

# Impact of nominal and measured satellite attitude on SLR- and DORIS-derived orbits of Jason satellites and altimetry results

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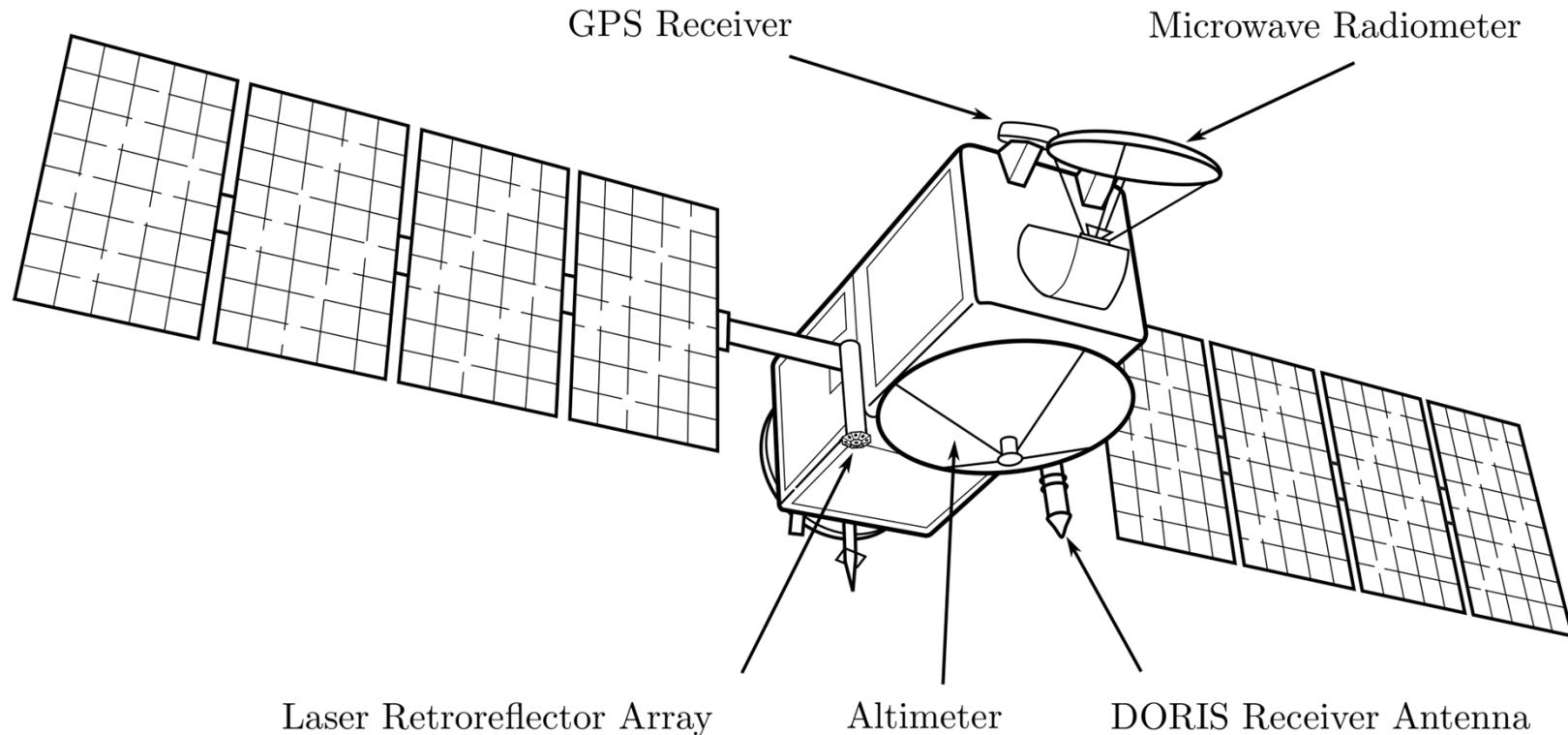
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Ocean Surface Topography Science Team Meeting (OSTST) 2019,  
21-25 October 2019, Chicago, Illinois, United States of America

# Outline

- ⇒ Importance of the knowledge on satellite attitude
- ⇒ Attitude representation and its processing at DGFI-TUM
- ⇒ Jason-1/-2/-3 satellite POD using nominal and measured satellite attitude
- ⇒ Impact of using measured attitude instead of nominal attitude on:
  - RMS fits of SLR and DORIS residuals,
  - standard deviation of single-satellite crossover differences,
  - orbit differences
- ⇒ Conclusions and outlook

# Geodetic payload of Jason satellites



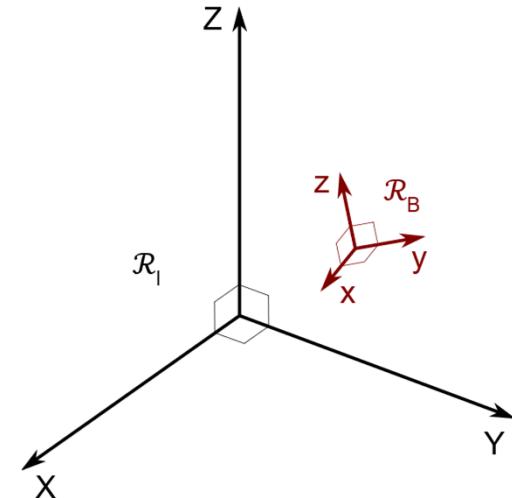
- Non-spherical satellites
- Precise information on satellite shape, size, surface optical properties, maneuvers and mass variations is required
- An information of satellite orientation (attitude) in space is required

# Attitude representations

## Different ways of attitude representation

Determination of the orientation of the satellite body reference system  $\mathcal{R}_B$  with respect to the inertial reference system  $\mathcal{R}_I$

- Euler angle and axis
- Direction cosine matrix
- Euler angles
- Quaternions



## Quaternions

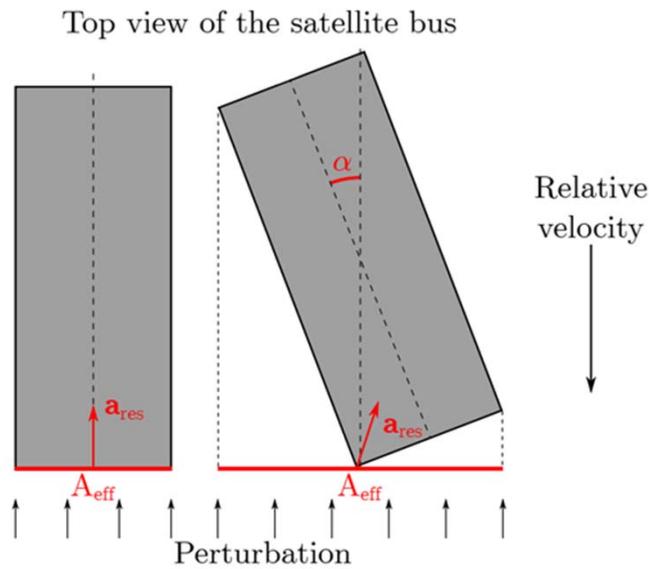
Composed of four elements  $q_s, q_x, q_y, q_z$  (the first one is scalar, the later three provide the orientation).

Defined by  $q = q_s + iq_x + jq_y + kq_z$  or  $q = [q_s \quad q_x \quad q_y \quad q_z]^T = [s \quad \mathbf{v}]^T$

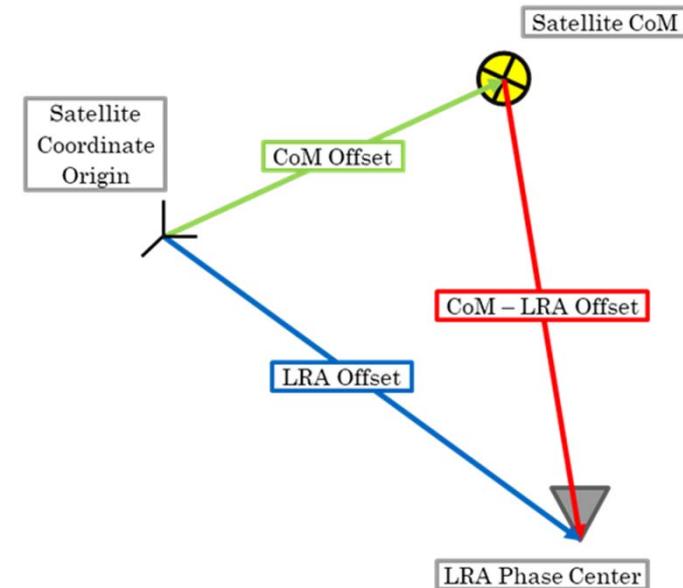
Trigonometric functions:  $q_s = \cos \frac{\theta}{2}, \quad q_x = e_1 \sin \frac{\theta}{2}, \quad q_y = e_2 \sin \frac{\theta}{2}, \quad q_z = e_3 \sin \frac{\theta}{2}$

Unit quaternions:  $|q| = \sqrt{q_s^2 + q_x^2 + q_y^2 + q_z^2} = 1$

# Importance of precise knowledge on satellite attitude for precise orbit determination



Affective satellite surface area  $A_{eff}$  of the surface forces depends on the orientation of non-spherical satellite w.r.t. perturbing force direction



Positions of the LRA and DORIS phase centers in the inertial reference frame depend on the satellite orientation in space

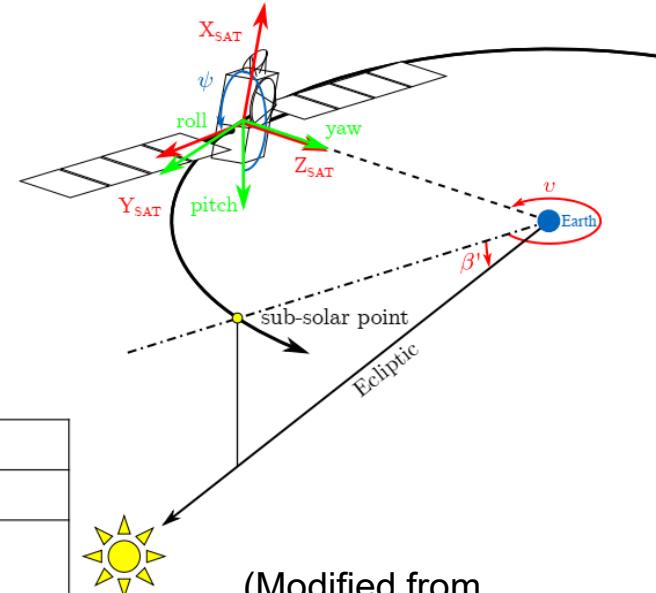
# Principle of the nominal yaw steering model for Jason satellites

Fulfillment of two prerequisites:

- Earth/nadir-pointing of the altimeter antenna
- Sun-pointing of the solar arrays

Usage of yaw steering algorithms based on those  
of TOPEX/Poseidon

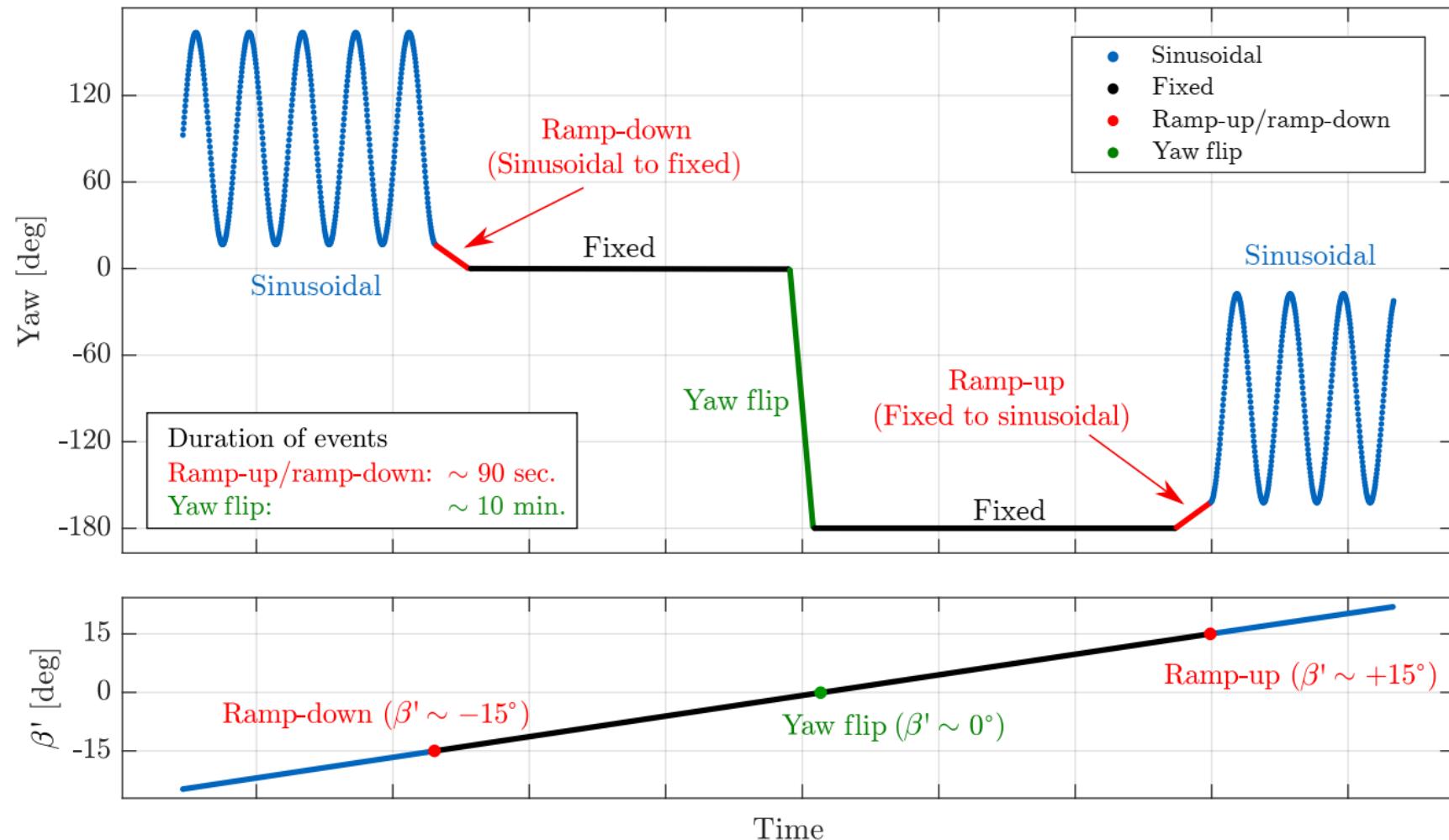
Yaw regime	Occurrence	Description
Sinusoidal	$ \beta  > 15^\circ$	Yaw sinusoidal law
Fixed	$ \beta  < 15^\circ$	Yaw = $0^\circ$ if $\beta > 0^\circ$ Yaw = $180^\circ$ if $\beta < 0^\circ$
Ramp-up	$ \beta  \geq 15^\circ$	Yaw fixed to sinusoidal
Ramp-down	$ \beta  \leq 15^\circ$	Yaw sinusoidal to fixed
Yaw flip	$ \beta  \approx 0^\circ$	Yaw = $0^\circ$ if $\beta > 0^\circ$ Yaw = $180^\circ$ if $\beta < 0^\circ$



(Modified from  
Cerry et al., 2010)

$$yaw_{nominal} = \psi_{nominal} = \begin{cases} 90^\circ - (90^\circ - \beta') \sin \nu & , \text{ if } \beta' > 15^\circ \\ -90^\circ + (90^\circ + \beta') \sin \nu & , \text{ if } \beta' < -15^\circ \end{cases}$$

# Changes of the yaw and $\beta'$ angles in the nominal yaw steering model



# Attitude processing at DGFI-TUM



Attitude data loading (determination of GPS week relevant files)

Combination of attitude quaternion files and a file containing solar panel orientation angles in a unique attitude file for each GPS week

Appropriate interpolation when varying epochs are given

## Data analysis

- Elimination of duplicate epochs
- Removal of invalid data
- Detection and rejection of outliers (defined by the user)
- Removal of quaternions without the norm 1
- Temporal resampling
- Removal of epochs within gaps of the other data set
- Determination of missing epochs in one data set with respect to the other one

## Data interpolation

- Quaternions: Spherical linear quaternion interpolation
- Solar panel angles: linear interpolation

# Precise orbit determination of Jason satellites using nominal and measured satellite attitude



Satellites and time spans analyzed:

- Jason-1 (January 13, 2002 to June 29, 2013)
- Jason-2 (July 20, 2008 to January 9, 2019)
- Jason-3 (February 17, 2016 to January 9, 2019)

Observations type used:

- SLR
- DORIS (for Jason-1 and Jason-2 only) in the IDS 2.2 format

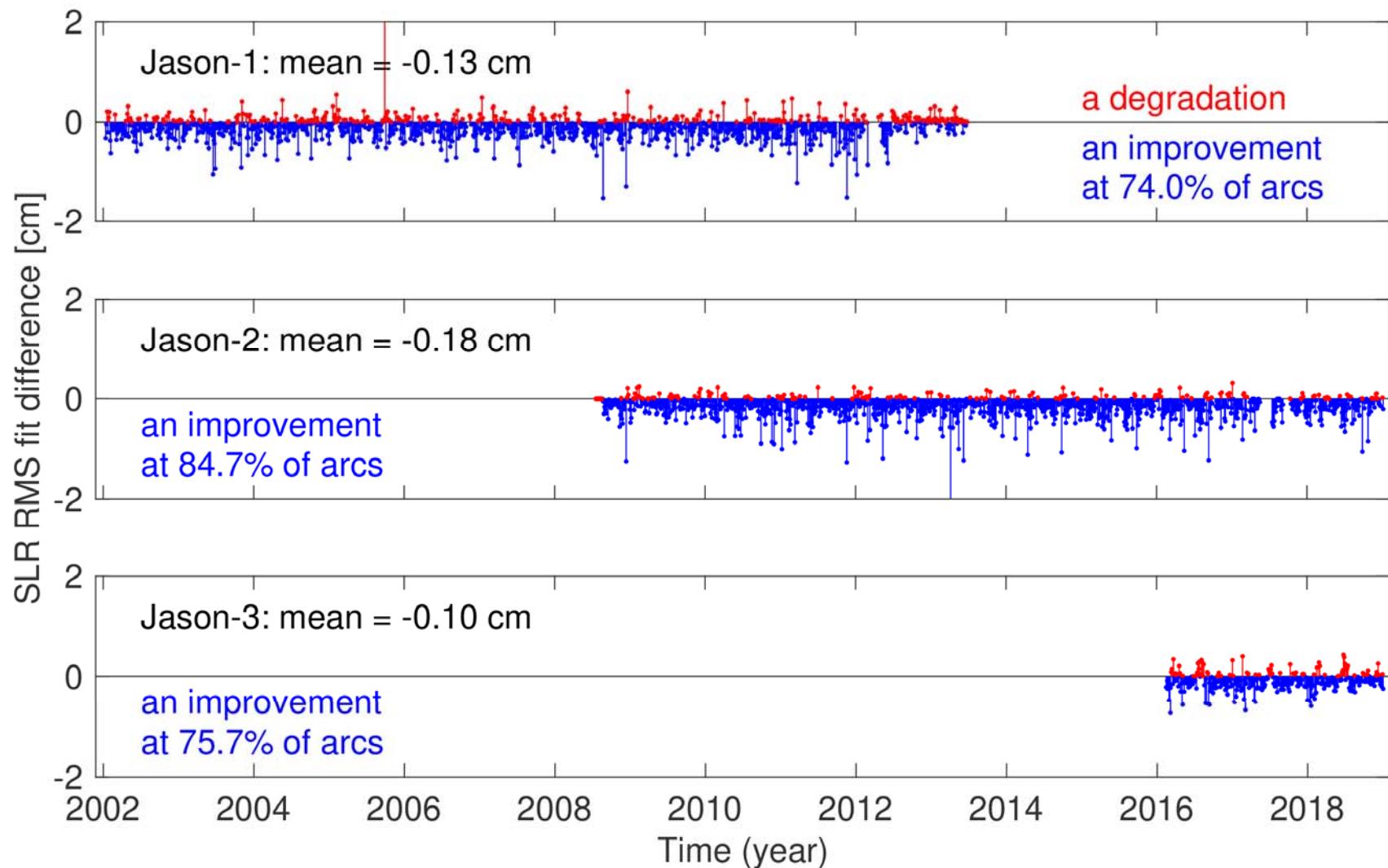
Software used: “DGFI Orbit and Geodetic parameter estimation Software”.

Background models and reference frames used:

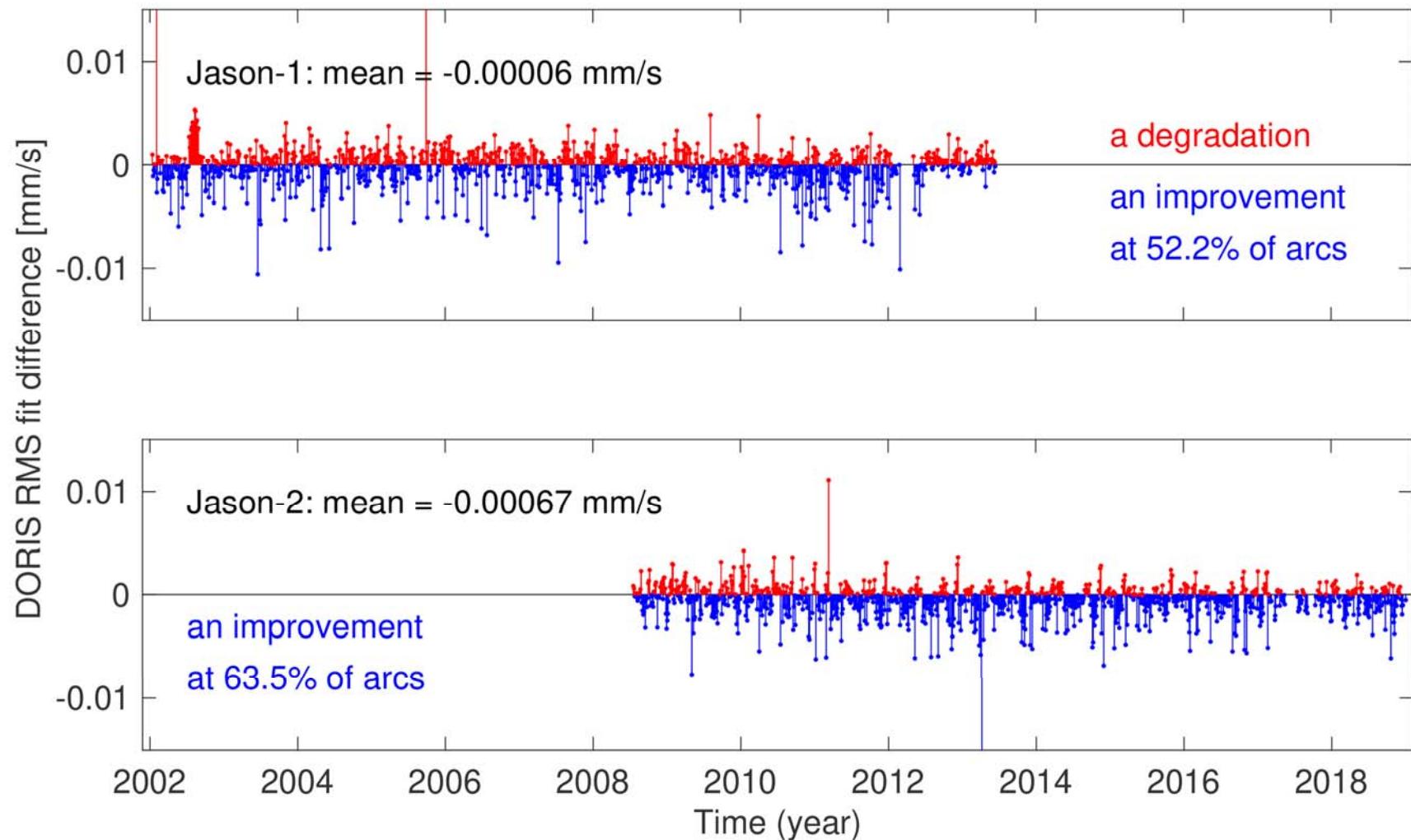
- Up-to-date models consistent with the IERS Conventions (2010)
- SLRF2014 for SLR and DPOD2014 for DORIS stations

Estimated parameters: Keplerian elements, solar radiation pressure scaling coefficient, Earth albedo scaling coefficient, along-track and normal empirical acceleration, atmospheric drag scaling coefficient (every 12 h); station frequency bias (for DORIS data, 1 per path)

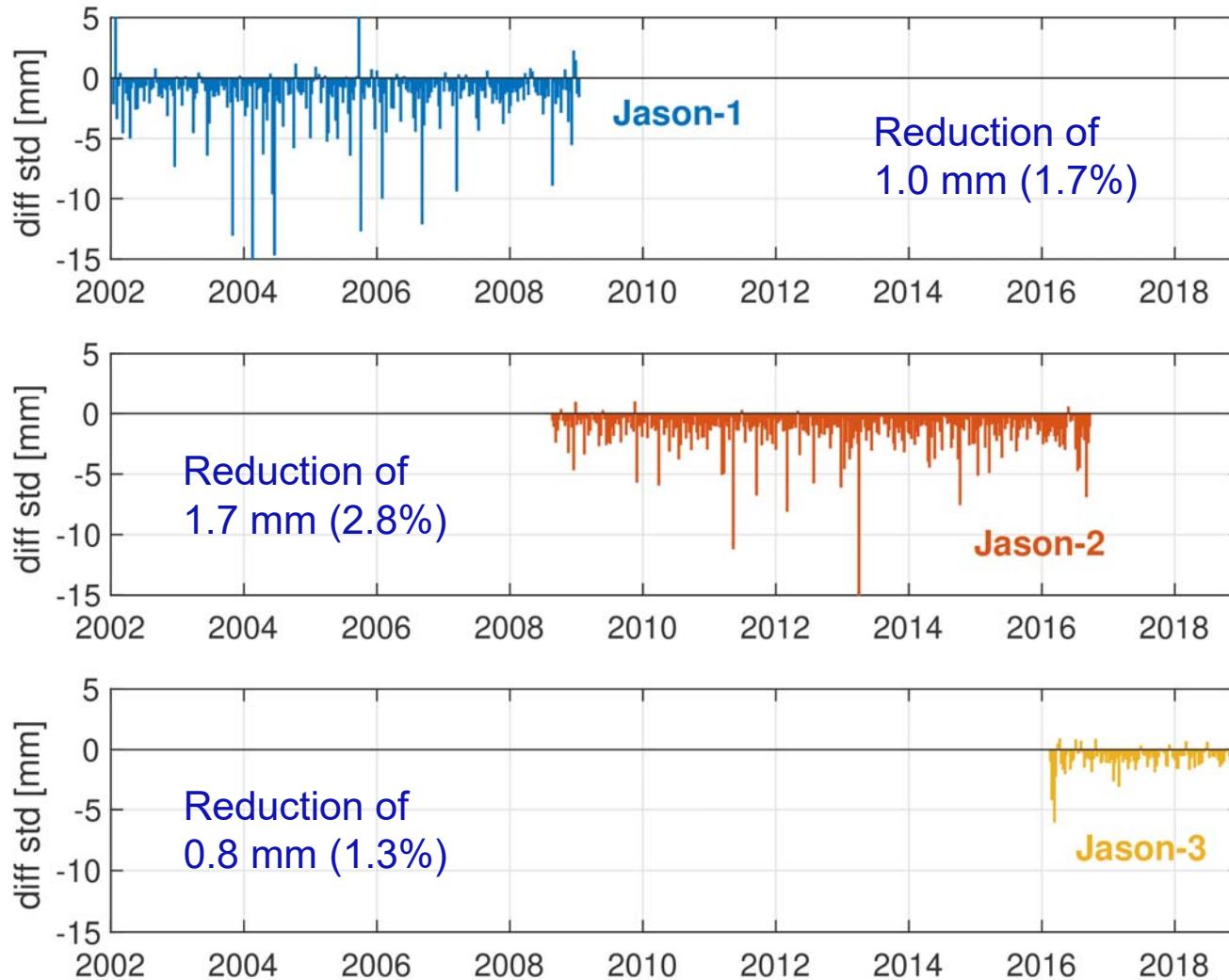
# Differences of SLR RMS fits of SLR-only orbits: “measured attitude” versus “nominal attitude”



# Differences of DORIS RMS fits of DORIS-only orbits: “measured attitude” versus “nominal attitude”



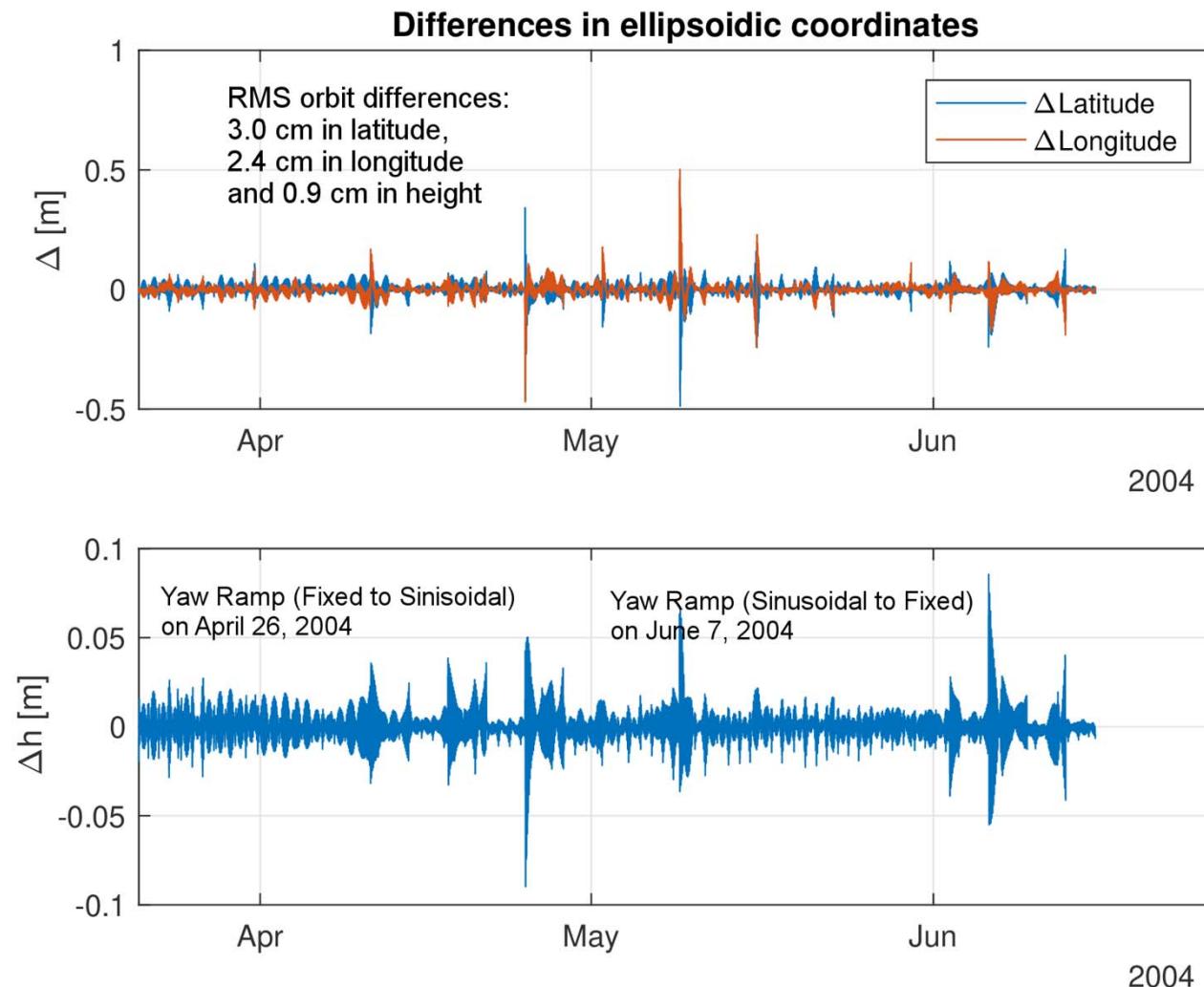
# Differences of standard deviation of single-satellite crossover differences



SLR-only  
orbits

An  
improvement  
when using  
“measured  
attitude”  
instead of  
“nominal  
attitude”

# Differences of Jason-1 satellite positions of two orbits: “measured attitude” versus “nominal attitude”



SLR-only orbits

The differences up to a few cm in the height direction

**Change  $|\beta'| < 15^\circ$  to  $|\beta'| < 30^\circ$  of the fixed law**

**for Jason-2 and Jason-3 from July 2017.**

**RMS-differences of Jason-1/-2/-3 satellite positions**

**of SLR-data based orbits: “measured” versus “nominal attitude”**

Satellite and $\beta'$ angle	Latitude (cm)	Longitude (cm)	Height (cm)
Jason-1 $ \beta'  < 15^\circ$	2.8	2.2	0.8
Jason-2 $ \beta'  < 15^\circ$	2.4	2.0	0.9
Jason-2 $ \beta'  < 30^\circ$	1.8	1.4	0.6
Jason-3 $ \beta'  < 15^\circ$	2.5	2.0	0.9
Jason-3 $ \beta'  < 30^\circ$	1.6	1.3	0.6

Increase of the maximum beta-prime angle for fixed yaw from  $15^\circ$  to  $30^\circ$  for Jason-2 and Jason-3 in July 2017 reduces the RMS differences between the SLR-data based orbits computed using nominal and measured attitude after that change by 25-36%.

Change  $|\beta'| < 15^\circ$  to  $|\beta'| < 30^\circ$  of the fixed law

for Jason-2 and Jason-3 from July 2017.

RMS-differences of Jason-1 and Jason-2 satellite positions  
of DORIS-data based orbits: “measured” versus “nominal attitude”

Satellite and $\beta'$ angle	Latitude (cm)	Longitude (cm)	Height (cm)
Jason-1 $ \beta'  < 15^\circ$	2.0	1.5	0.65
Jason-2 $ \beta'  < 15^\circ$	1.8	1.5	0.67
Jason-2 $ \beta'  < 30^\circ$	1.5	1.1	0.64

Use of the nominal attitude instead of measured attitude causes RMS differences of the DORIS-data based orbits of Jason-1 and Jason-2 of about 6-7 mm.

Increase of the maximum beta-prime angle for fixed yaw from  $15^\circ$  to  $30^\circ$  for Jason-2 in July 2017 reduces the RMS differences between the DORIS-data based orbits computed using nominal and measured attitude after that change by 4, 16 and 23% in the height, latitude and longitude directions, respectively.

# Conclusions and outlook

- ⇒ Precise knowledge on the **Jason satellite attitude** is important for precise orbit determination of these satellites
- ⇒ Using **measured satellite attitude** (satellite body orientation in the quaternion form and solar panel angles) instead of nominal attitude
  - **reduces SLR RMS fits** at 74-85% of processed arcs by 1.0-1.8 mm (5-8%),
  - **slightly reduces DORIS RMS fits** at 52-64% of processed arcs,
  - **reduces standard deviation** of single-satellite **crossover differences** by 0.8-1.7 mm (1.3-2.8%)
  - causes the **RMS differences** of Jason-1/-2/-3 **satellite coordinates** in the height direction at the level of about 6-9 mm for the SLR data based orbits and of about 6-7 mm for the DORIS data based orbits
- ⇒ Change of the **maximum  $\beta'$  angle for the fixed law** from  $15^\circ$  to  $30^\circ$  for Jason satellites reduces the RMS differences of satellite coordinates computed using nominal and measured attitude by 25-36% for SLR-data based orbits and by 4-23% for DORIS-data based orbits.
- ⇒ Preprocessed at DGFI-TUM attitude data of Jason-1, -2 and -3 will be made available  
**(soon!)**

# Reference



Julian Zeitlhöfler (2019) Nominal and observation-based attitude realization for precise orbit determination of the Jason satellites, Master's thesis, Technical University of Munich, Department of Civil, Geo and Environmental Engineering, Deutsches Geodätisches Forschungsinstitut (DGFI-TUM).