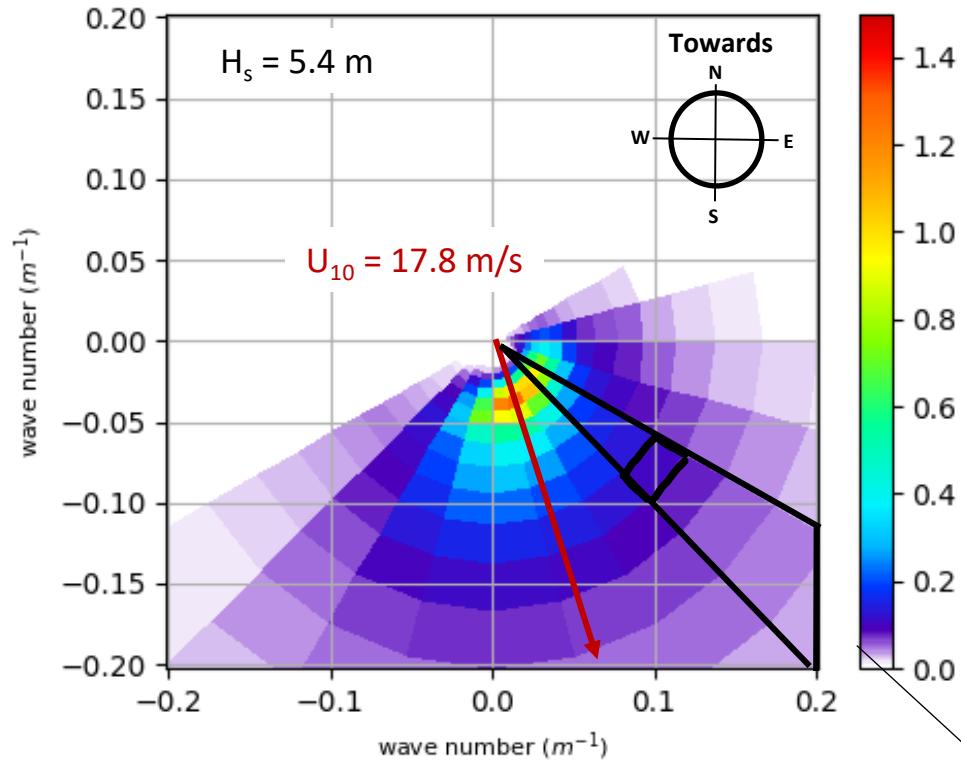
- Ocean surface circulation

*The Stokes drift climate knowledge at the global scale
only relies on models today*

Stokes drift estimation from SWIM

Kenyon 1969

MODEL (WAM)



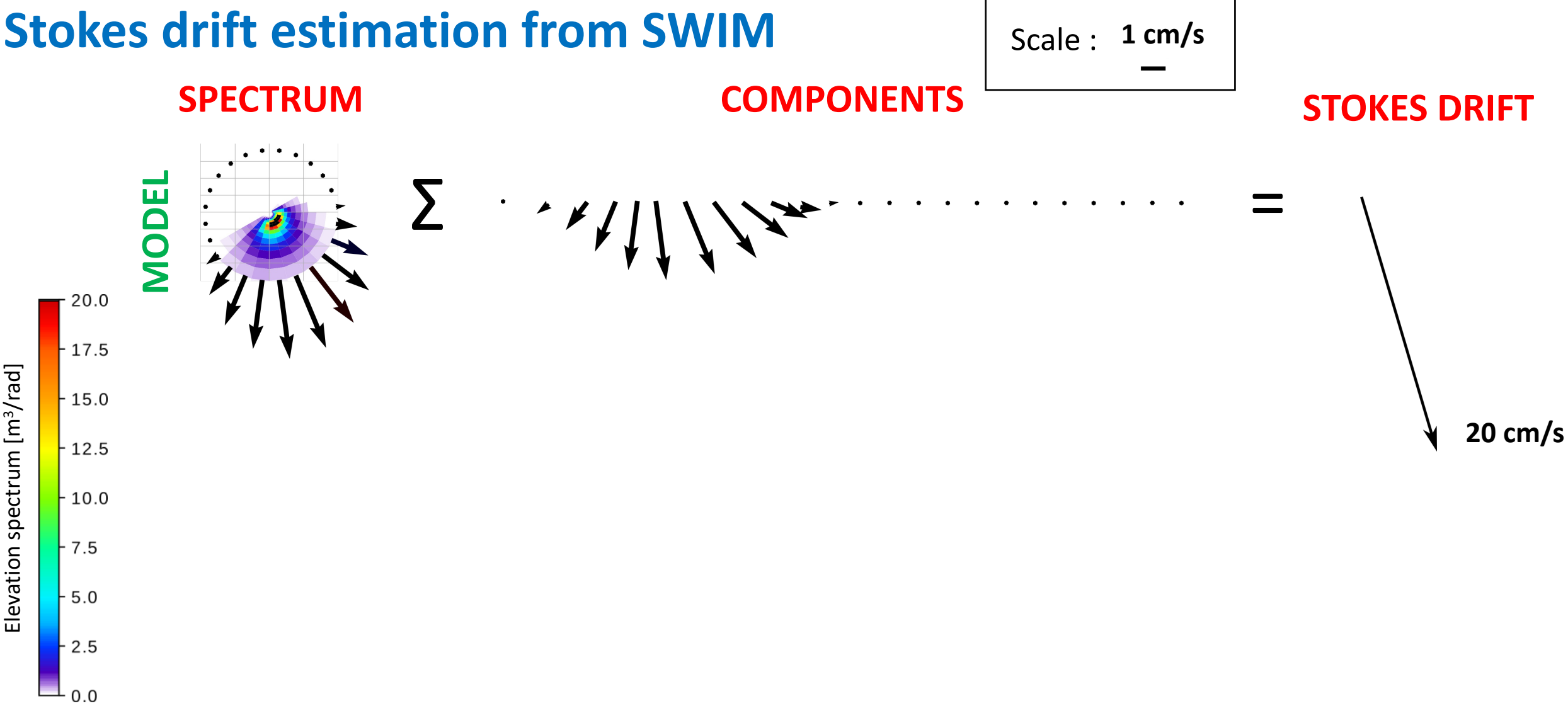
Stokes component =

$$\int k \times dk \times S(k, \varphi) \times \text{Phase velocity} \times e^{2kz}$$

z = depth

$$\sqrt{\frac{g}{k}}$$

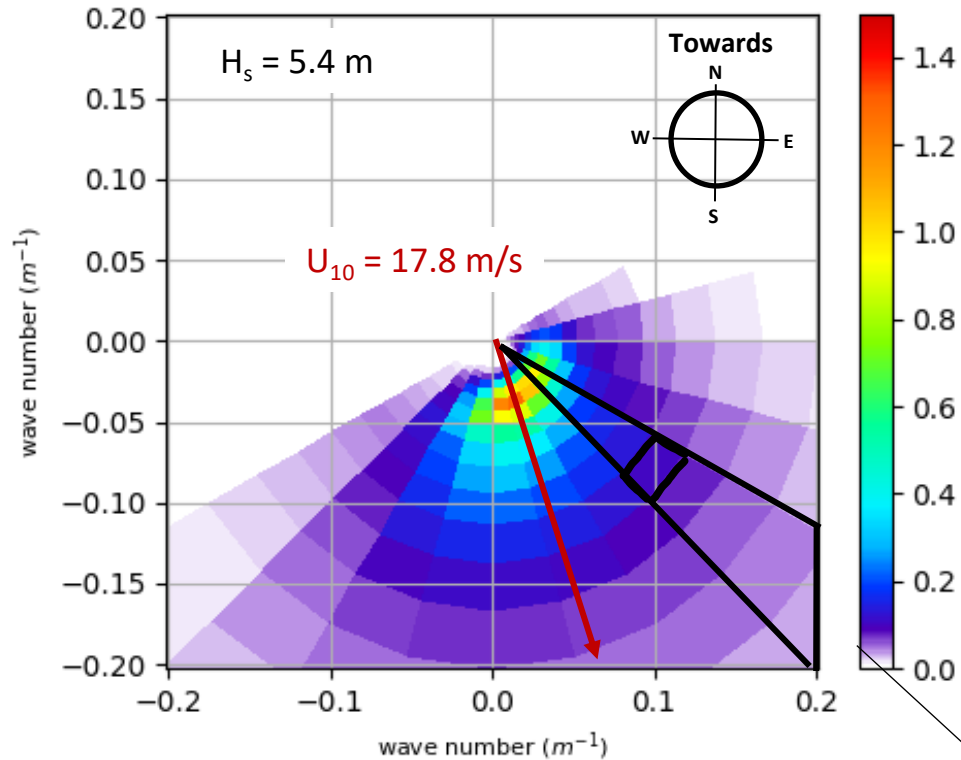
Stokes drift estimation from SWIM



Stokes drift estimation from SWIM

Kenyon 1969

SWIM RAW (10°)



Stokes component =

$$\int k \times dk \times S(k, \varphi) \times \text{Phase velocity} \times e^{2kz}$$

$z = \text{depth}$

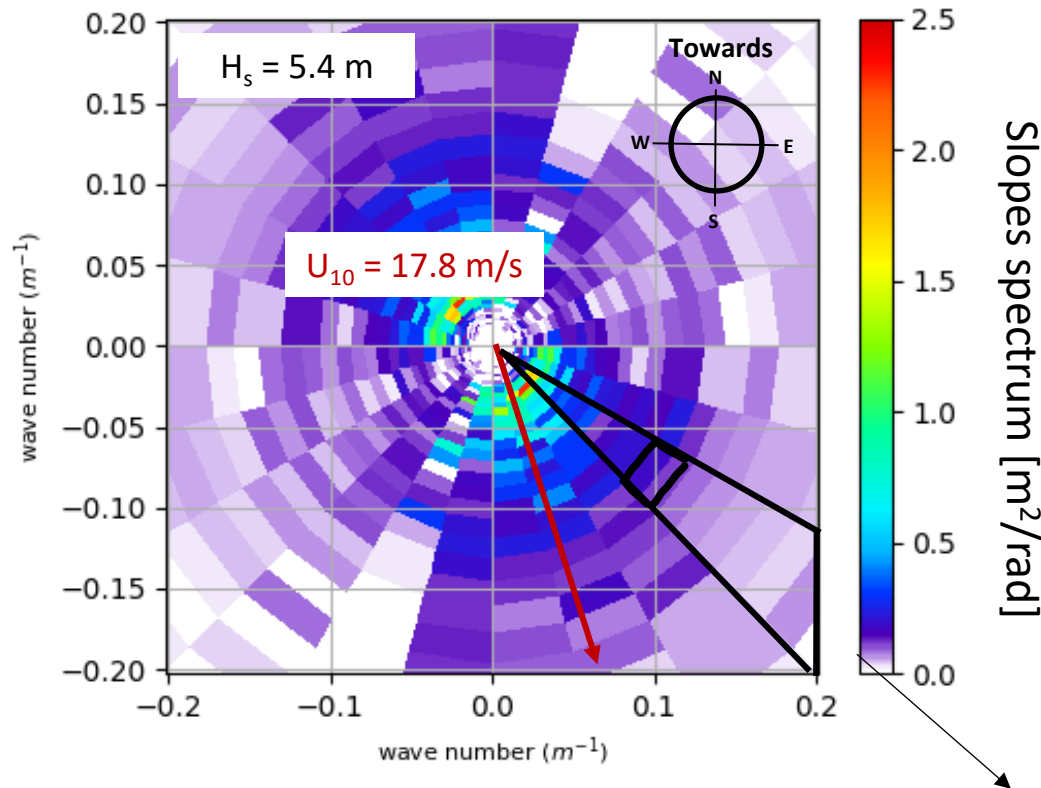
$\sqrt{\frac{g}{k}}$

3.7 cm/s

Stokes drift estimation from SWIM

Kenyon 1969

SWIM RAW (10°)



Stokes component =

$$\int k \times dk \times d\varphi \times S(k, \varphi) \times \text{Phase velocity} \times e^{2kz}$$

z = depth

$$\sqrt{\frac{g}{k}}$$

2.3 cm/s

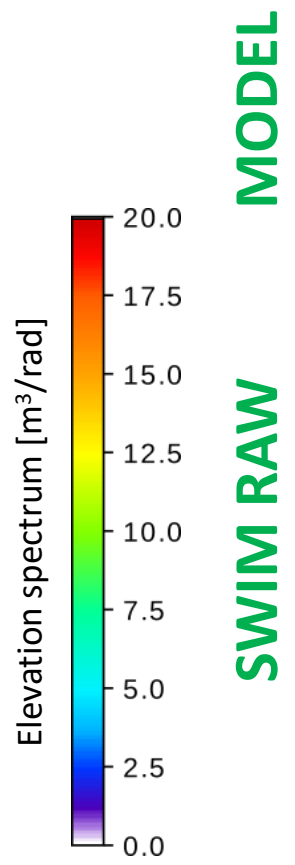
Stokes drift estimation from SWIM

Scale : 1 cm/s
—

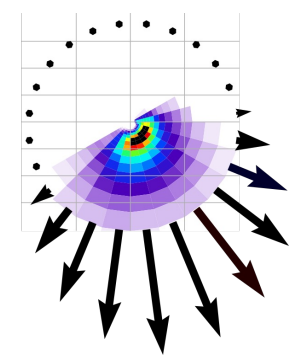
SPECTRUM

COMPONENTS

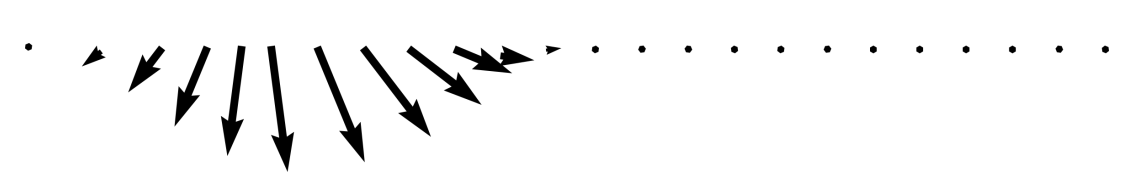
STOKES DRIFT



MODEL

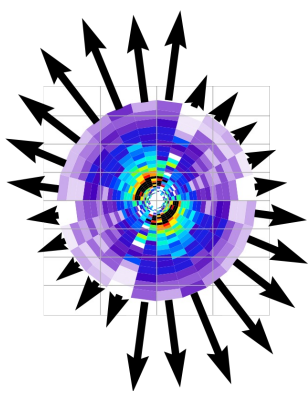


Σ

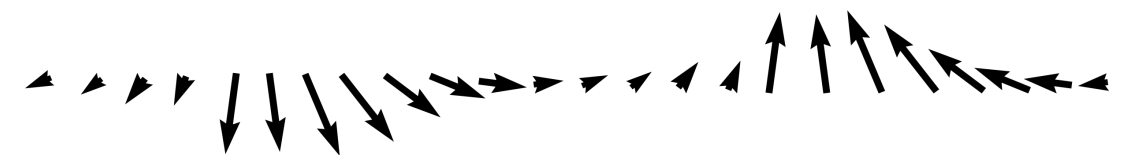


=

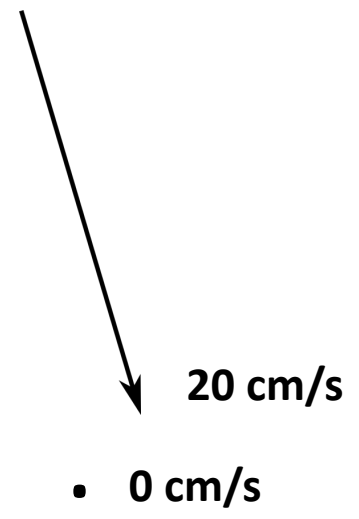
SWIM RAW



Σ



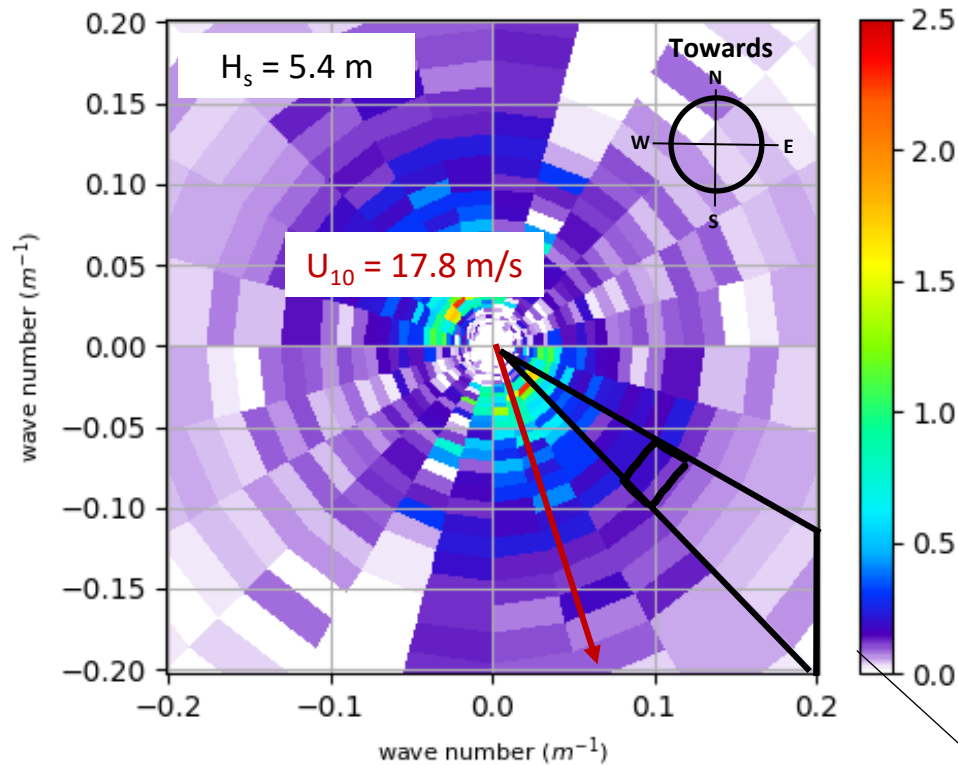
=



Stokes drift estimation from SWIM

Kenyon 1969

SWIM RAW (10°)



Stokes component =

$$\int k \times dk \times S(k, \varphi) \times \text{Phase velocity} \times e^{2kz}$$

z = depth

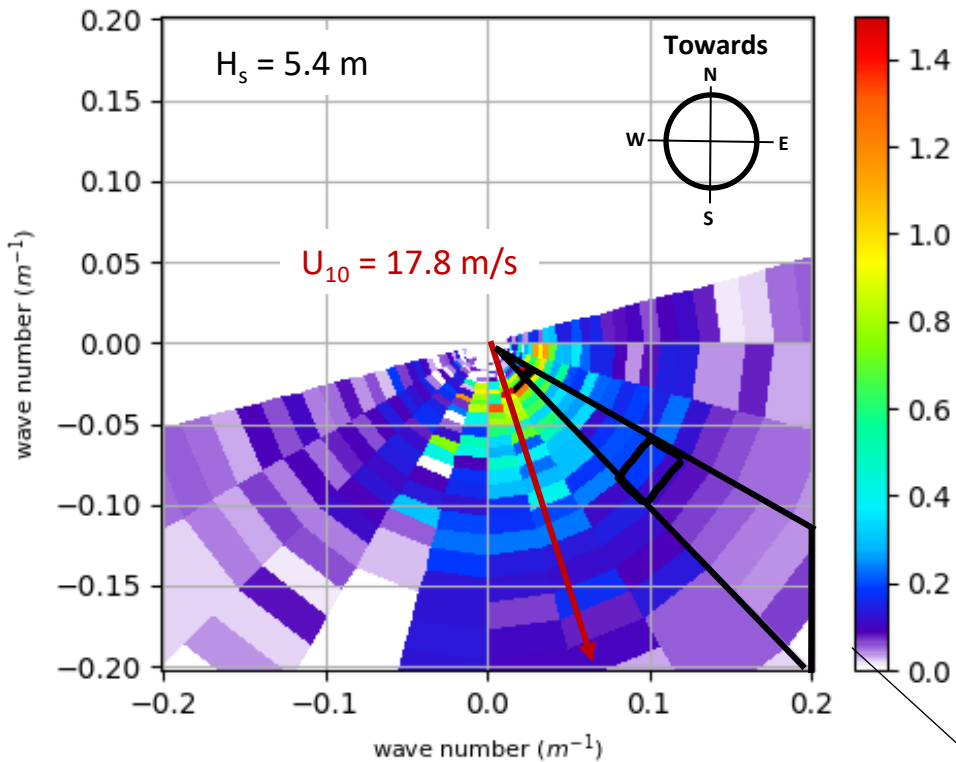
$\sqrt{\frac{g}{k}}$

2.3 cm/s

Stokes drift estimation from SWIM

Kenyon 1969

SWIM (10°)



Stokes component =

$$\int \underbrace{k \times dk}_{d\varphi} \times S(k, \varphi) \times \text{Phase velocity} \times e^{2kz}$$

z = depth

$\sqrt{\frac{g}{k}}$

Stokes drift estimation from SWIM

Scale : 1 cm/s
—

SPECTRUM

COMPONENTS

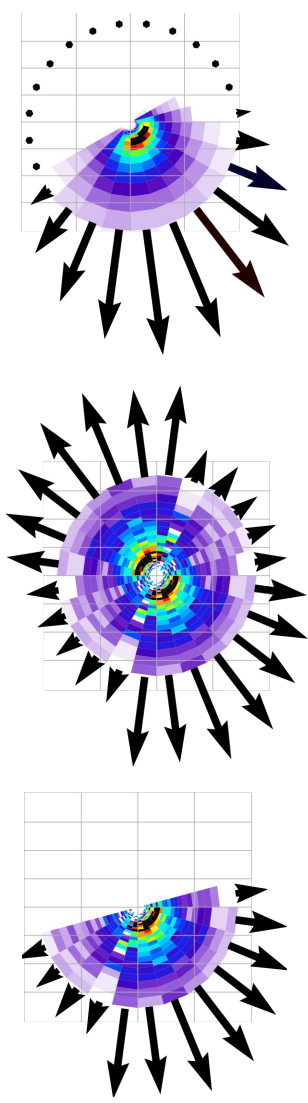
STOKES DRIFT

Elevation spectrum [m³/rad]

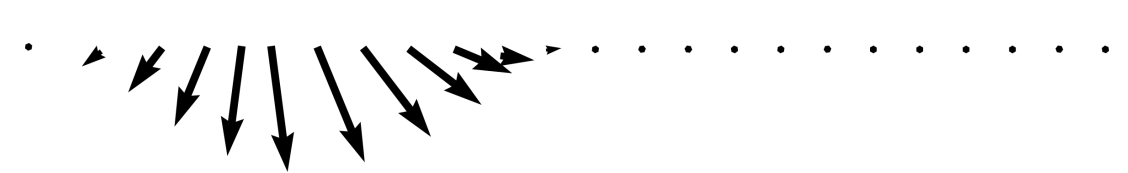
MODEL

SWIM RAW

SWIM



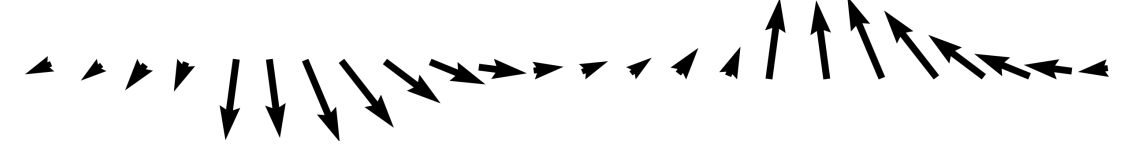
Σ



=

20 cm/s

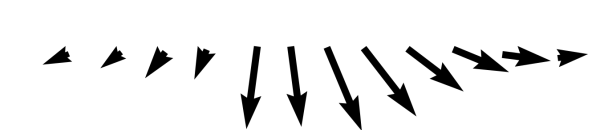
Σ



=

• 0 cm/s

Σ



=

13 cm/s

SWIM Stokes drift estimation from SWIM

Known limitations :

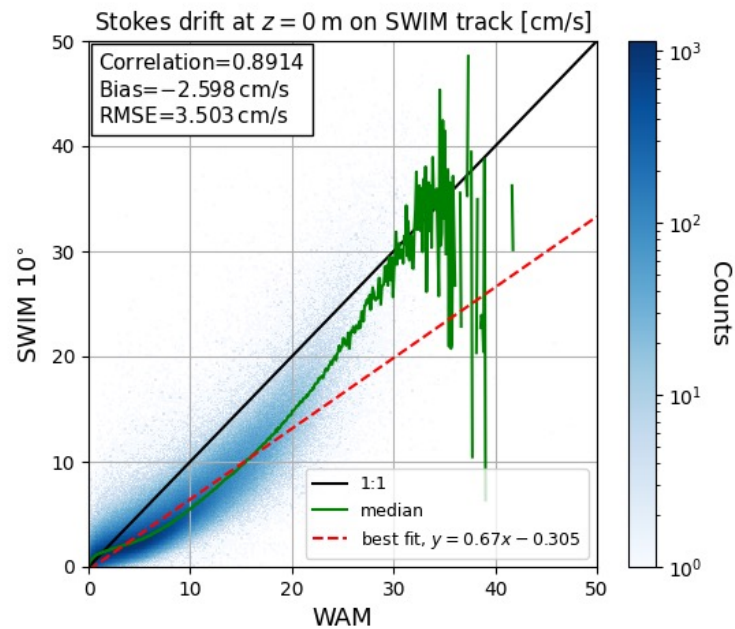
- Ambiguity
- Truncation

Test performed using :

- WAM and SWIM (focus on 10°) **colocated** on year 2021
- Wind direction from ECMWF forecast (in SWIM L2)

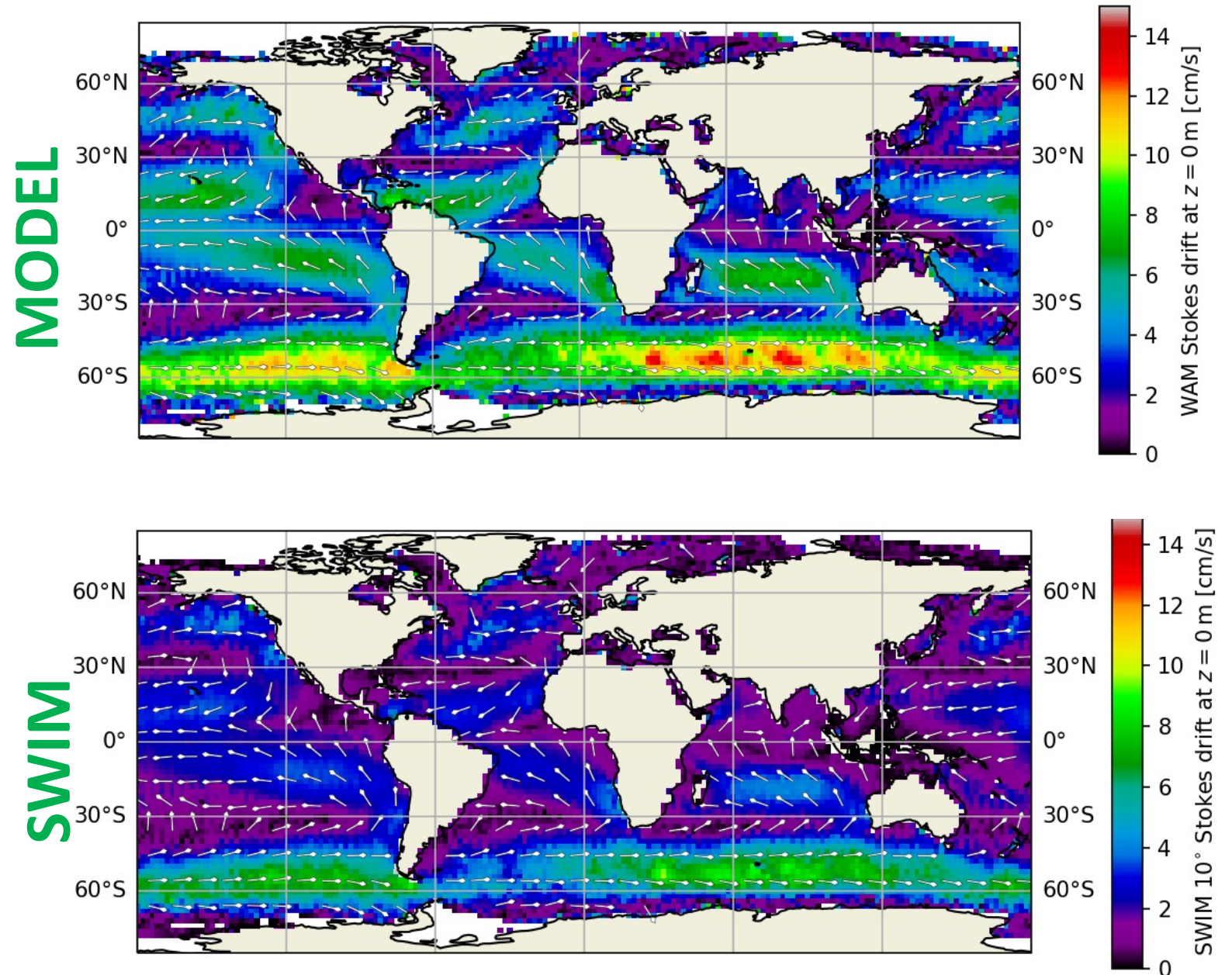
Performances - overview

depth = 0 m



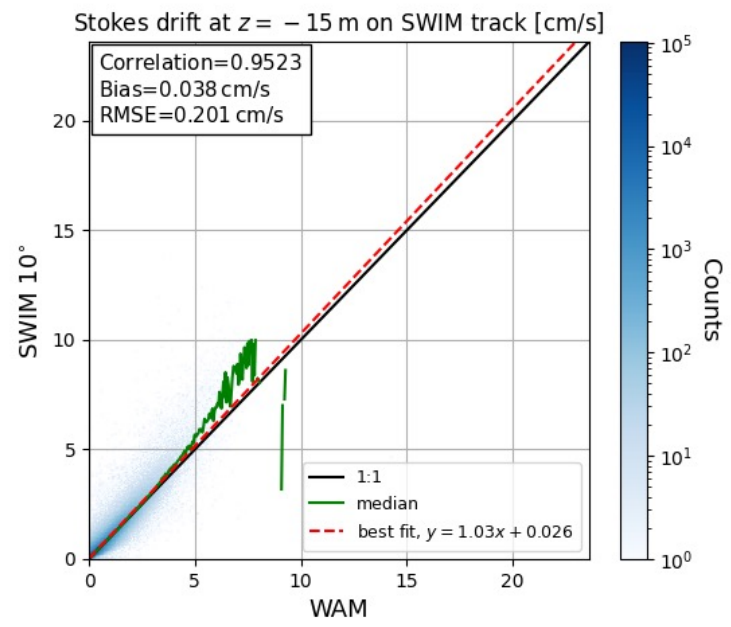
Negative bias
caused by short
waves truncation

Mean Stokes drift vector over 2021 (2x2°) on SWIM track

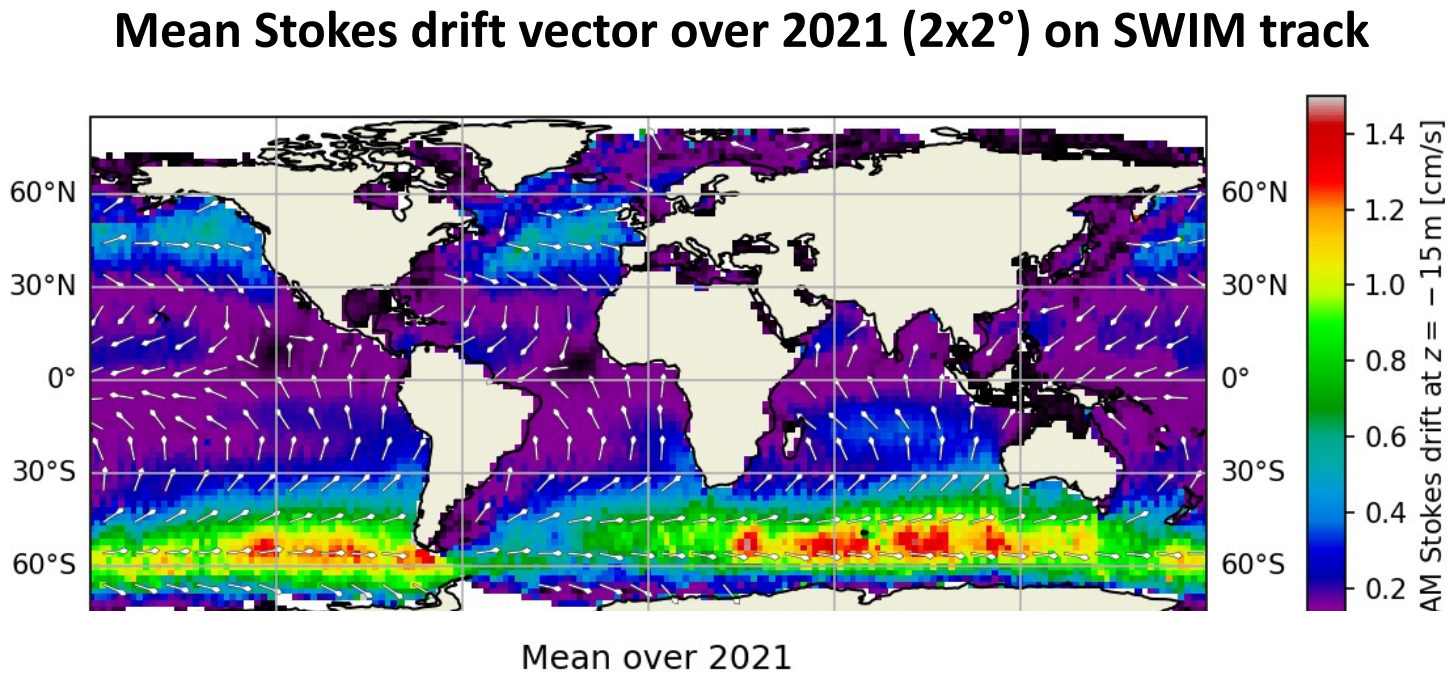


Performances - overview

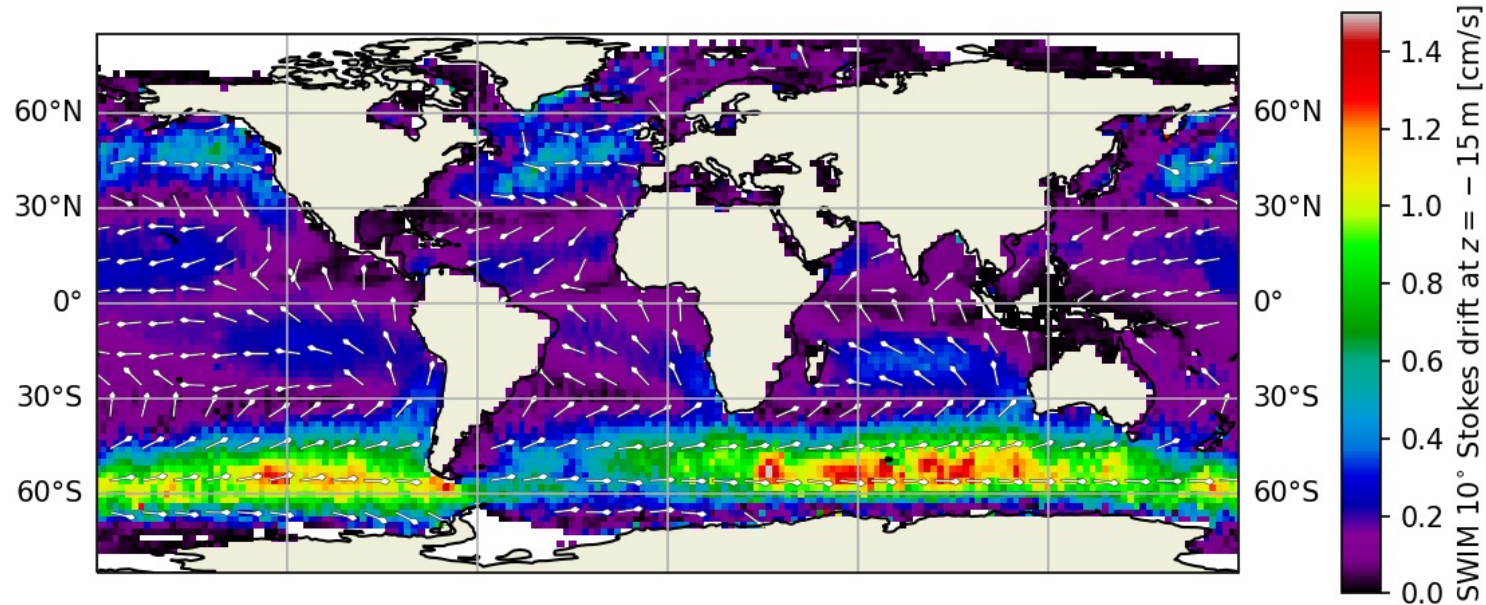
depth = -15 m



MODEL



SWIM

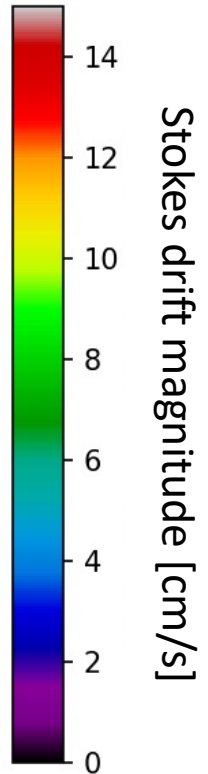
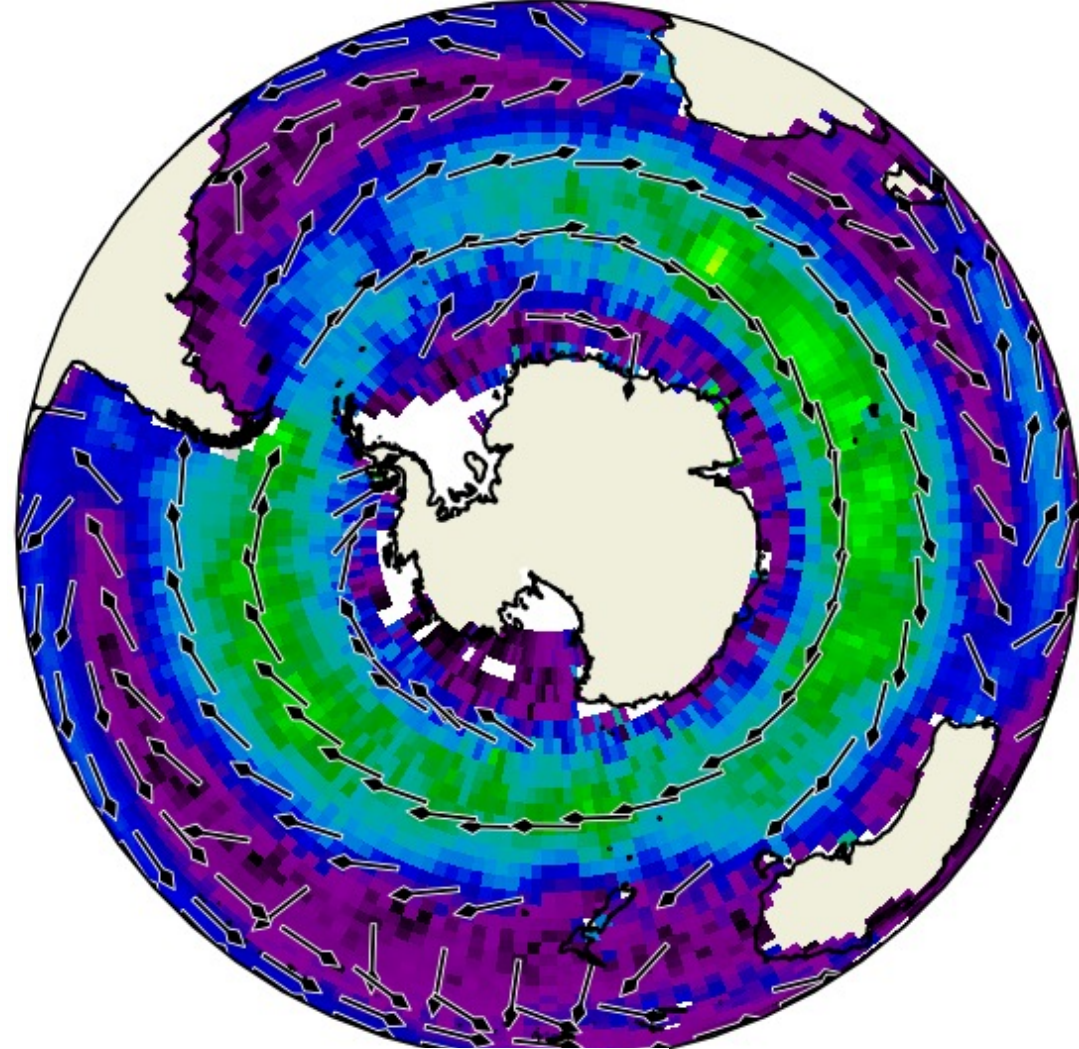
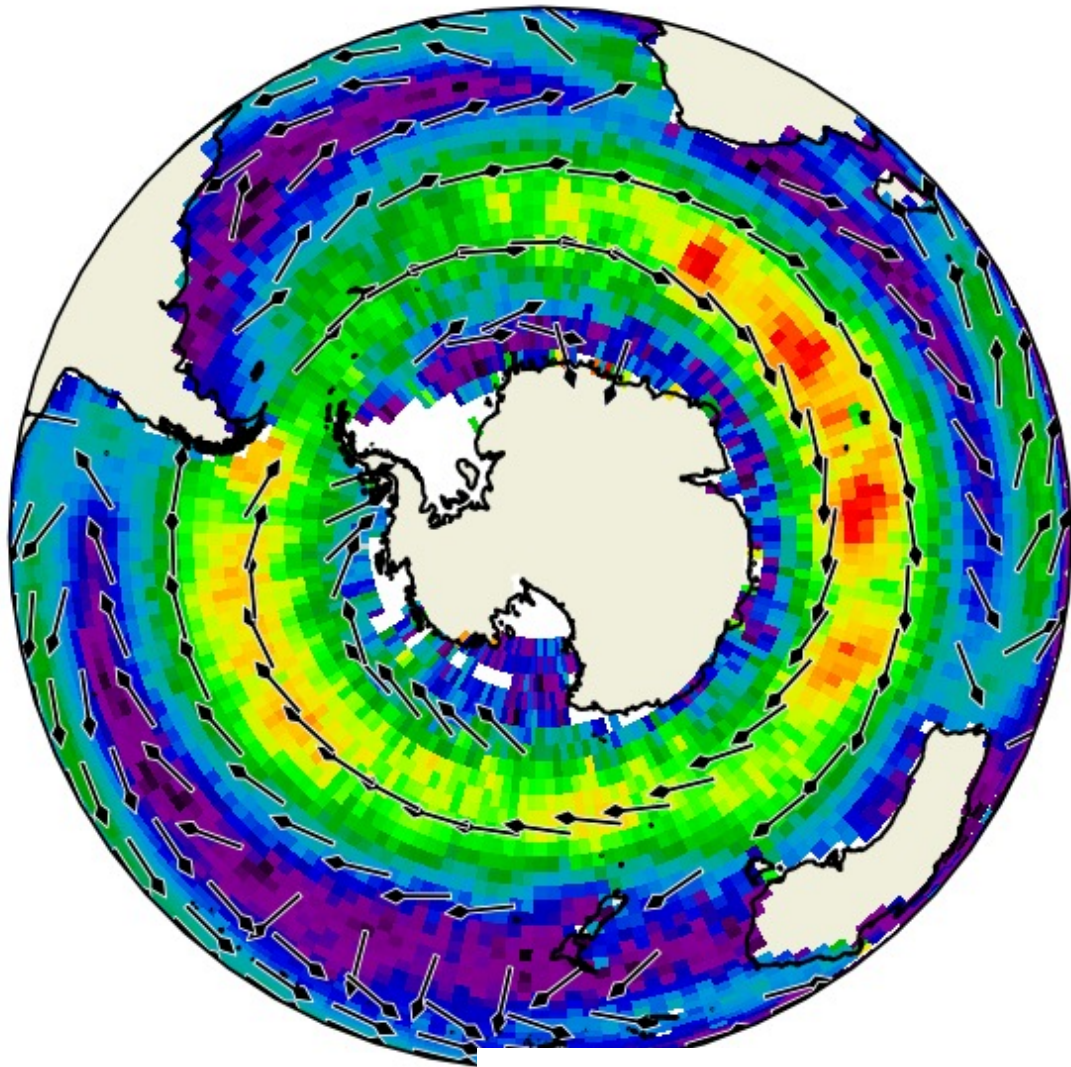


Performances – Southern Ocean

MODEL (WAM)

depth = 0 m

SWIM (10°)



Mean Stokes drift vector over 2021 (2x2°) on SWIM track

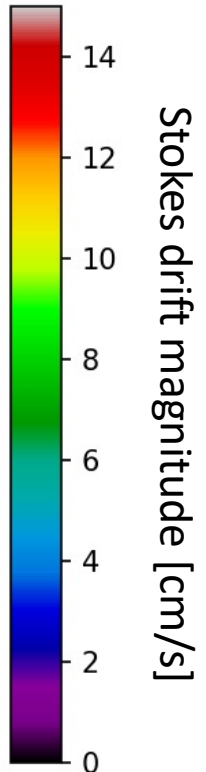
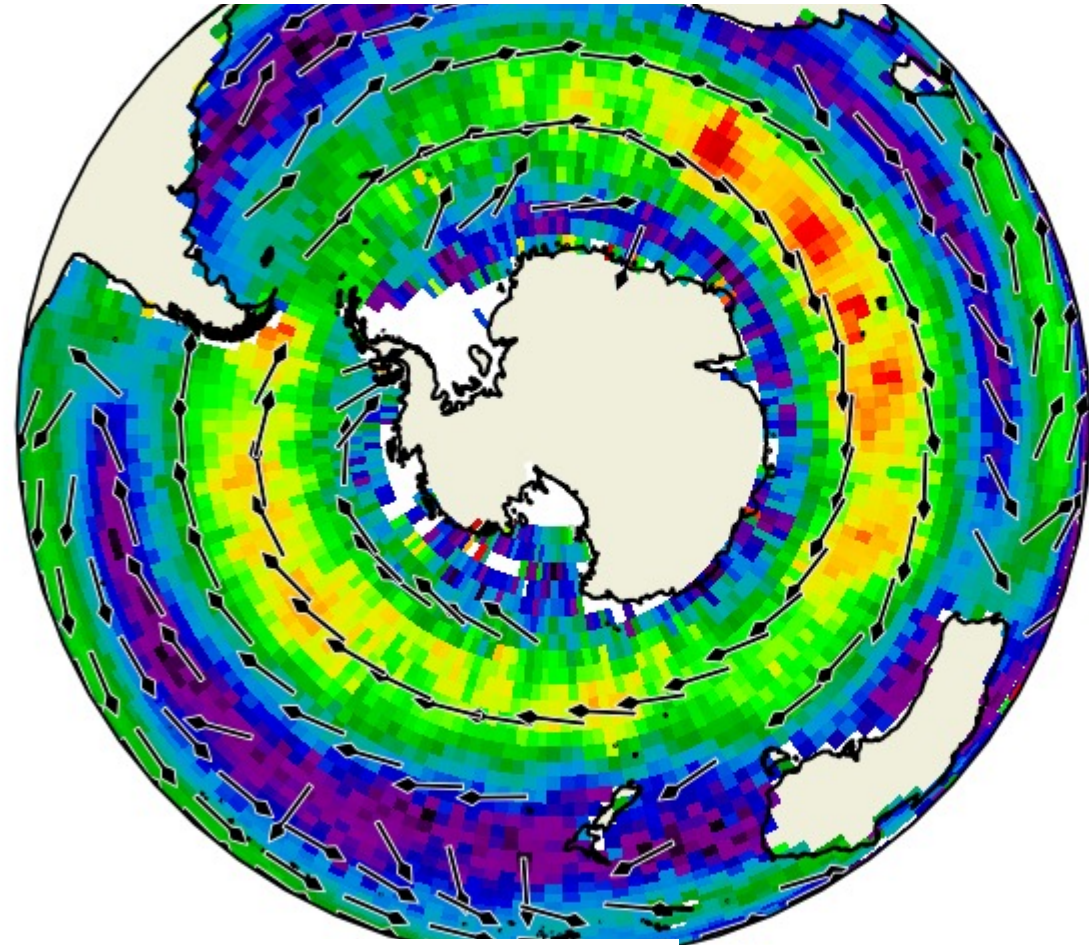
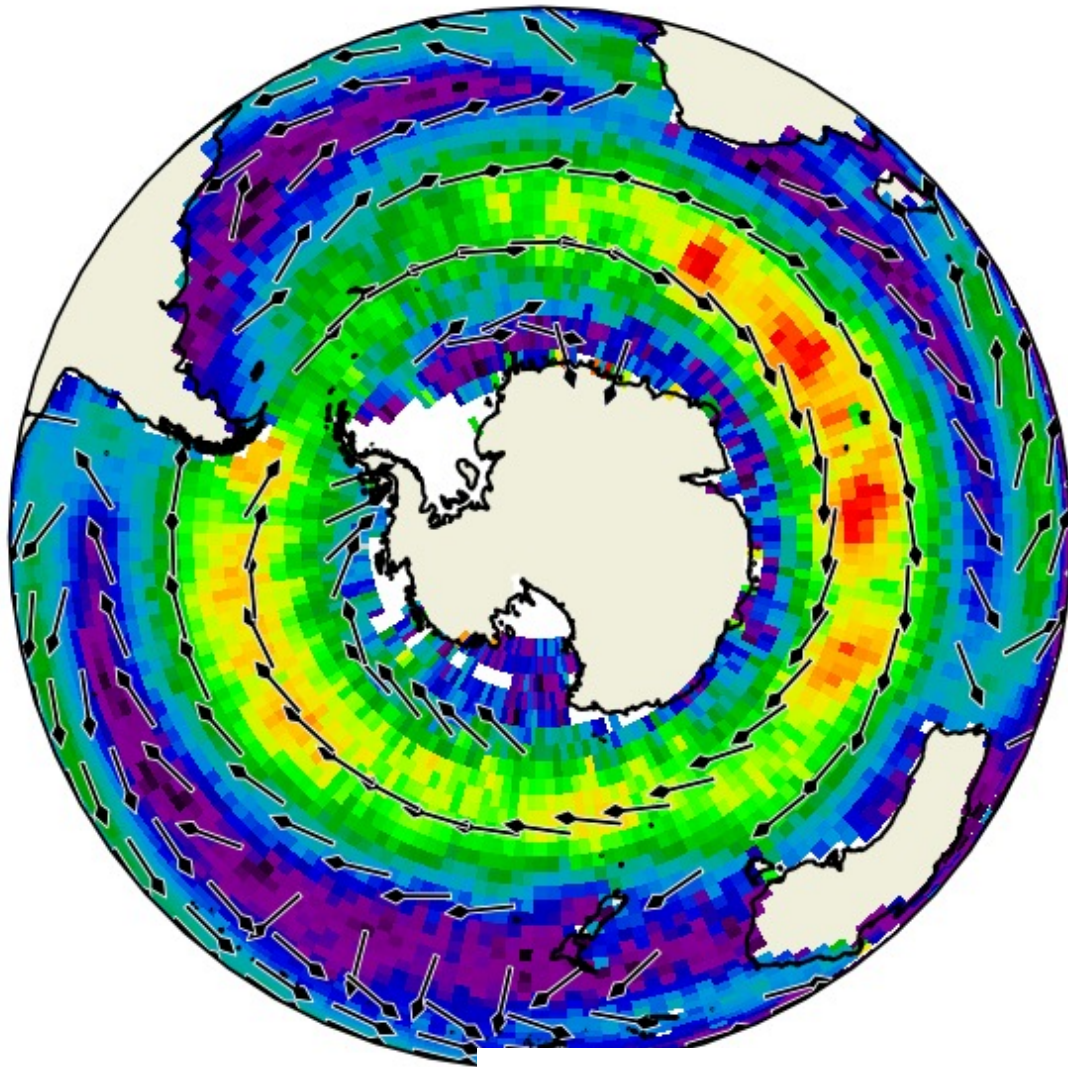
Performances

MODEL (WAM)

depth = 0 m

SWIM (10°)

+ Model independent theoretical wind-sea correction (Elfouhaily et al. 1997)



Mean Stokes drift vector over 2021 (2x2°) on SWIM track

Conclusions

- **Prototype algorithm and validation presented**
- **Encouraging results**
 - $Z = 0$ m : truncation biases (~ 20 to 40%), coherent with waves spectrum knowledge
 - $Z = -15$ m : very low bias ($\ll 1\%$)

-> *Demo products available on demand*

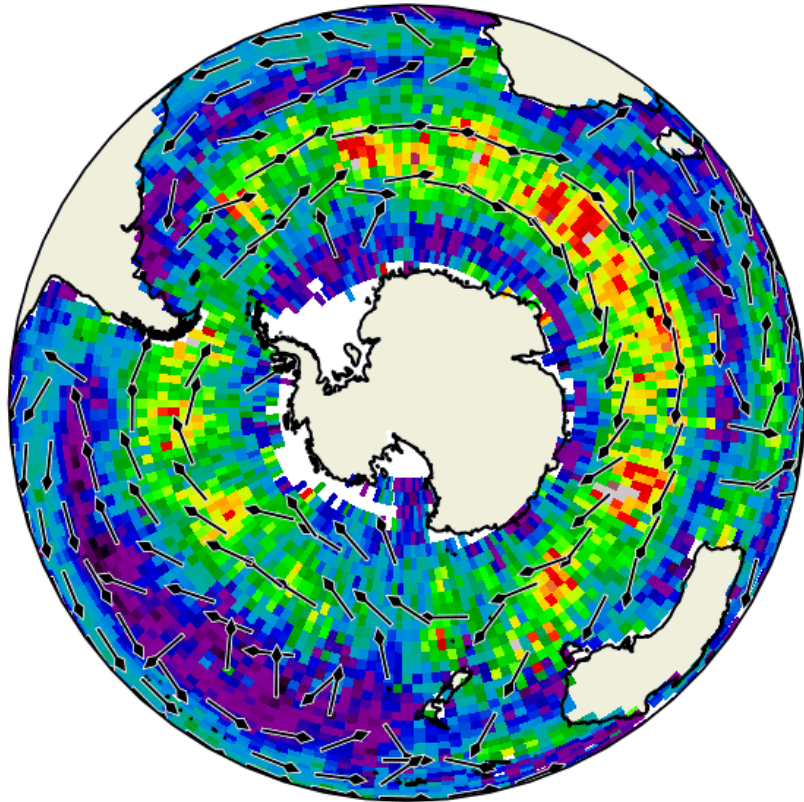
Stokes transport

- **Way forward**
 - Algorithm to correct for truncation and ambiguity
 - Young seas/multiple wave systems
- **Longer term perspectives**
 - Beams combination to improve performances
 - Using synergy with SCAT wind for full independence from any model
 - SWIM added value to be further characterized (~ 100 km variability)

Performances

MODEL (WAM)

January 2021

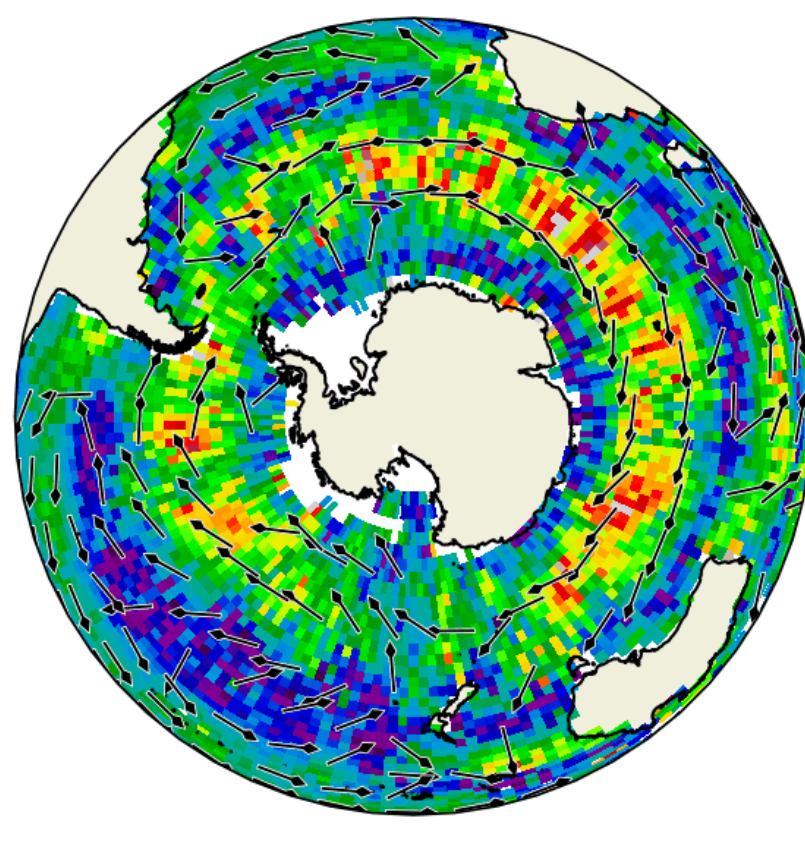


depth = 0 m

SWIM (10°)

+ Model independent theoretical wind-sea correction (Elfouhaily et al. 1997)

January 2021



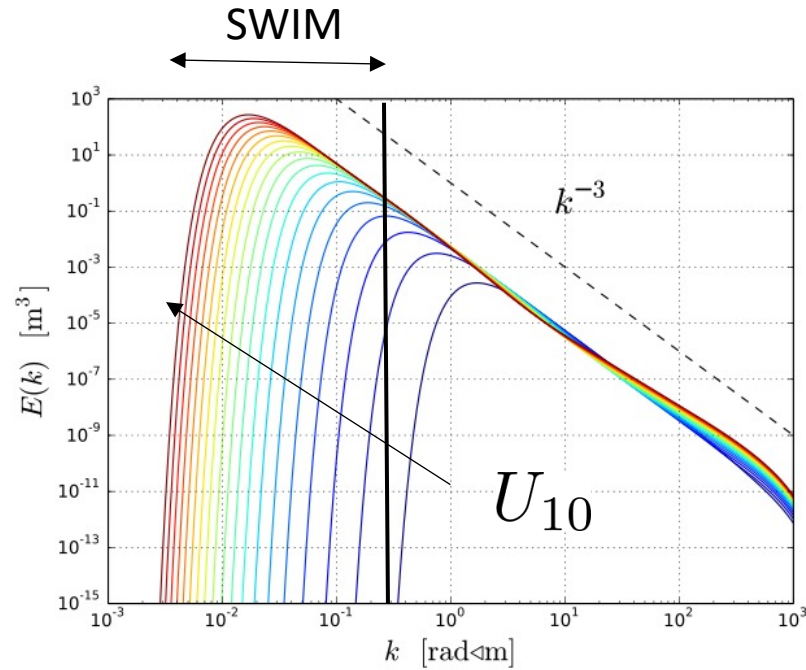
Mean Stokes drift vector over 2021 (2x2°) on SWIM track

Additional

Stokes theoretical correction

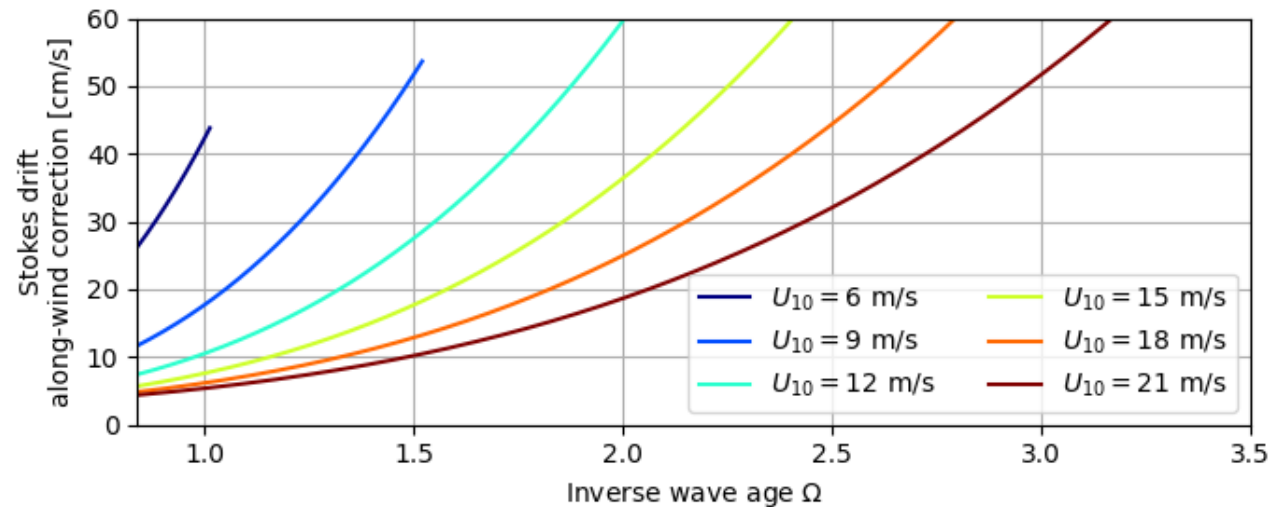
Elfouhaily et al. 1997

Adding in the wind direction the Stokes drift expected from an Elfouhaily spectrum for waves $0 < \lambda < 22\text{m}$



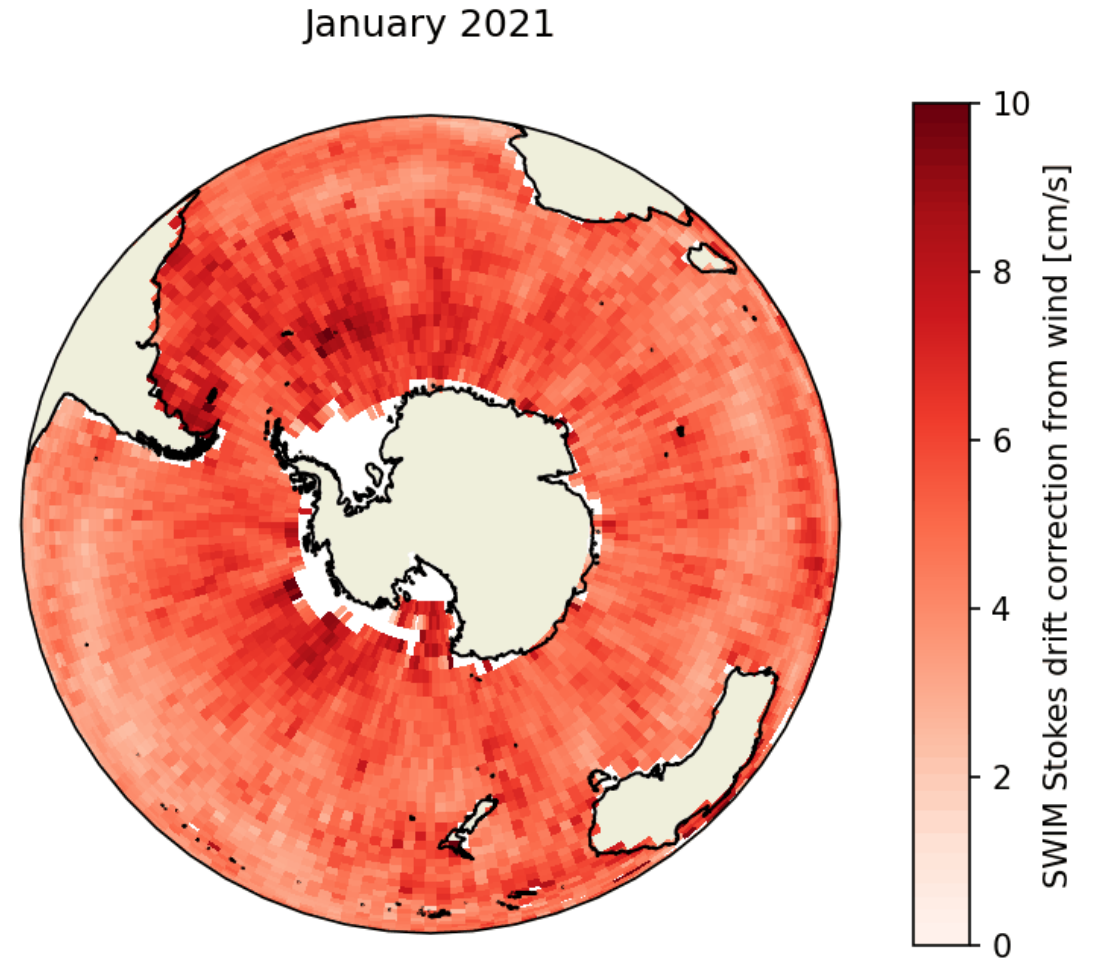
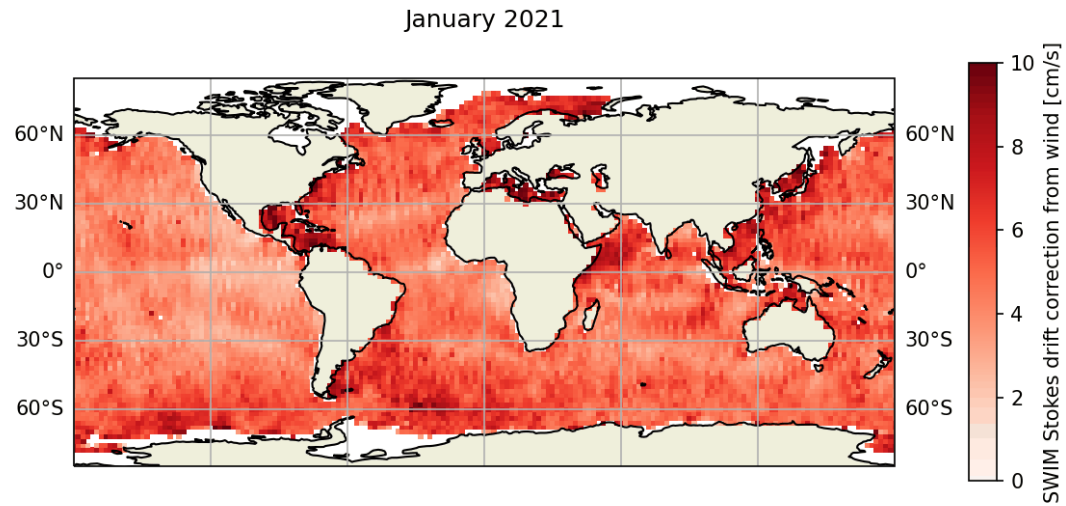
$$\Delta U_S(z=0) \simeq U_{S0} \sqrt{\Omega} \left[1 + \left(\frac{U_{10}}{\Omega U_0} \right)^{-2.5} \right]$$

$$U_{S0} = 3.7 \text{ cm/s} \quad U_0 = 15.3 \text{ m/s} \quad \Omega \simeq \frac{U_{10}}{c_p}$$



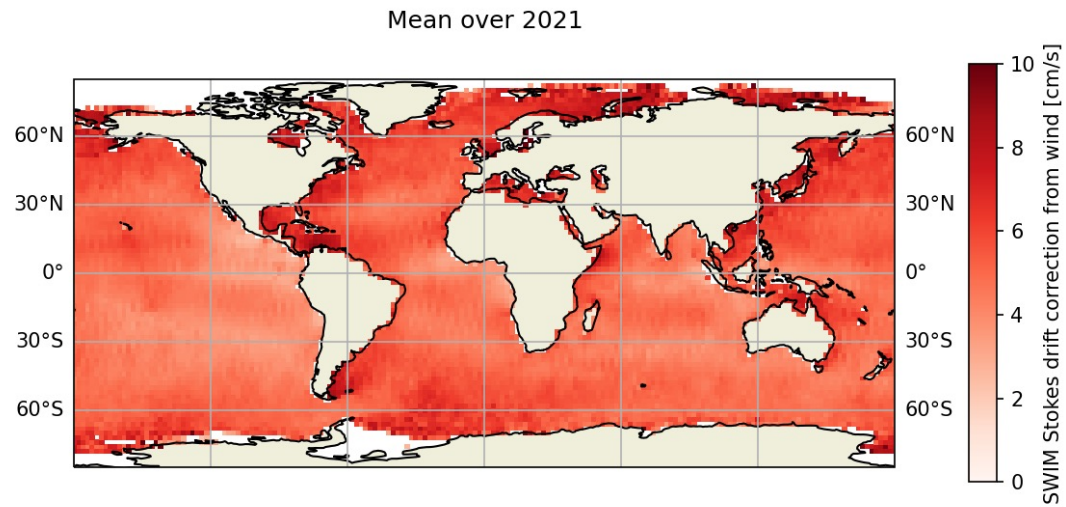
Stokes theoretical correction

U_{10} from ECMWF forecast
Peak from SWIM 10°

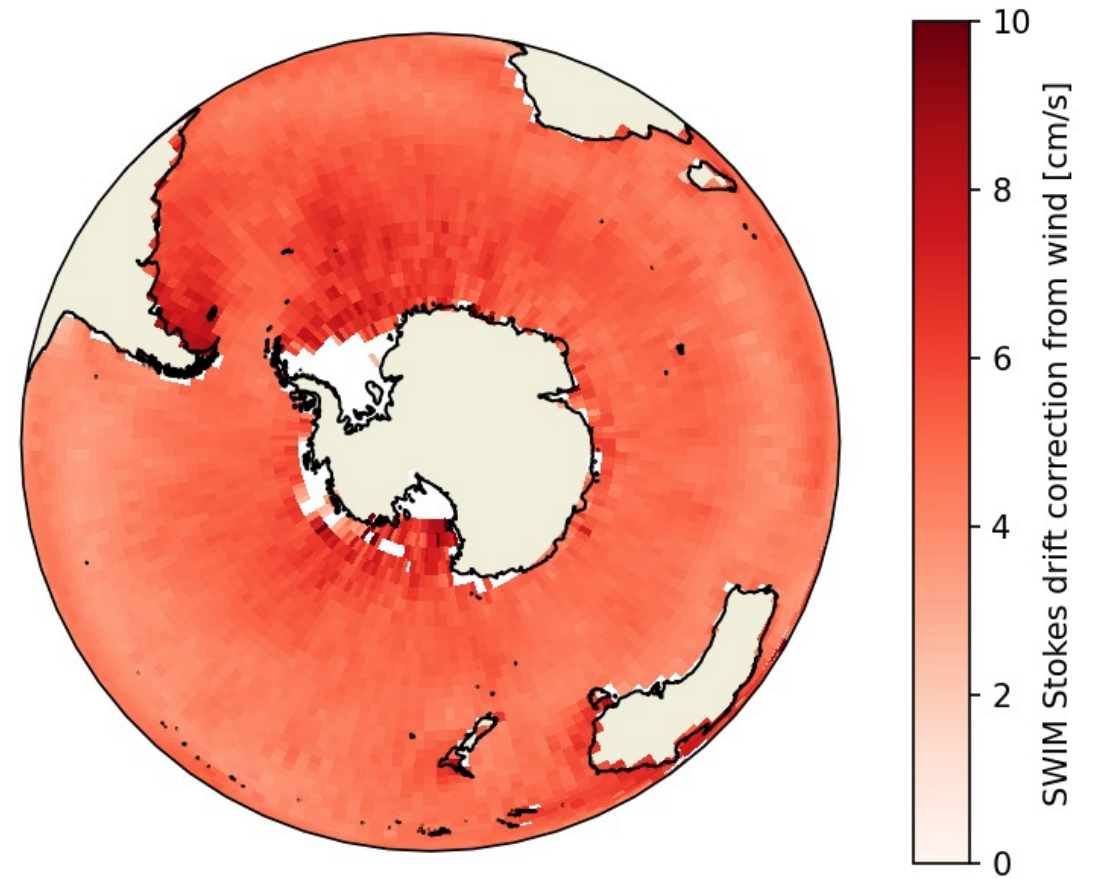


Stokes theoretical correction

U_{10} from ECMWF forecast
Peak from SWIM 10°



Mean over 2021

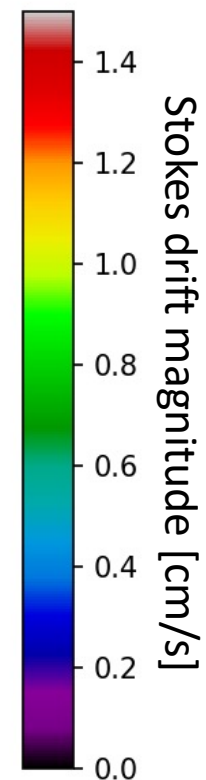
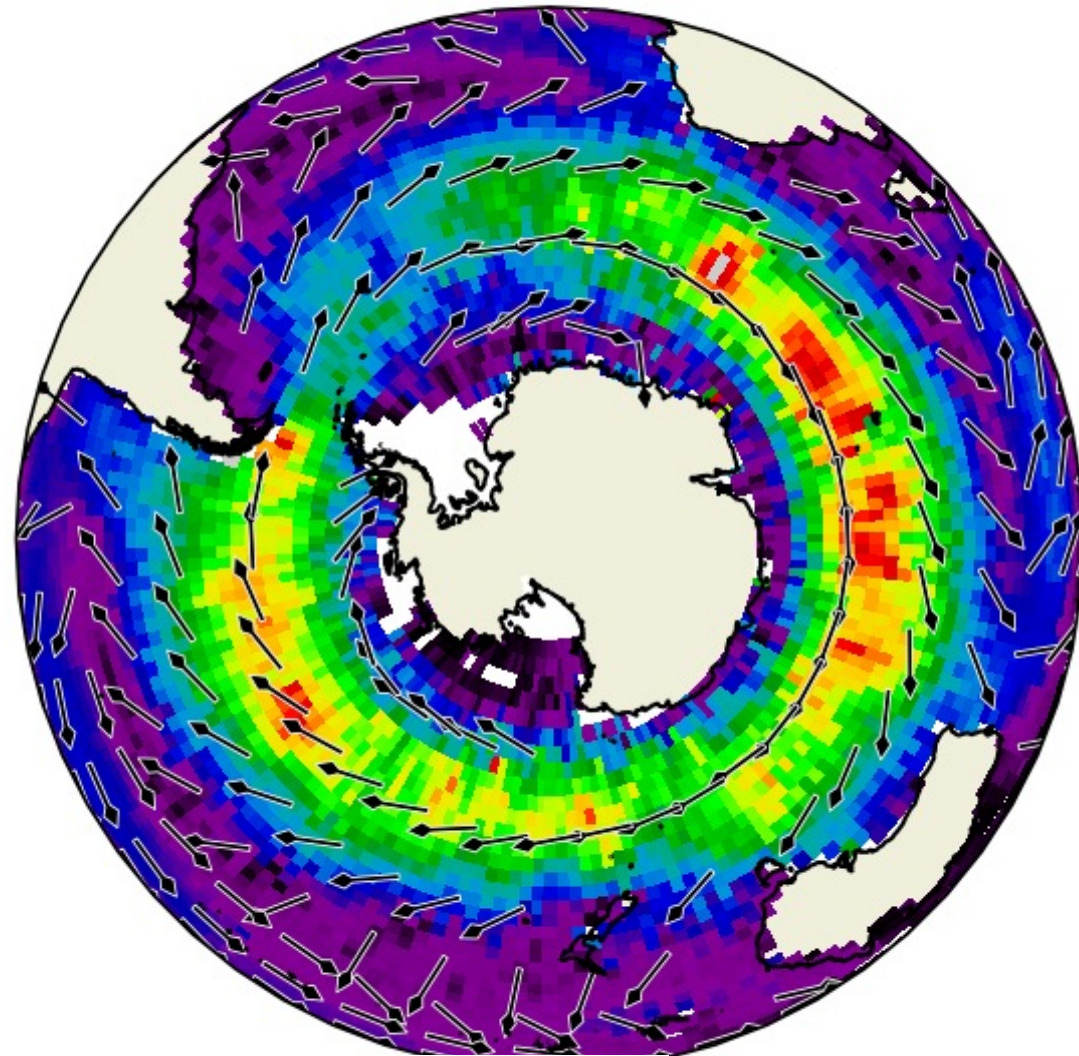
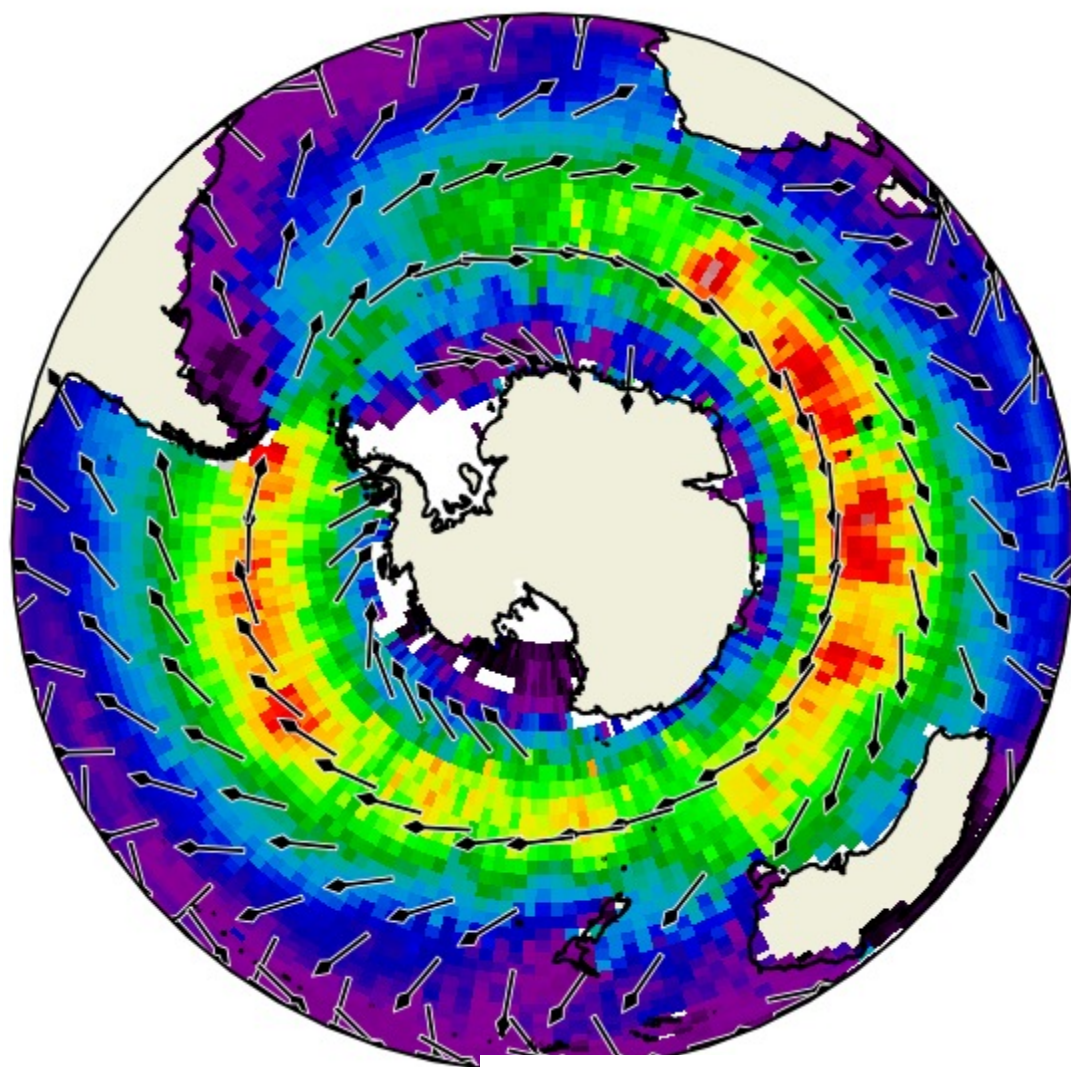


Performances

MODEL (WAM)

depth = -15 m

SWIM (10°)



Mean Stokes drift vector over 2021 (2x2°) on SWIM track

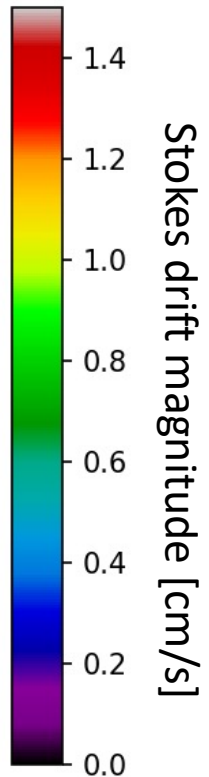
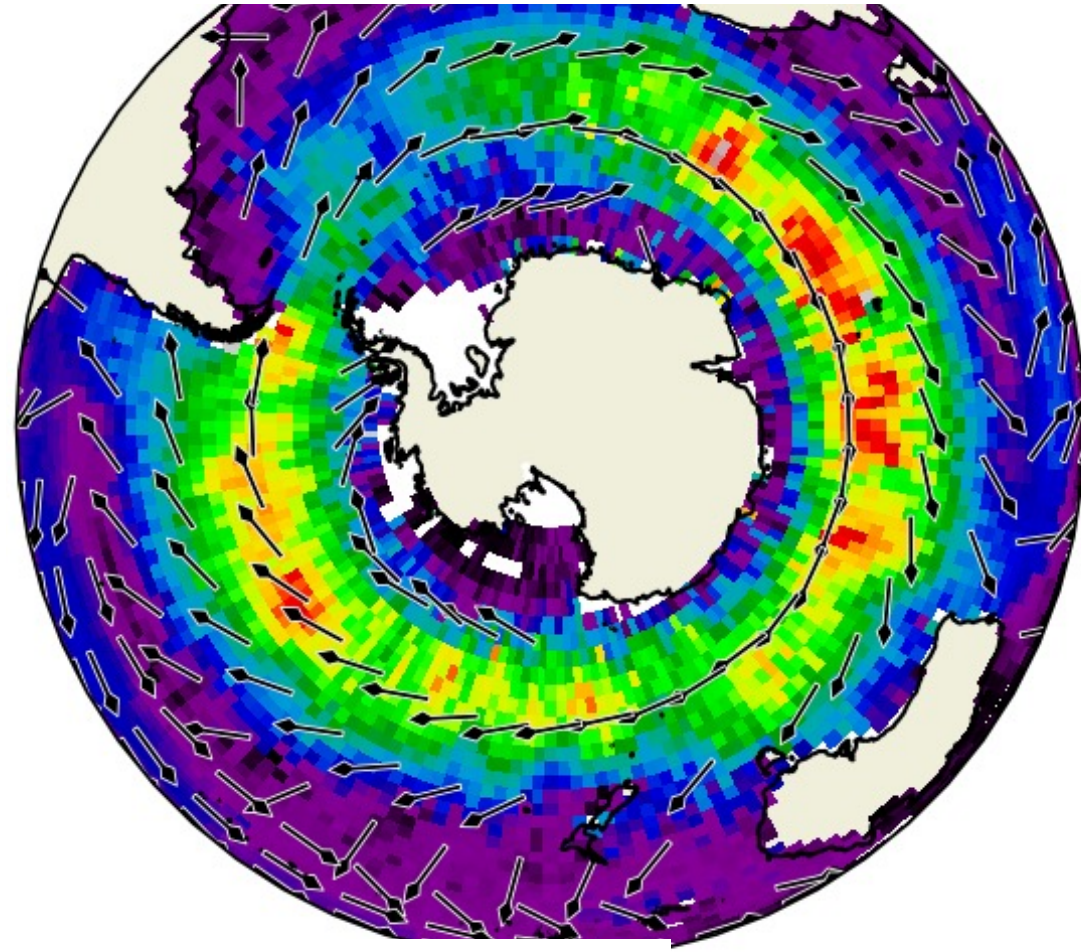
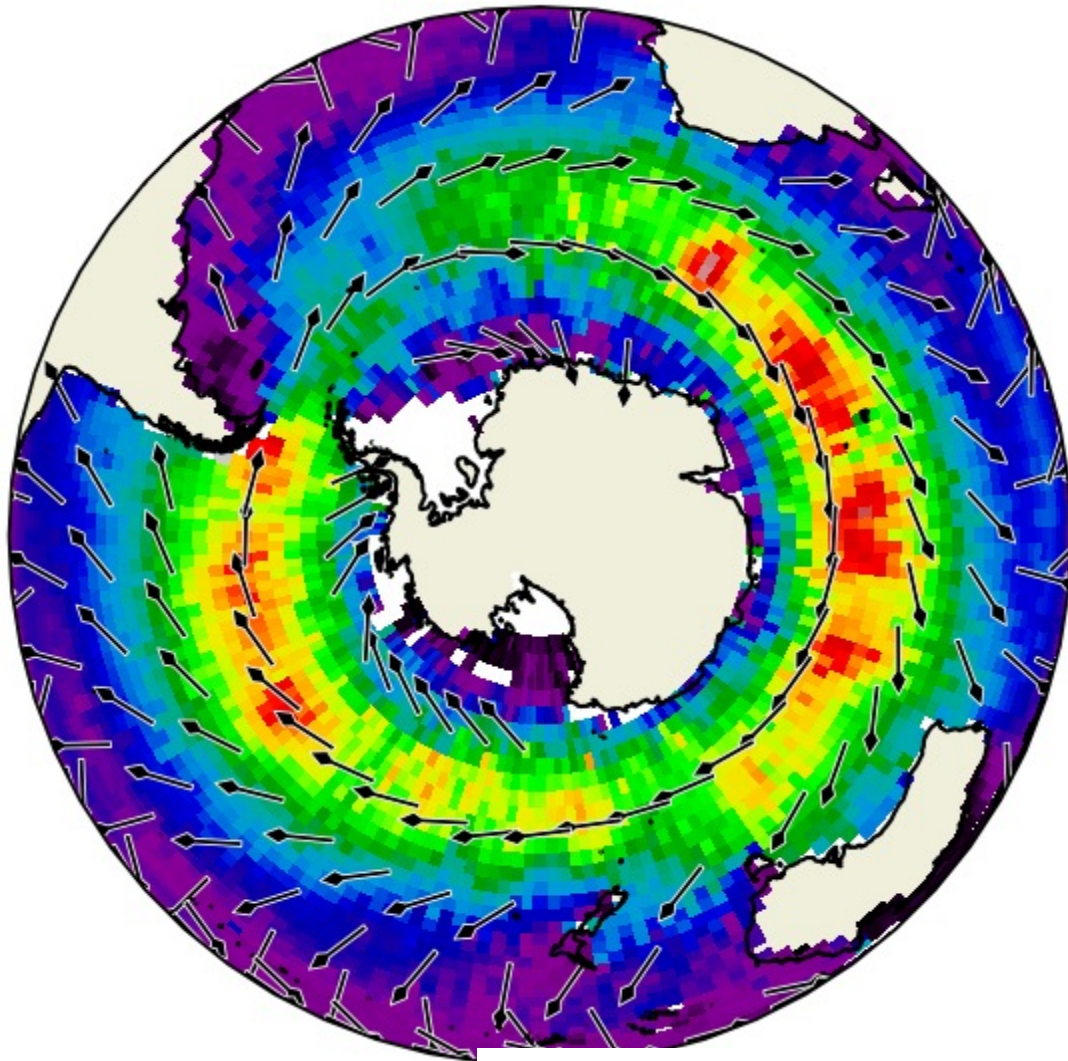
Performances

MODEL (WAM)

depth = -15 m

SWIM (10°)

+ Theoretical wind-sea correction
(Elfouhaily et al. 1997)

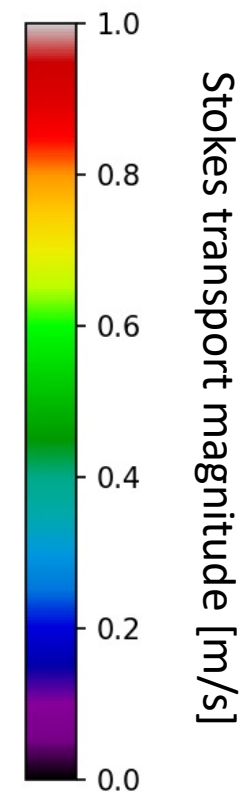
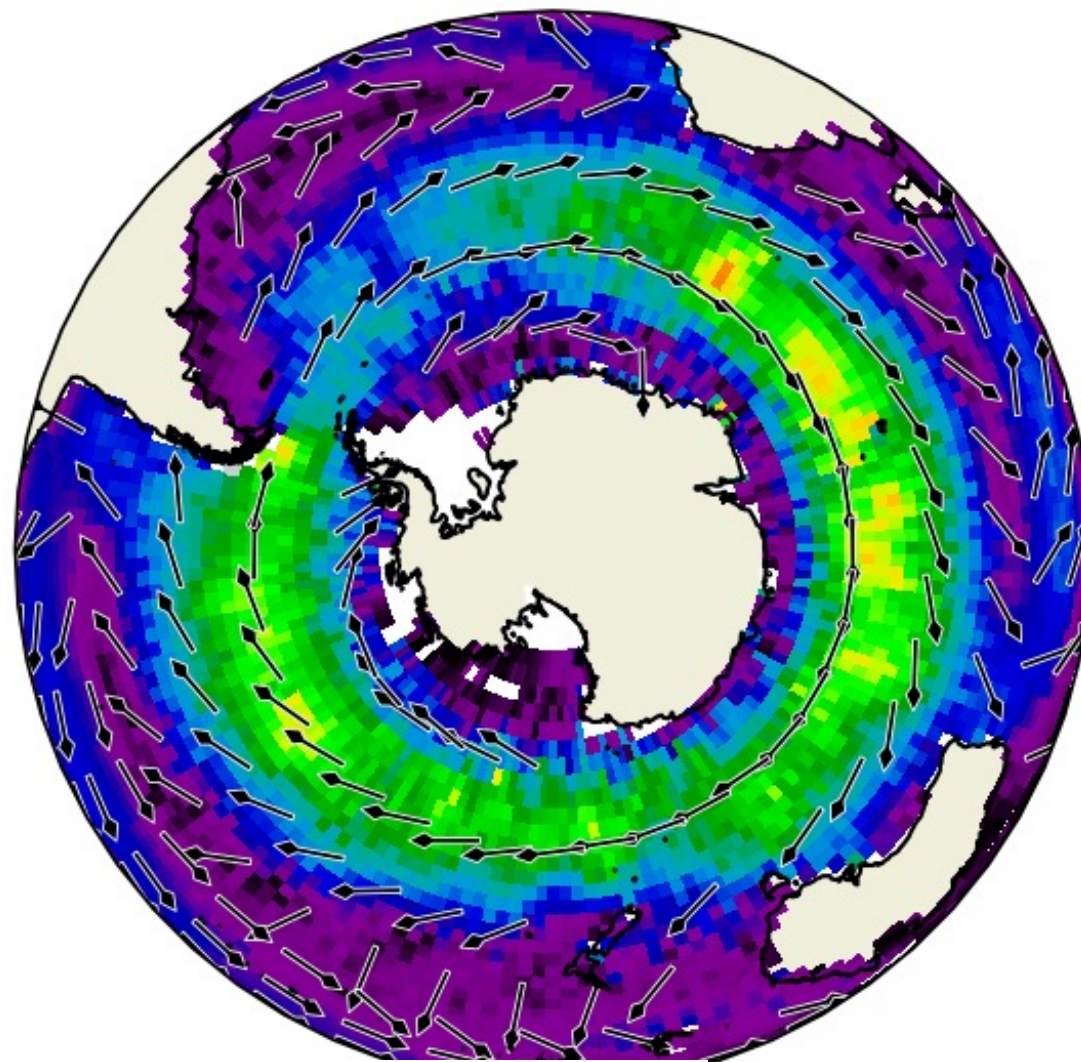
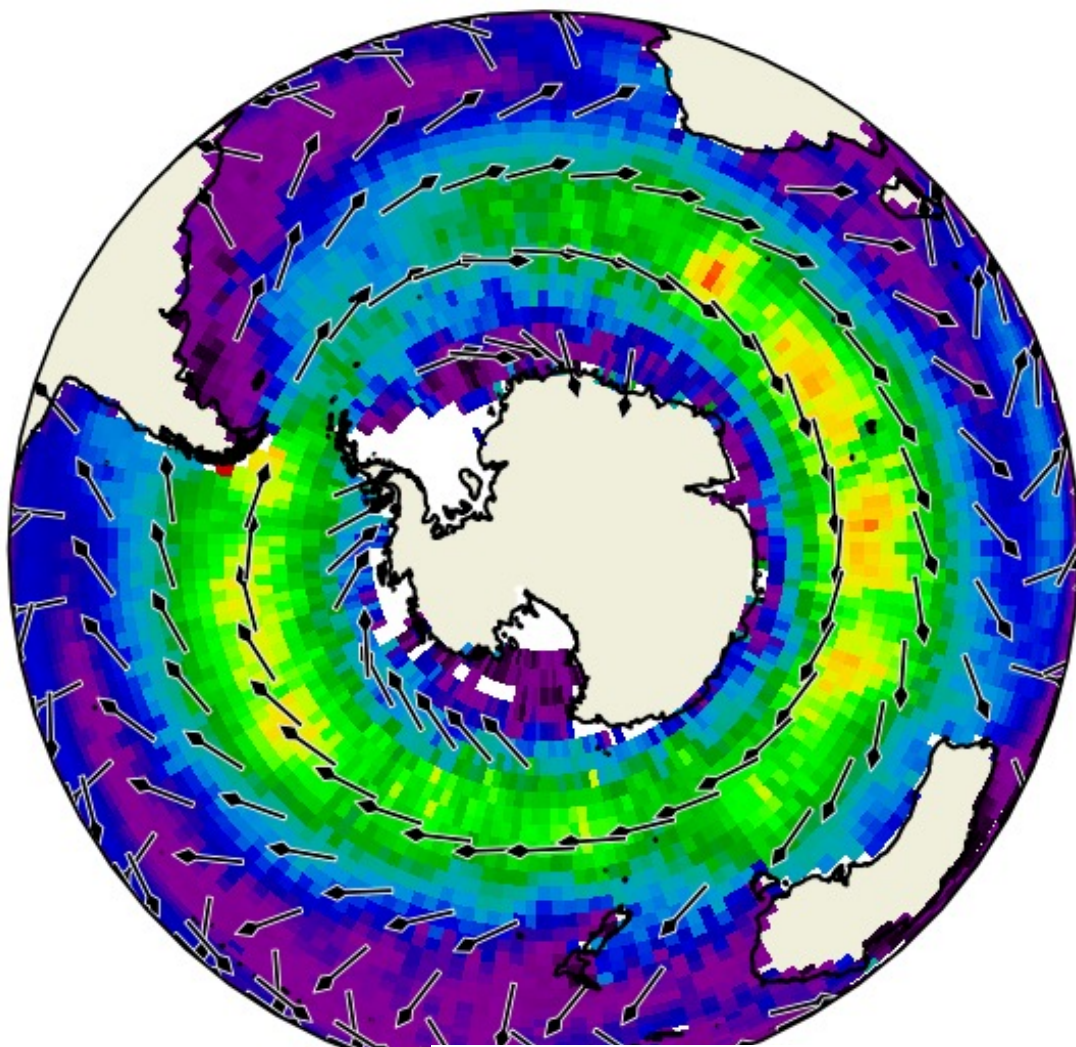


Mean Stokes drift vector over 2021 (2x2°) on SWIM track

Performances

MODEL (WAM)

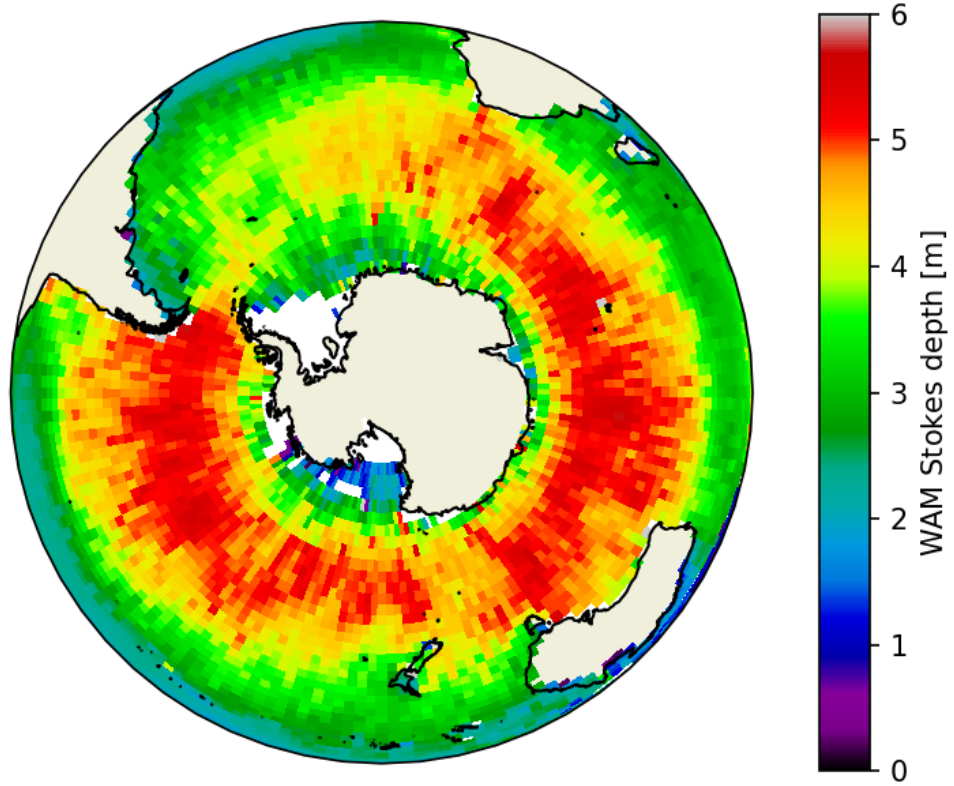
SWIM (10°)



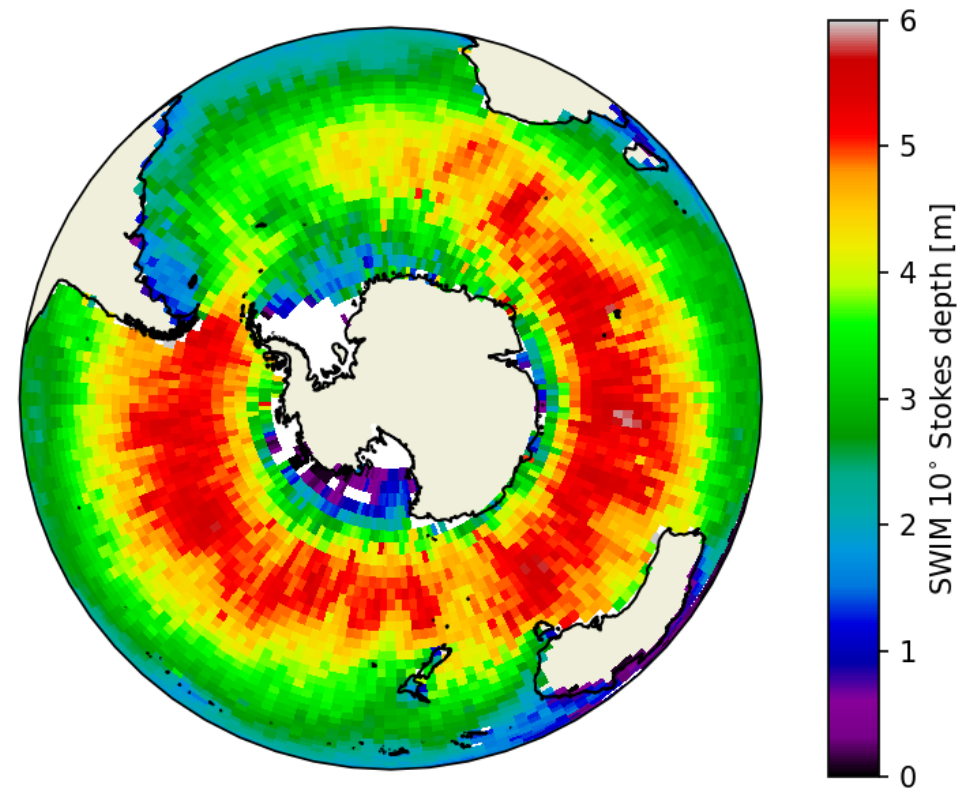
Mean Stokes transport vector over 2021 (2x2°) on SWIM track

Performances

Mean over 2021

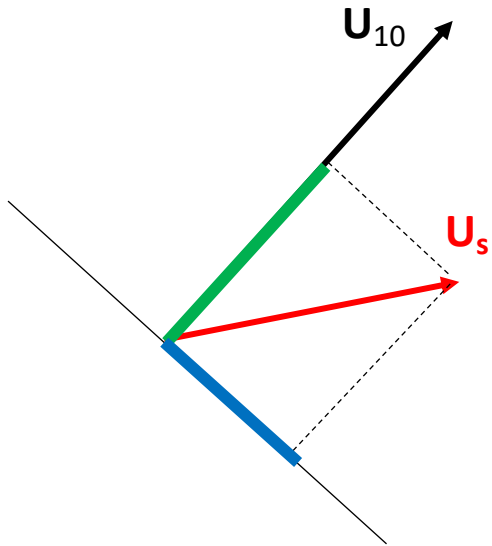


Mean over 2021



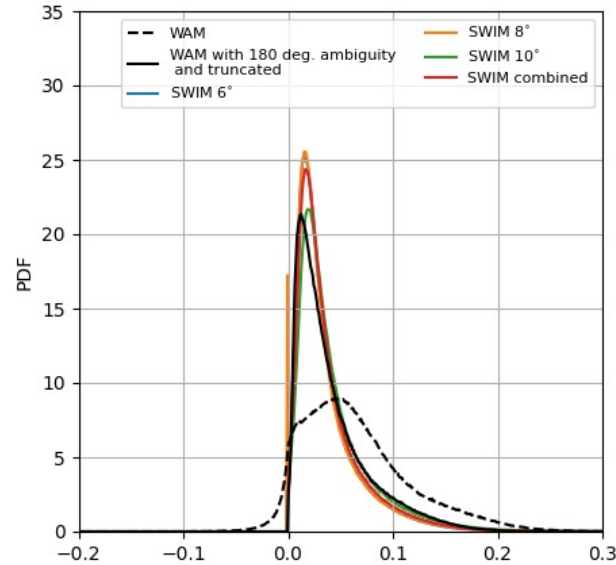
Performances - disambiguation

Hypothesis : Stokes drift
direction \sim wind direction

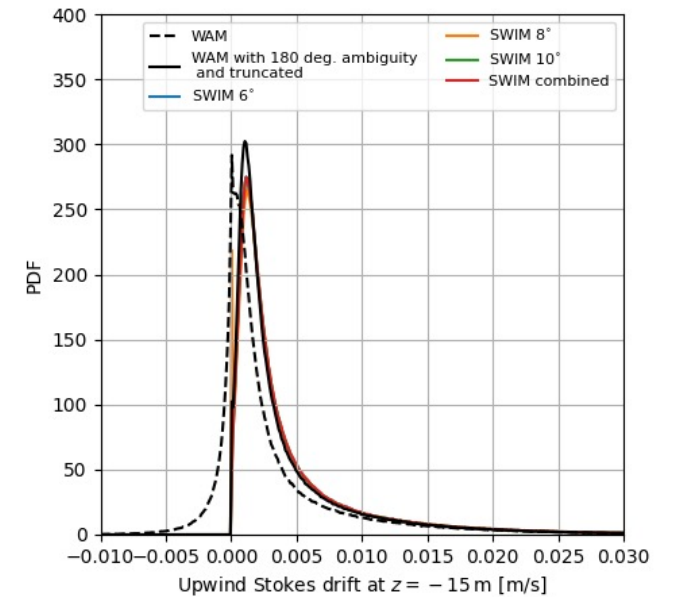


Along-wind
Stokes drift

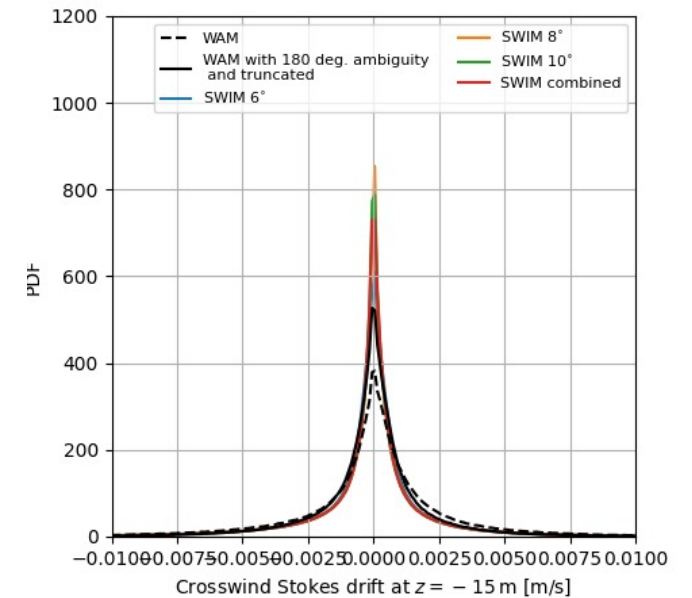
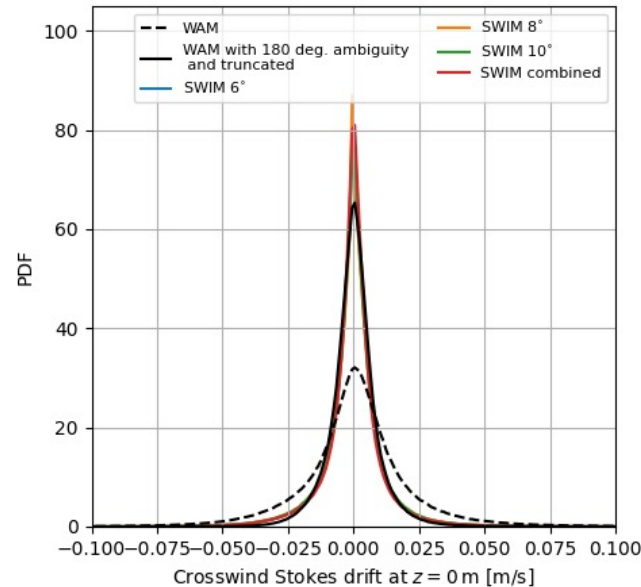
$z = 0 \text{ m}$



$z = -15 \text{ m}$

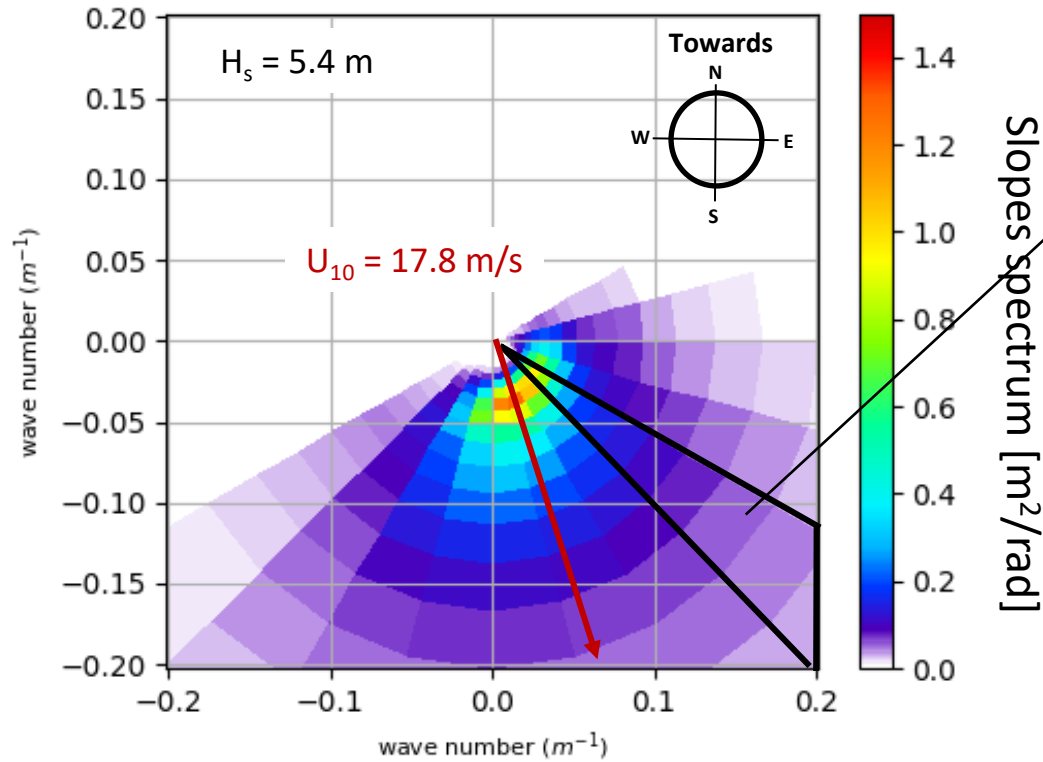


Crosswind
Stokes drift



Stokes drift estimation from SWIM

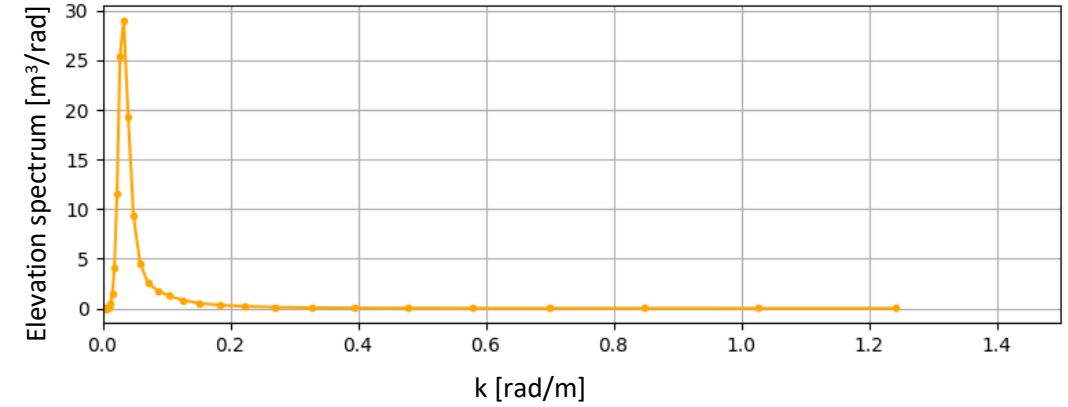
MODEL (WAM)



Kenyon 1969

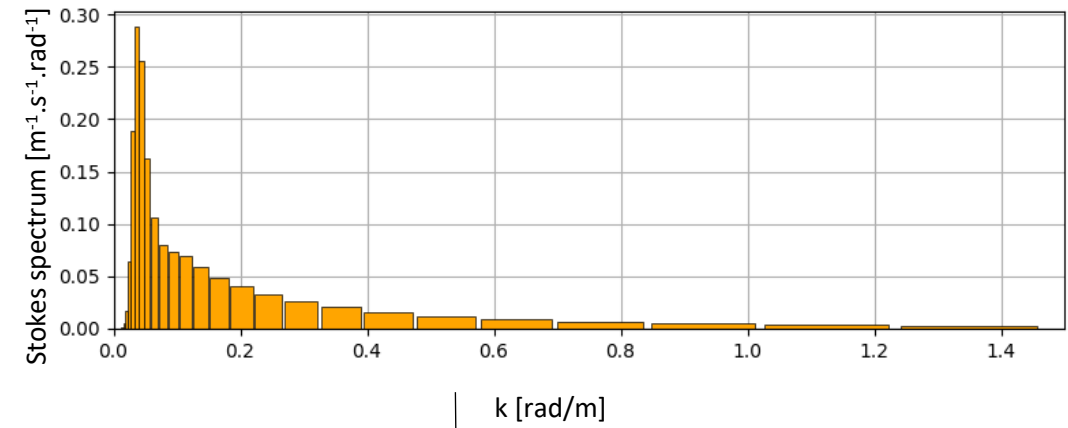
$$\int \dots dk$$

3.7 cm/s



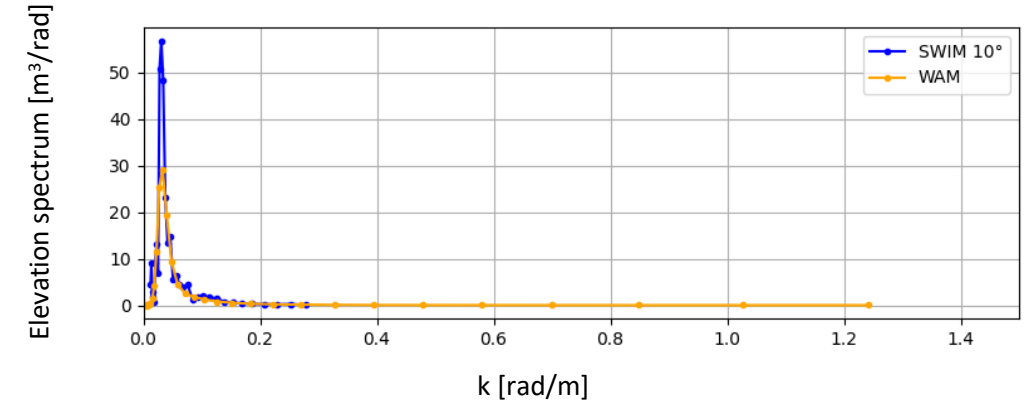
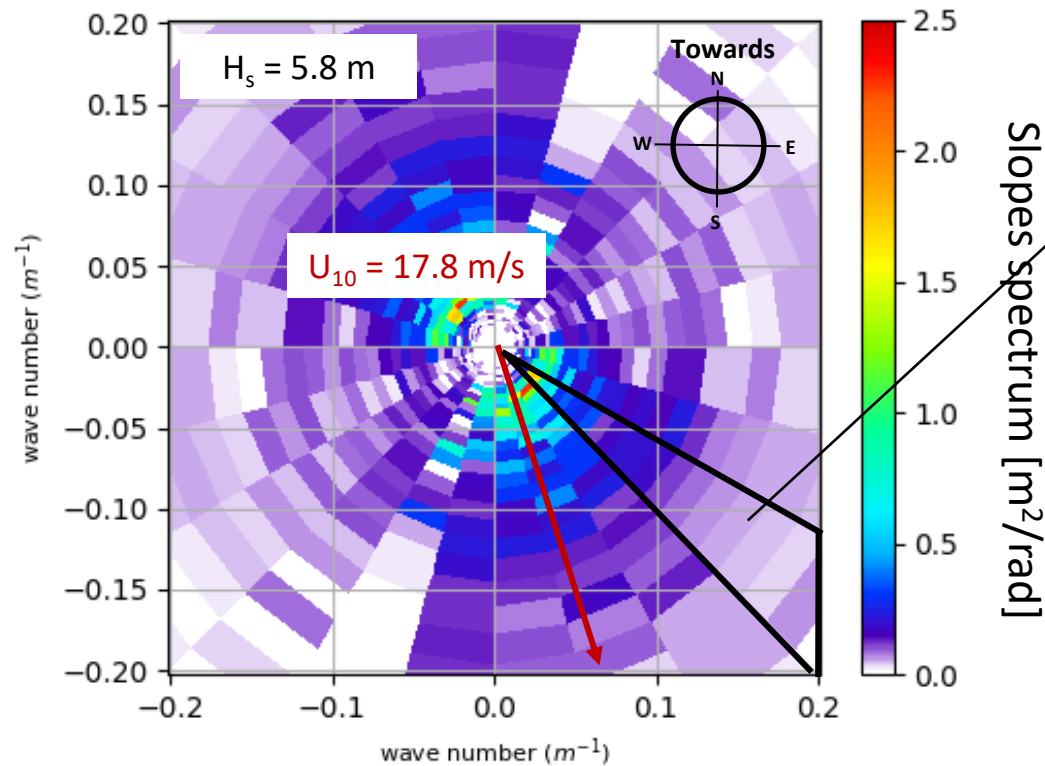
Kenyon 1969

$$\times 2\sqrt{gk}^{1.5}$$

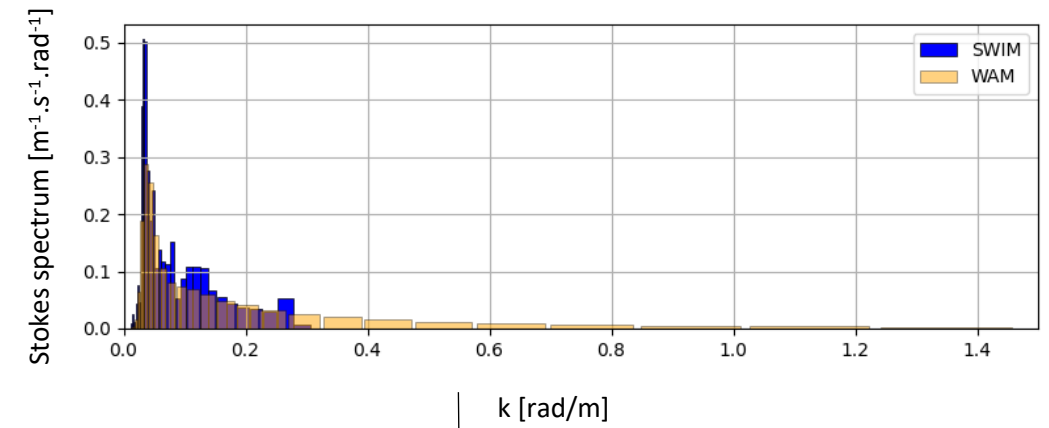


Introduction - Stokes drift estimation

SWIM RAW (10° beam)



$$\times 2\sqrt{g}k^{1.5}$$

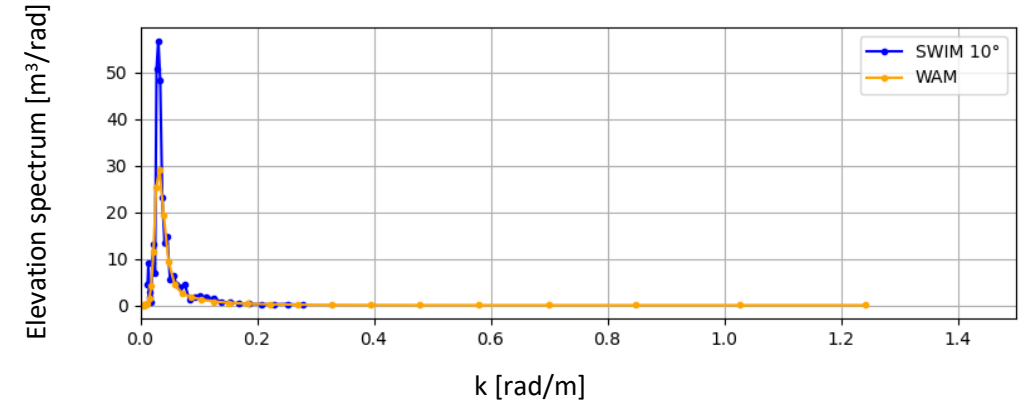
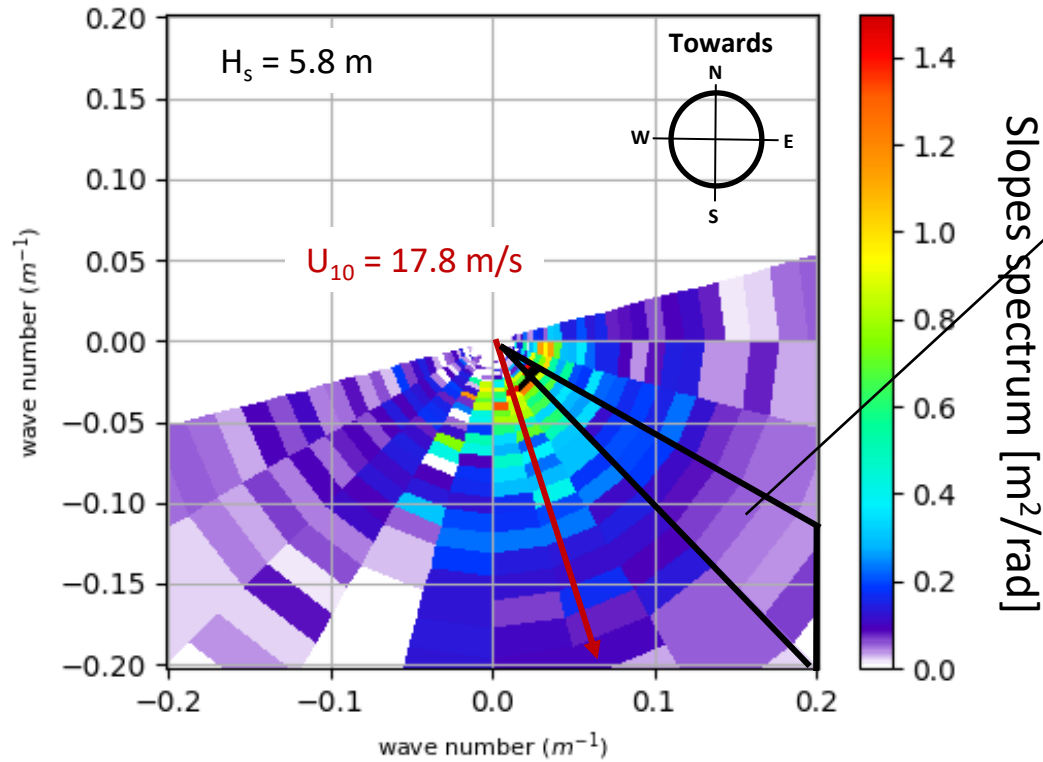


$$\int \dots dk$$

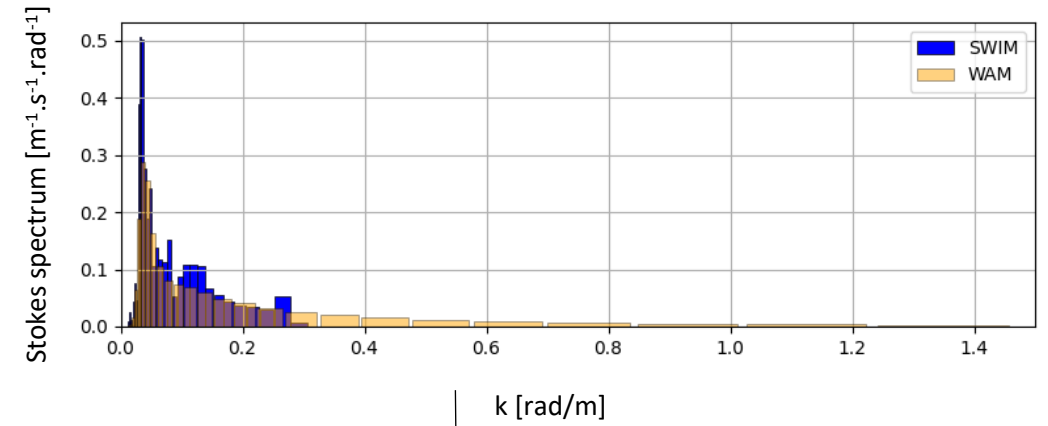
2.9 cm/s

Introduction - Stokes drift estimation

SWIM (10°)



$$\times 2\sqrt{g}k^{1.5}$$

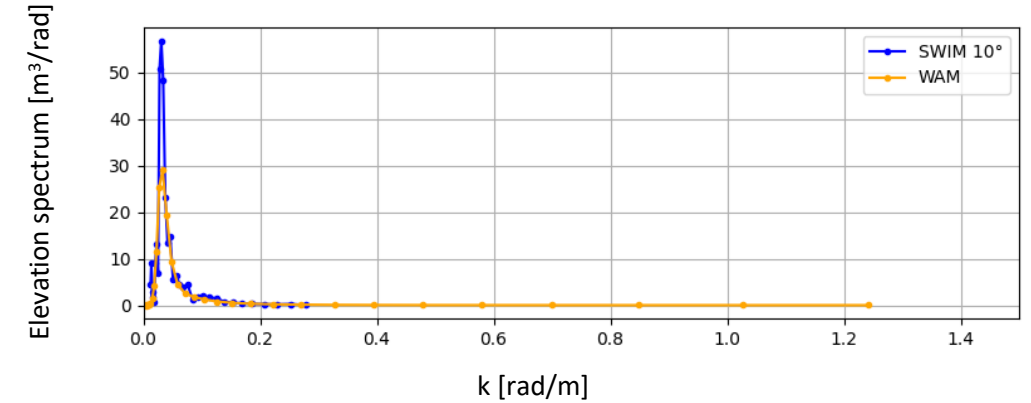
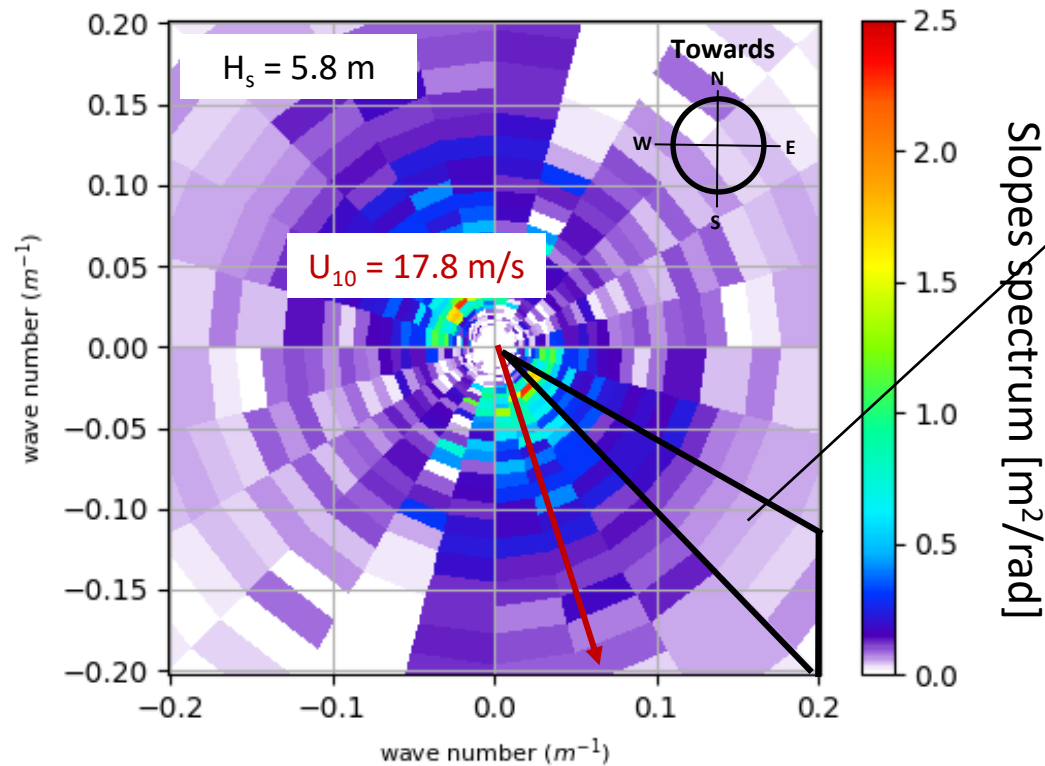


$$\int \dots dk$$

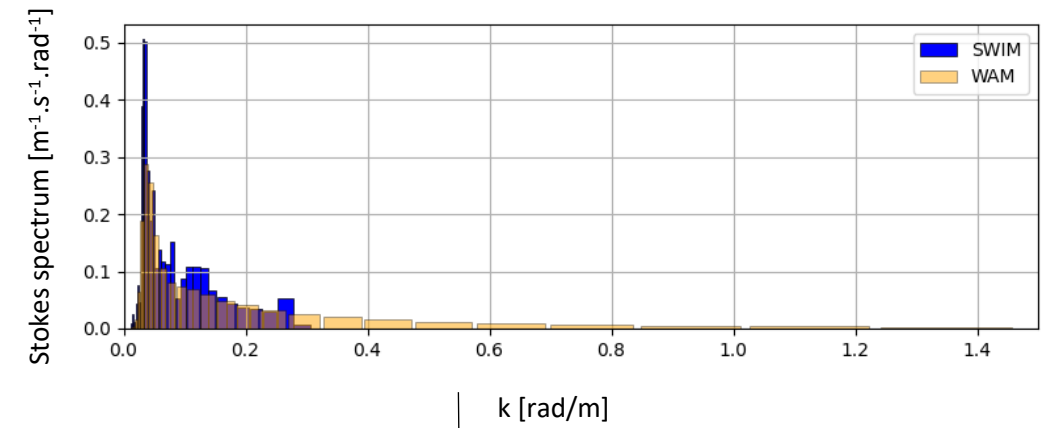
2.9 cm/s

Introduction - Stokes drift estimation

SWIM RAW (10° beam)



$$\times 2\sqrt{gk}^{1.5}$$

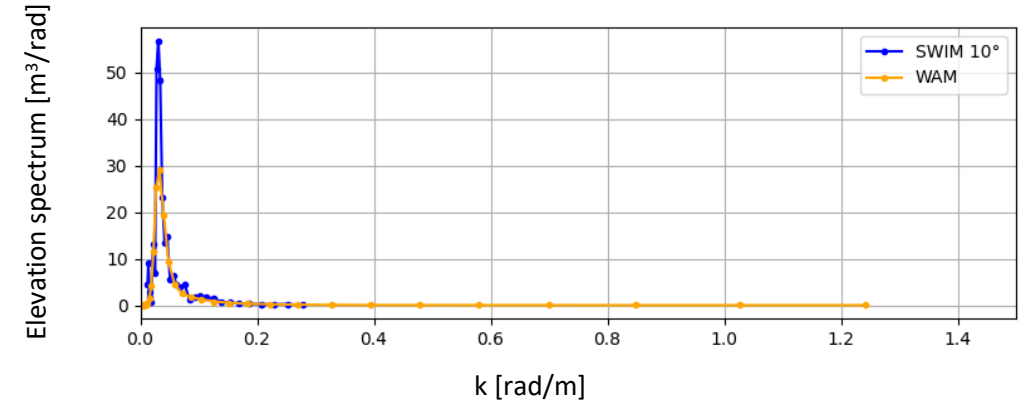
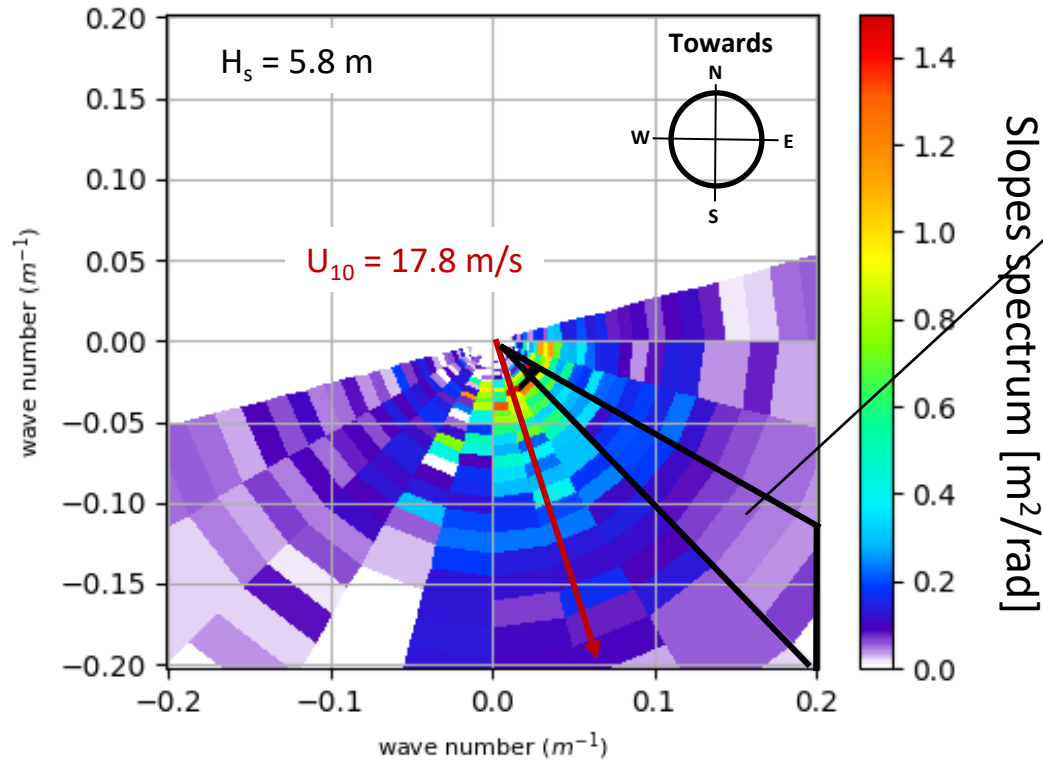


$$\int \dots dk$$

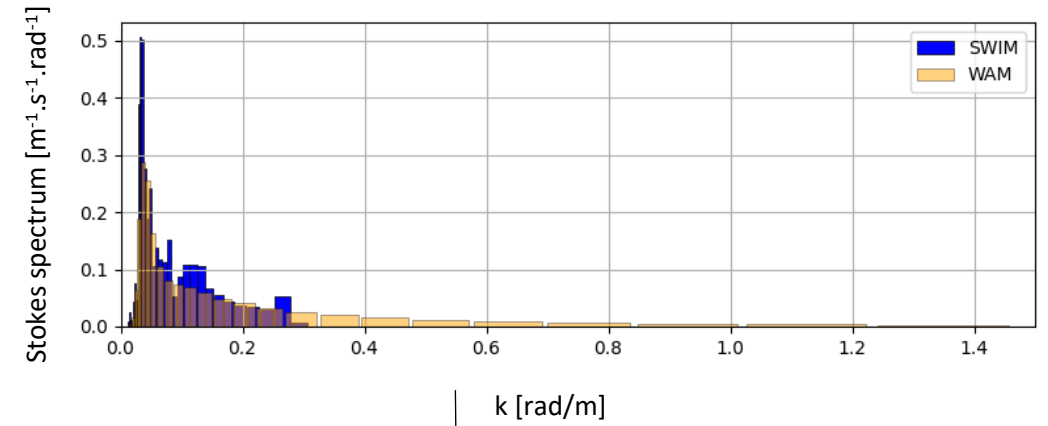
2.9 cm/s

Introduction - Stokes drift estimation

SWIM (10°)



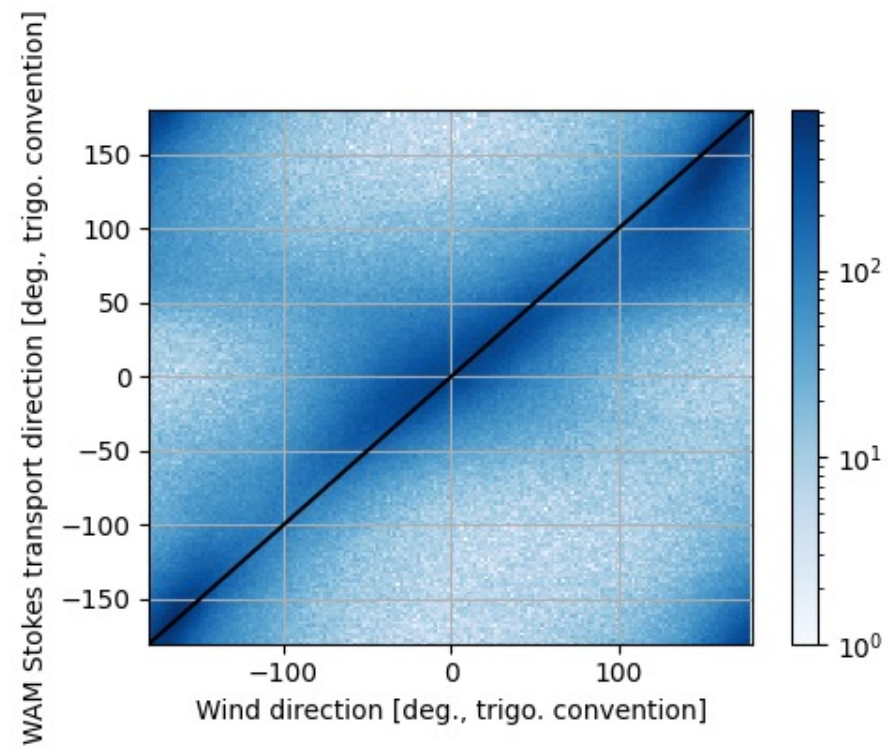
$$\times 2\sqrt{g}k^{1.5}$$



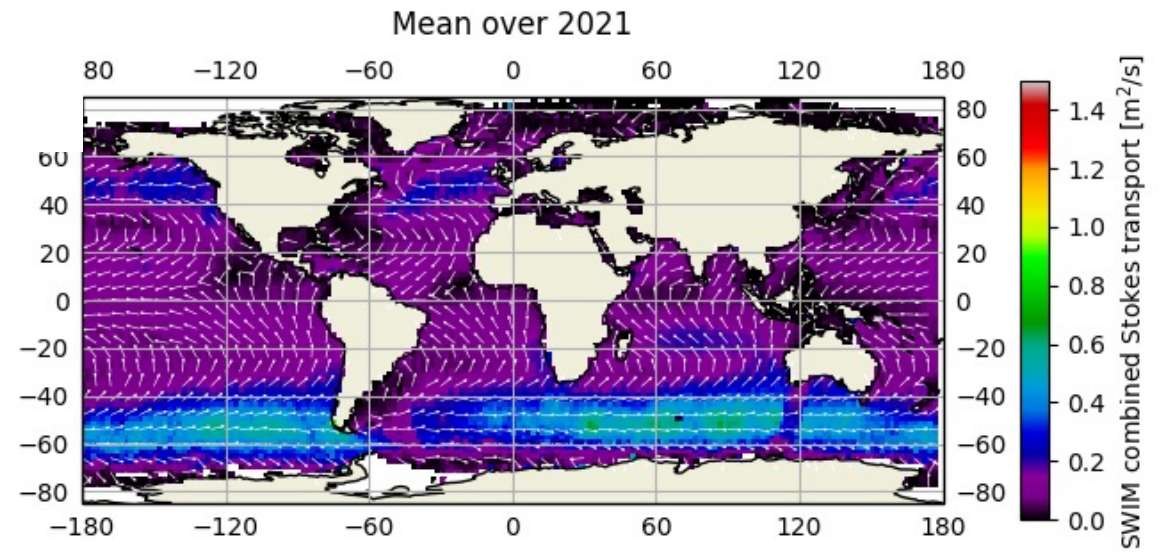
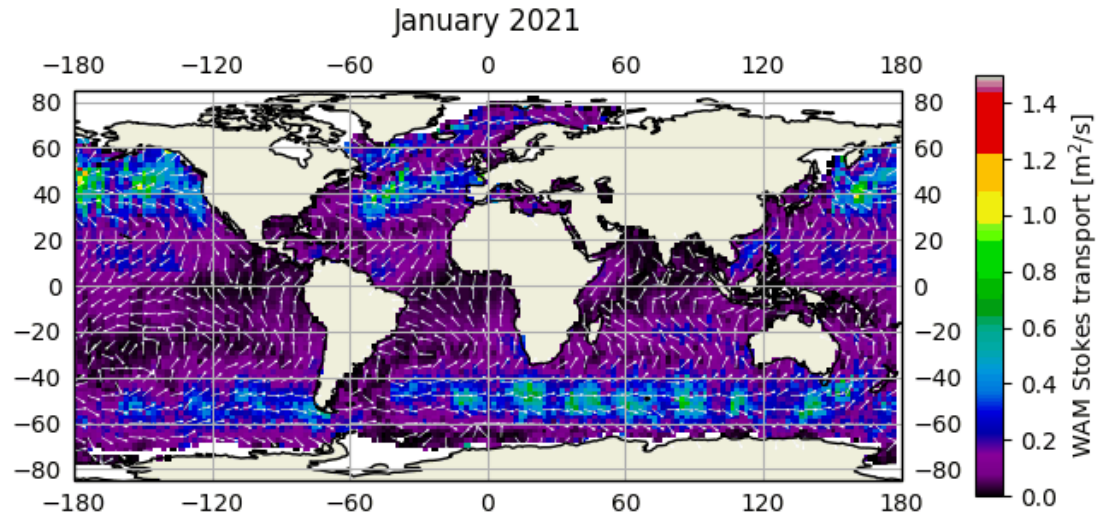
$$\int \dots dk$$

2.9 cm/s

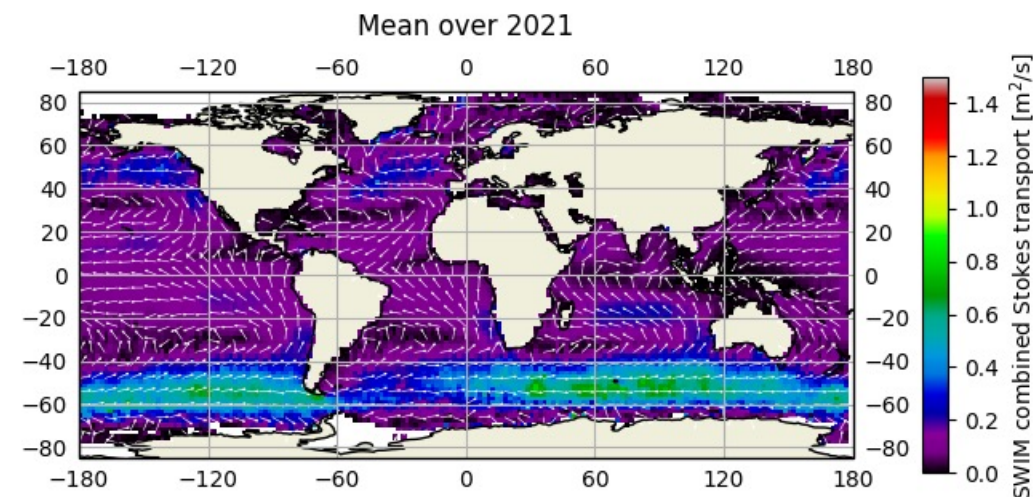
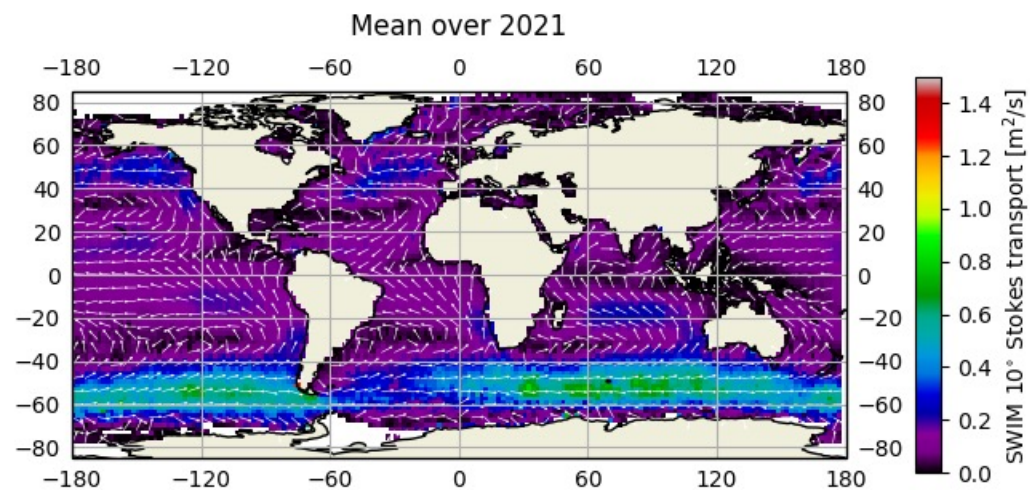
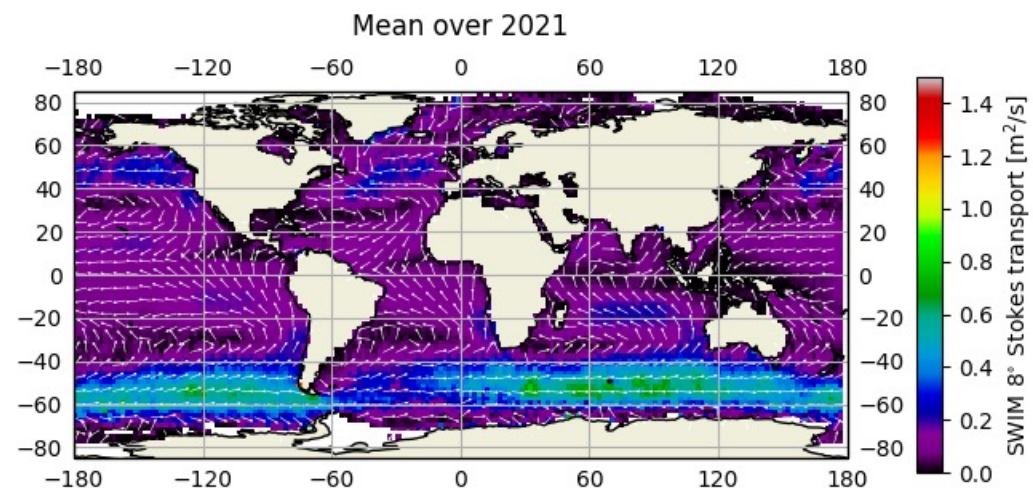
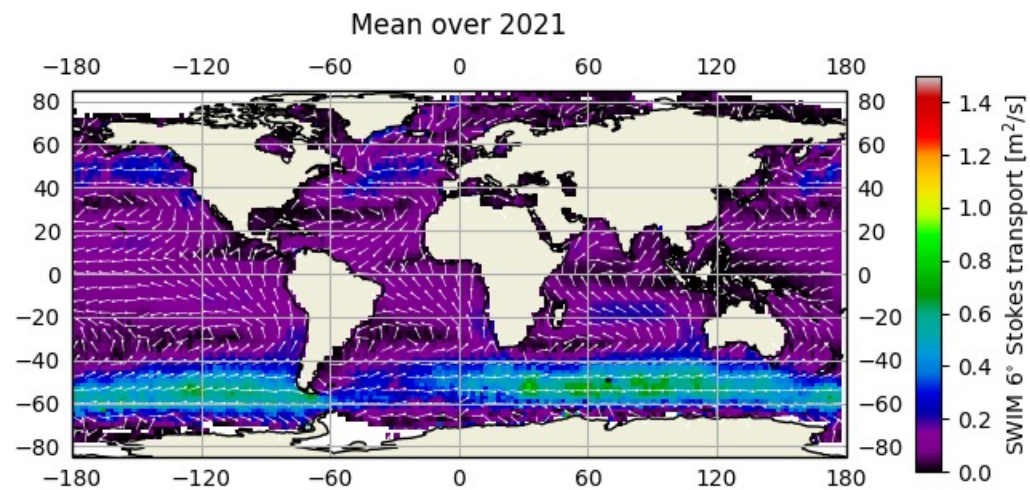
2D transport



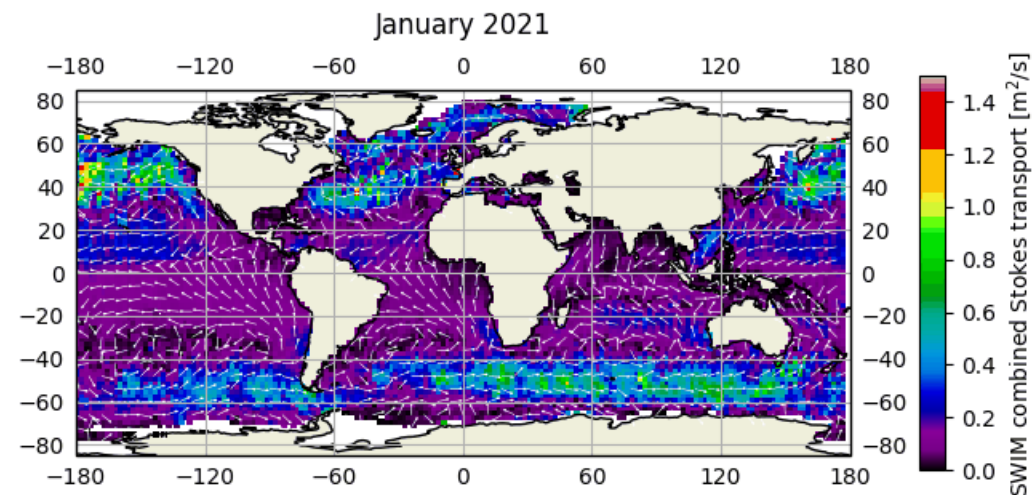
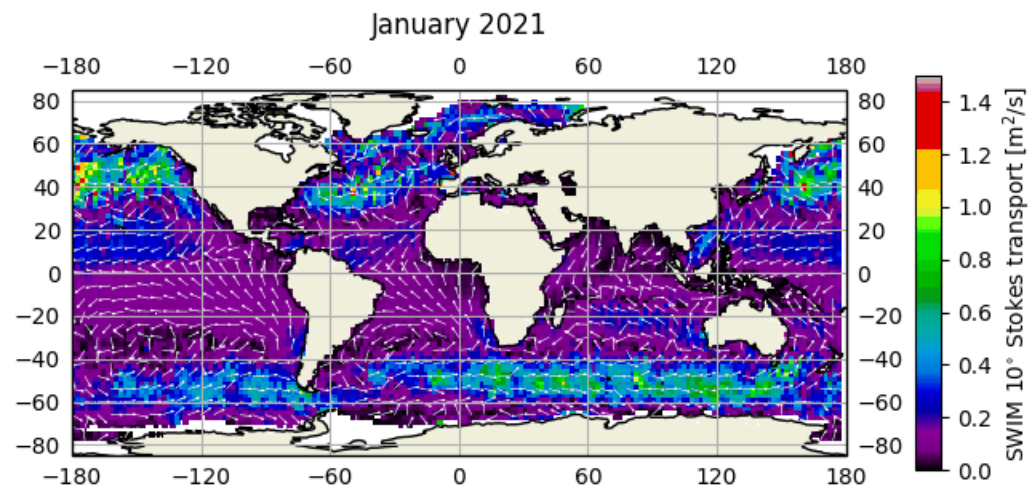
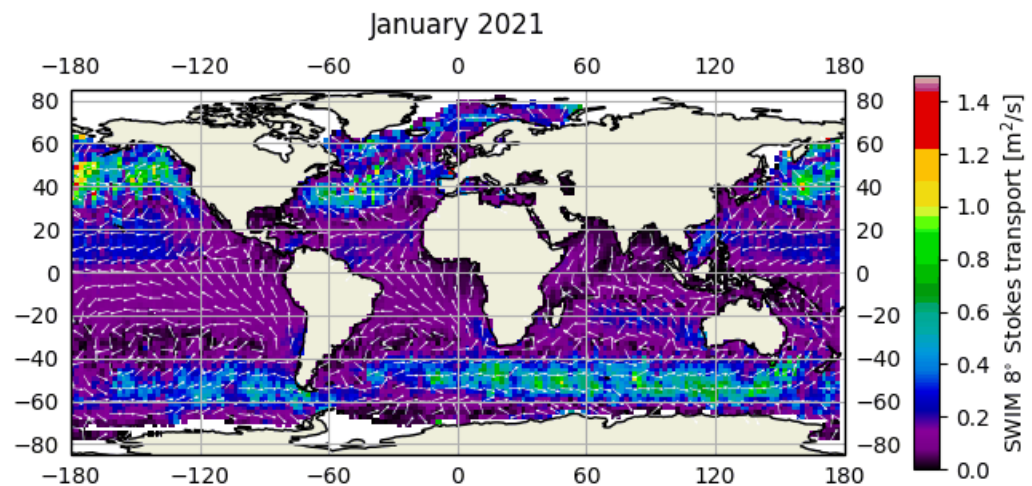
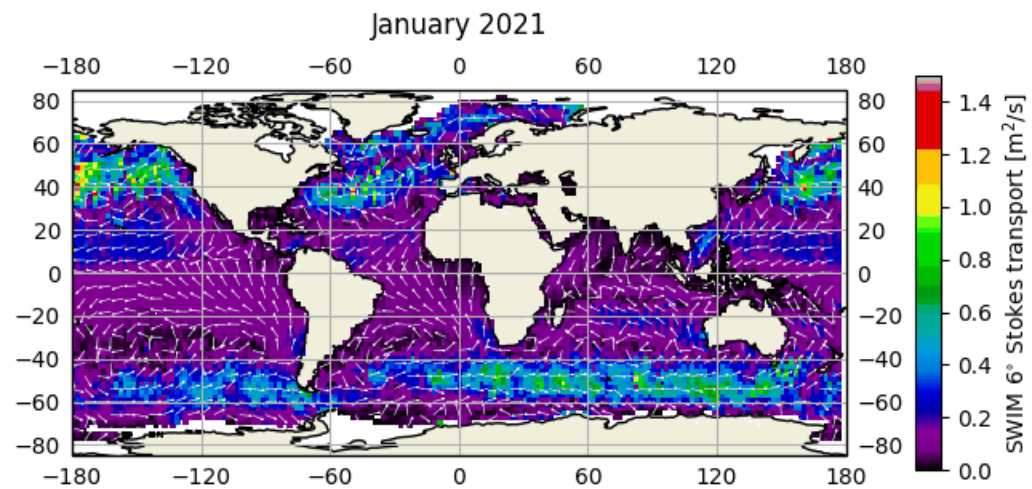
WAM 2D transport



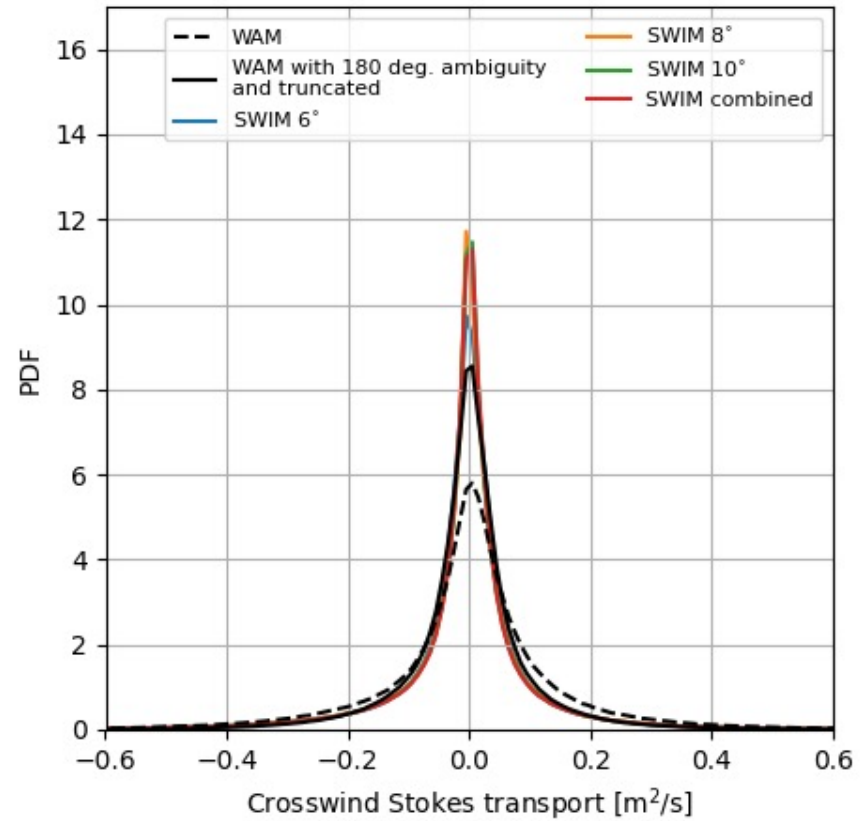
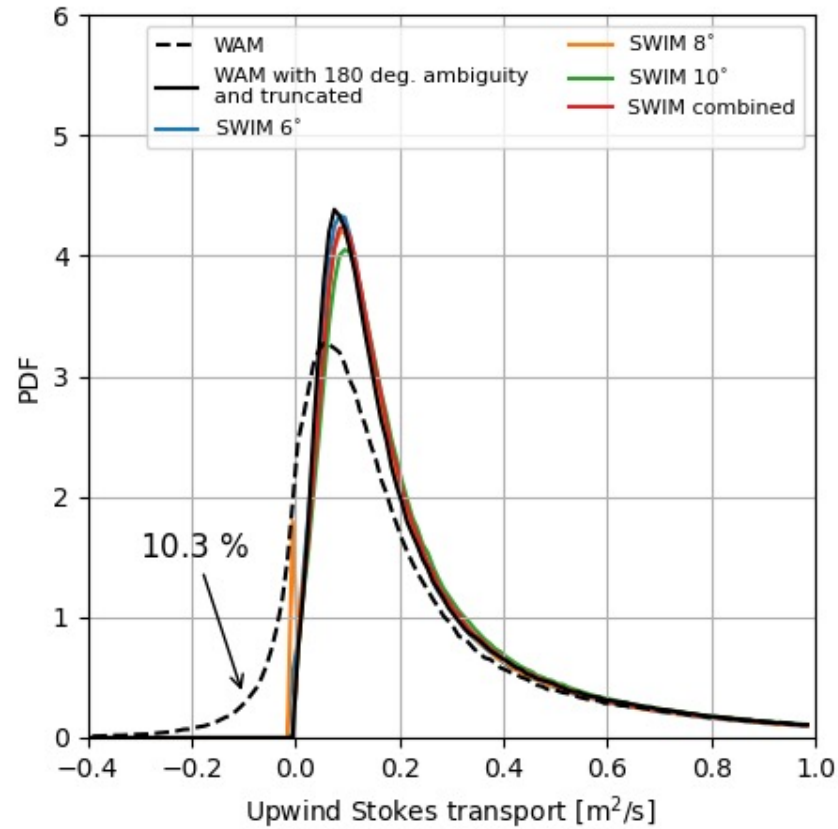
SWIM 2D transport



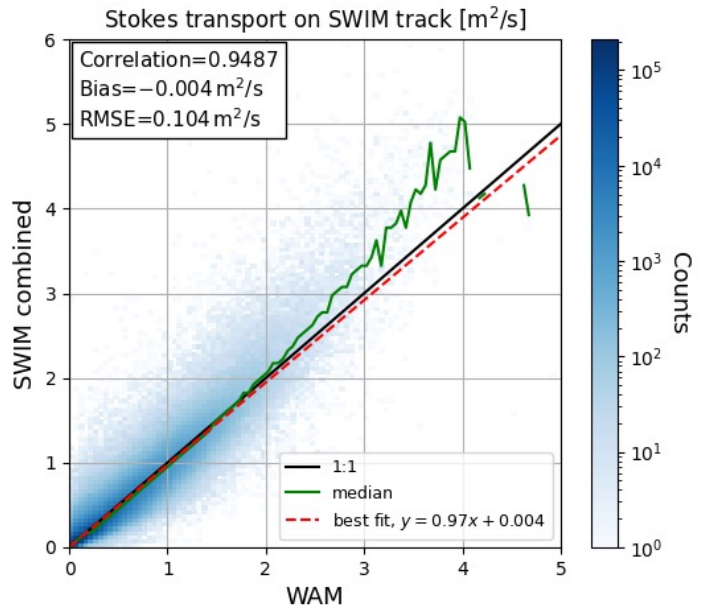
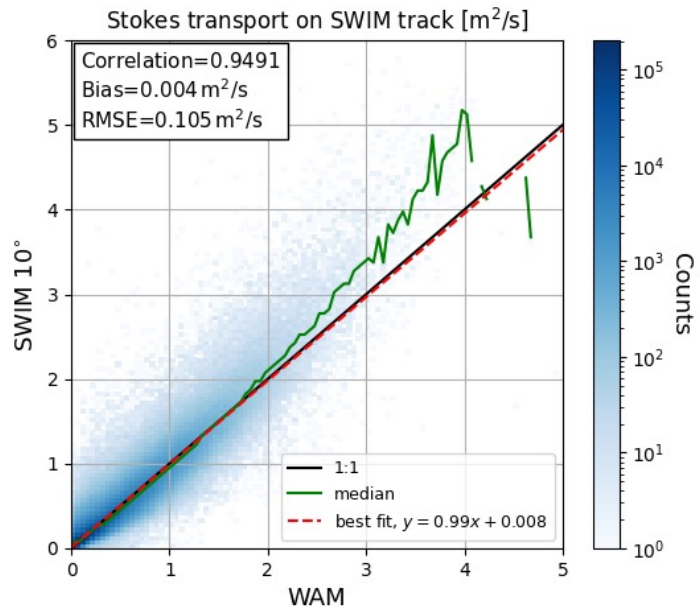
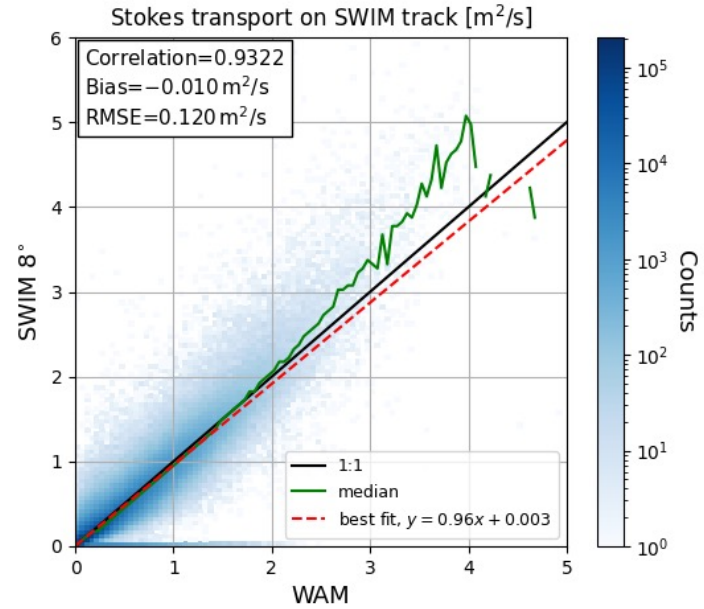
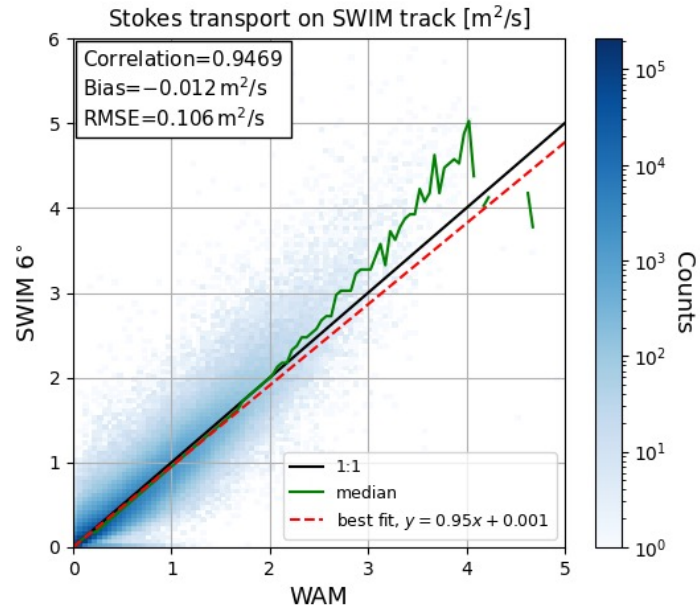
SWIM 2D transport



2D transport



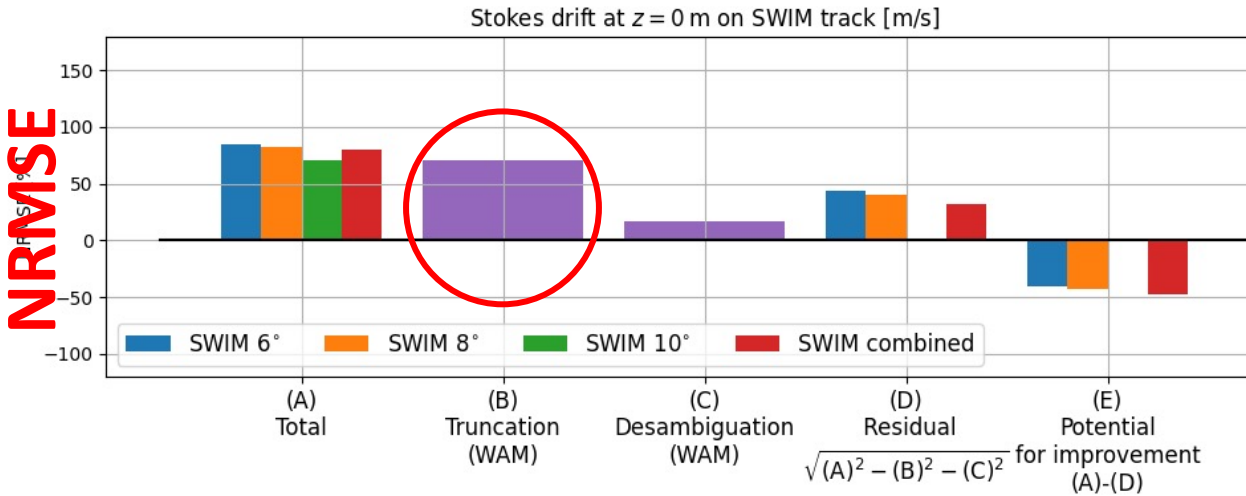
2D transport



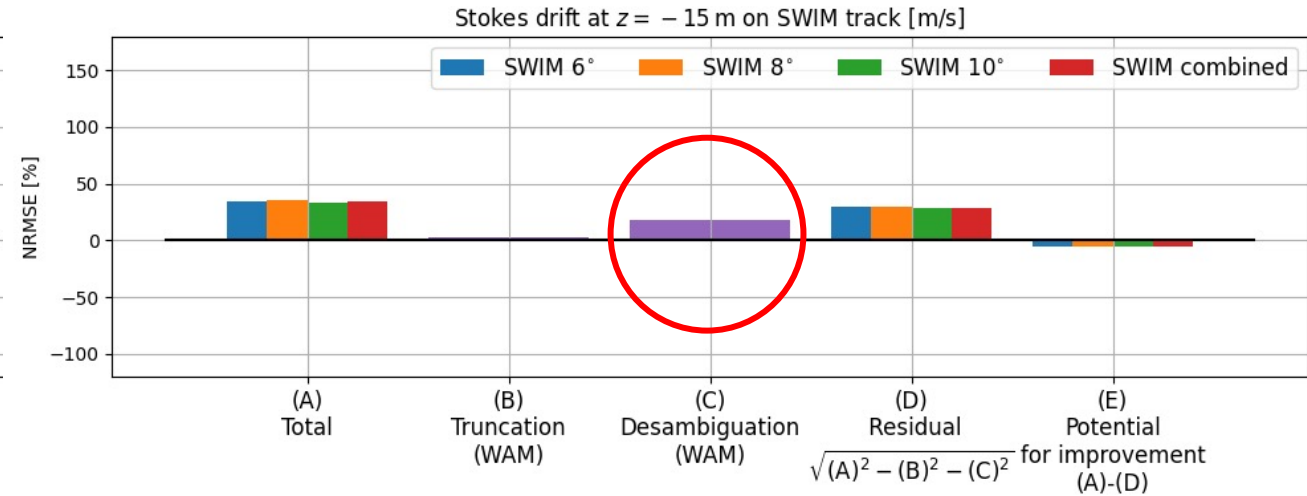
Performances - error budget with respect to WAM

NRMSE = Normalized Root Mean Square Error

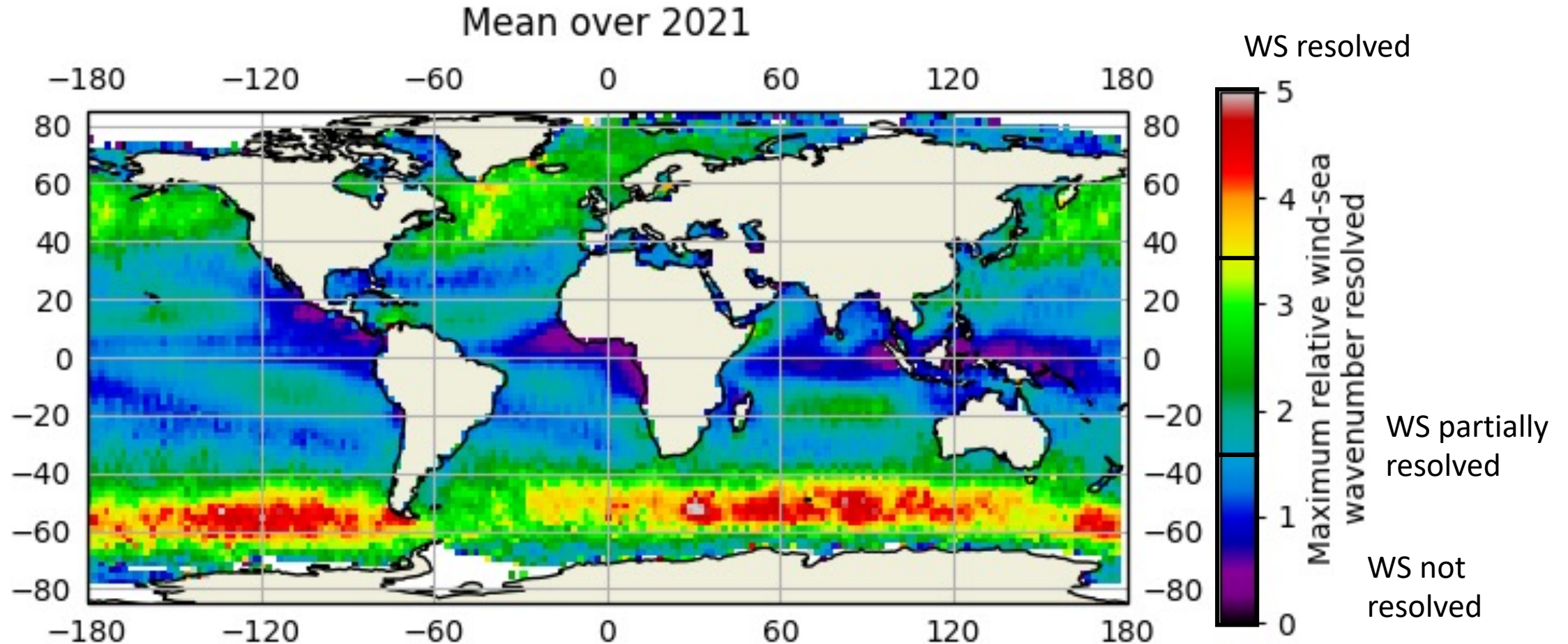
z = 0 m



z = -15 m

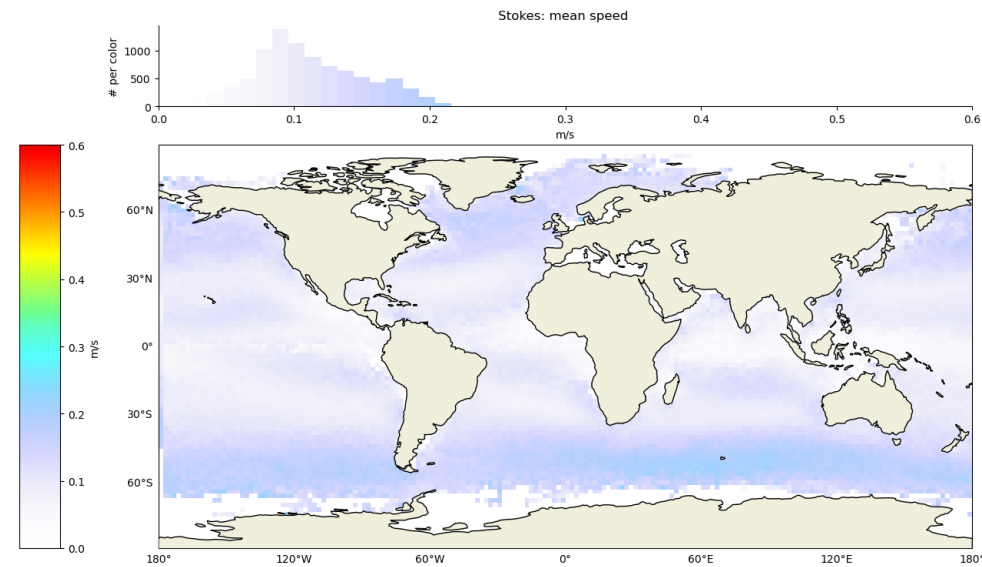
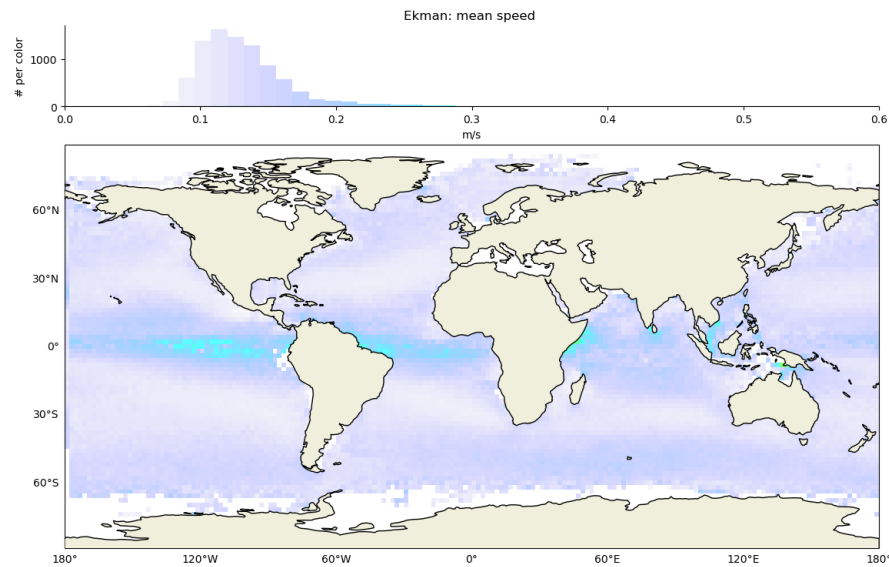
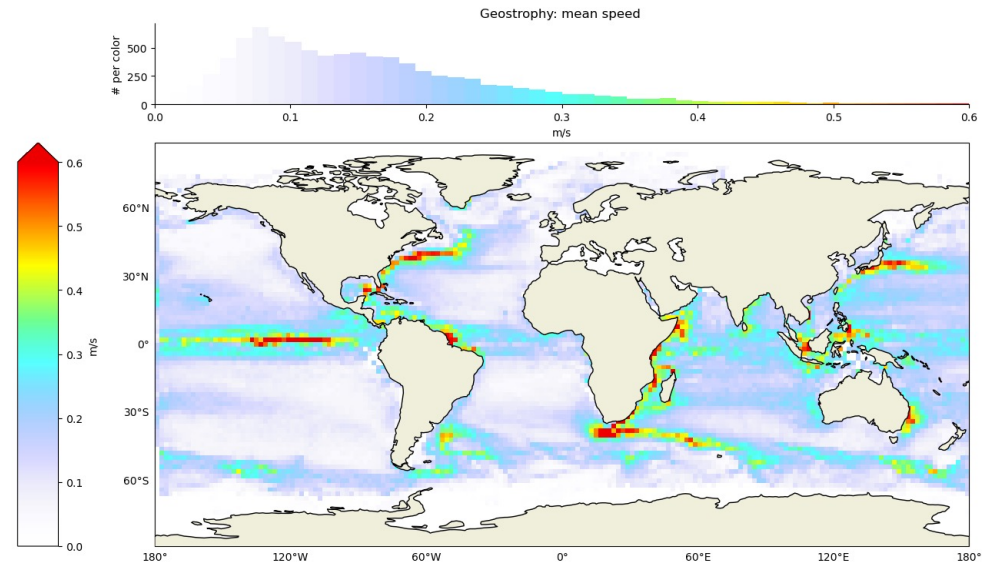
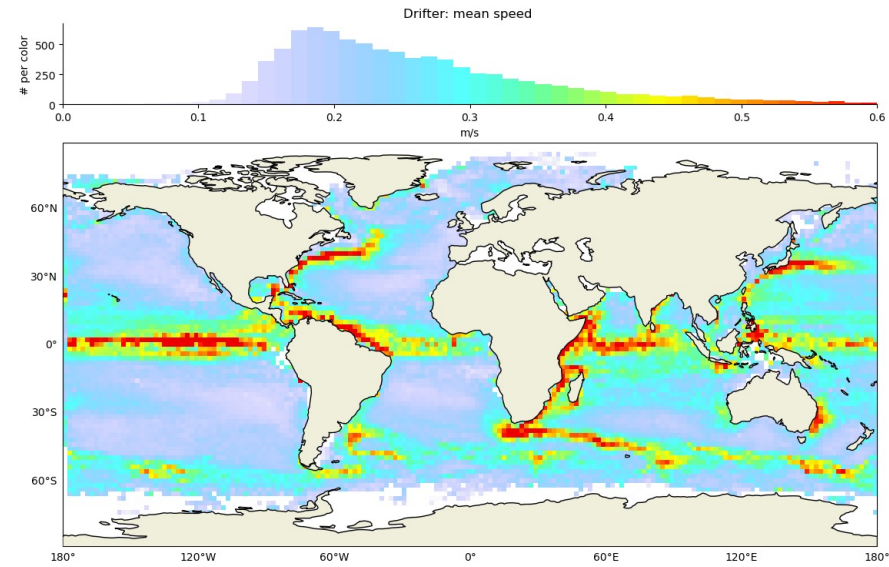


Correction proposition at the surface

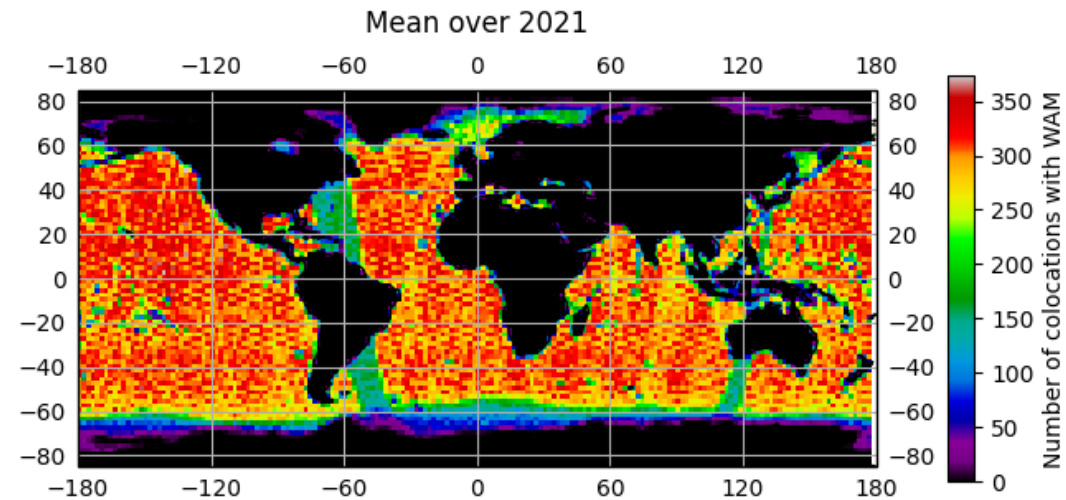
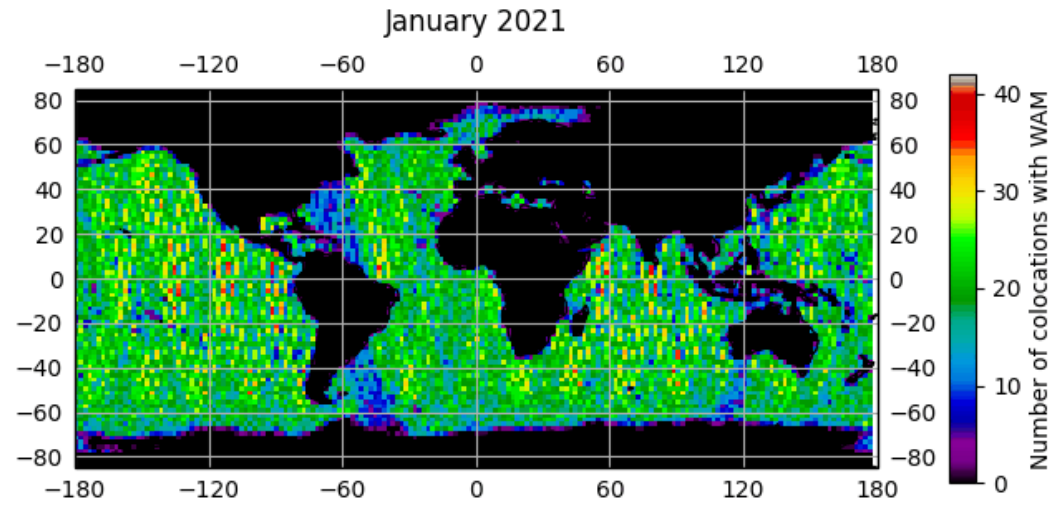


Assuming wave age = 1

Introduction – Stokes drift



Number of colocations



Wind vector

